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# The Ionosphere

## Origins, Structure, and Variability

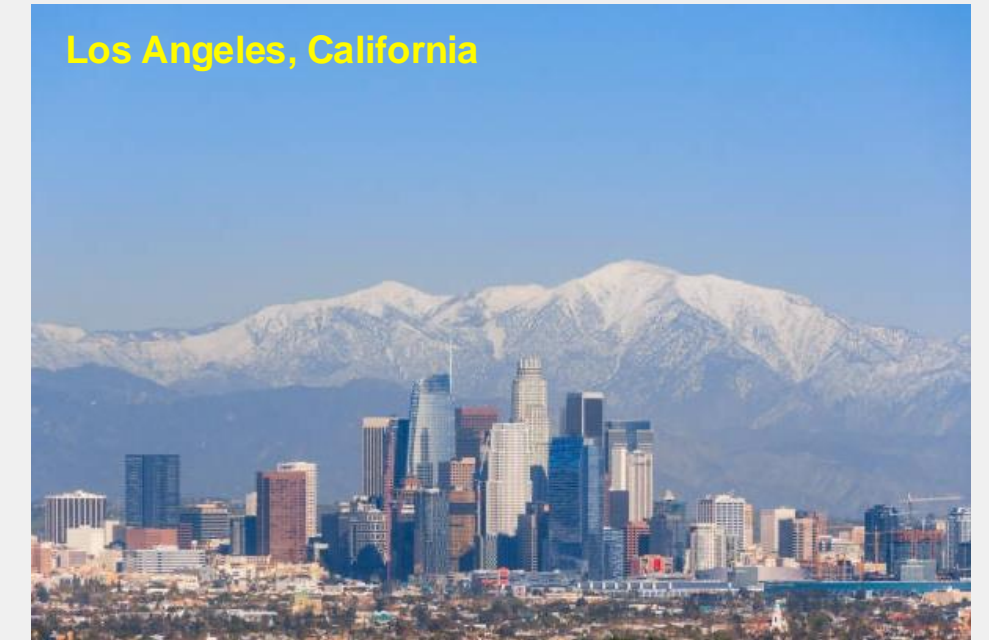
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Robert A. Marshall



# A bit about me

- ❖ **Grew up in Vancouver, BC, Canada**
- ❖ BS: Electrical Engineering, University of Southern California
- ❖ MS/PhD: Electrical Engineering, Stanford University
- ❖ Postdoc (< 2 years) at Boston University
- ❖ Research Associate (4 years) back at Stanford
- ❖ **Now 9 years at University of Colorado Boulder, Aerospace Engineering Sciences**
  - ❖ Tenured in 2022
  - ❖ Sabbatical in 2023: Orléans, France
  - ❖ Associate Chair for Graduate Studies: 2023—present







### PhD students



Alex  
Wold



James  
Cannon



Paraksh  
Vankawala



Wyatt  
Spies

### Research Engineers



Sebastian  
Wankmueller



Siwani  
Regmi

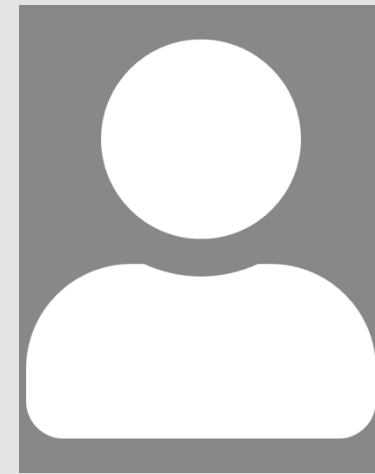


Conor  
Cunningham

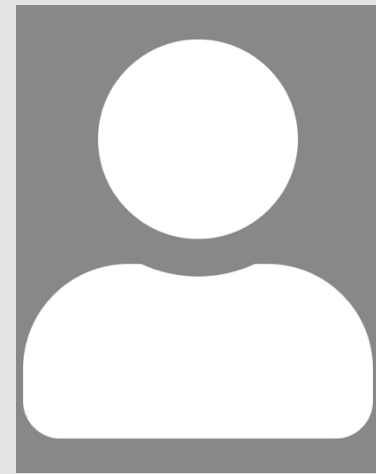


Joe  
Buescher

### Undergraduates



Julia  
Claxton



Anant  
Telikicherla



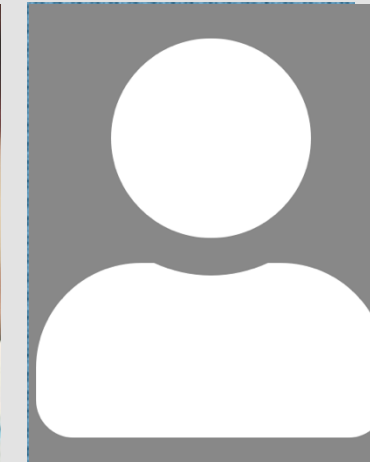
Tzu-Hsun  
Kao



Tai  
Matayay



Ryan  
Dick



Ash  
Tribble

### Postdoctoral Scholars



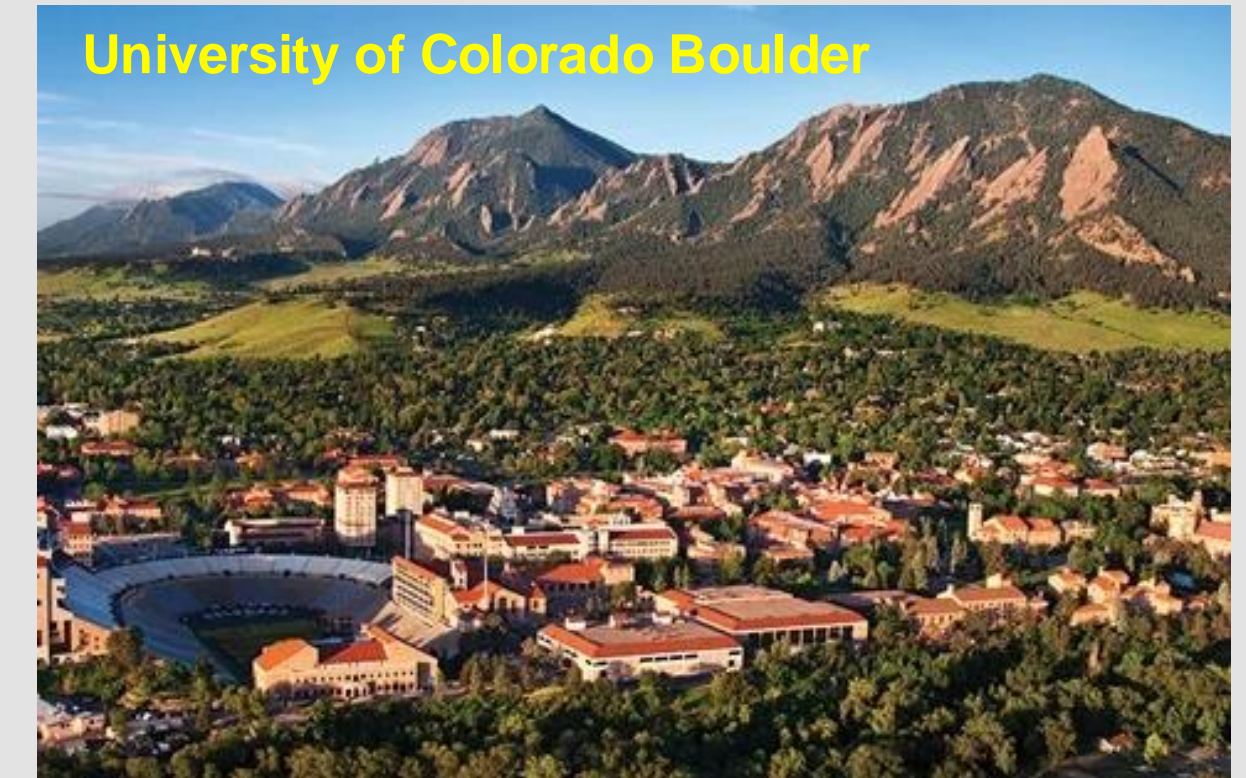
Alex  
Shane



Carolina  
Peña

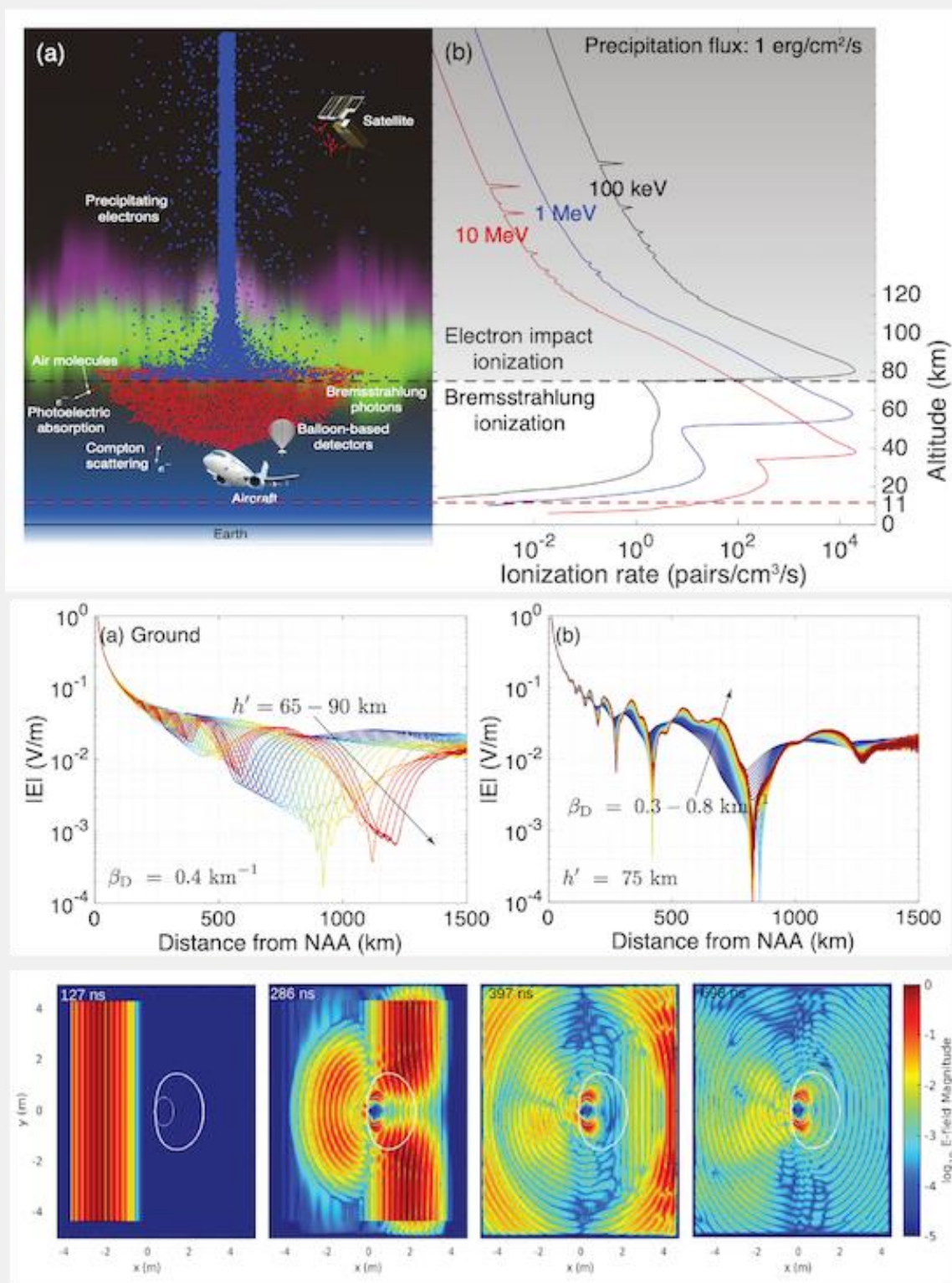
### LAIR Alumni:

- 4 postdocs that have moved on
- 6 PhDs graduated
- 4 MS theses
- 20+ undergraduates

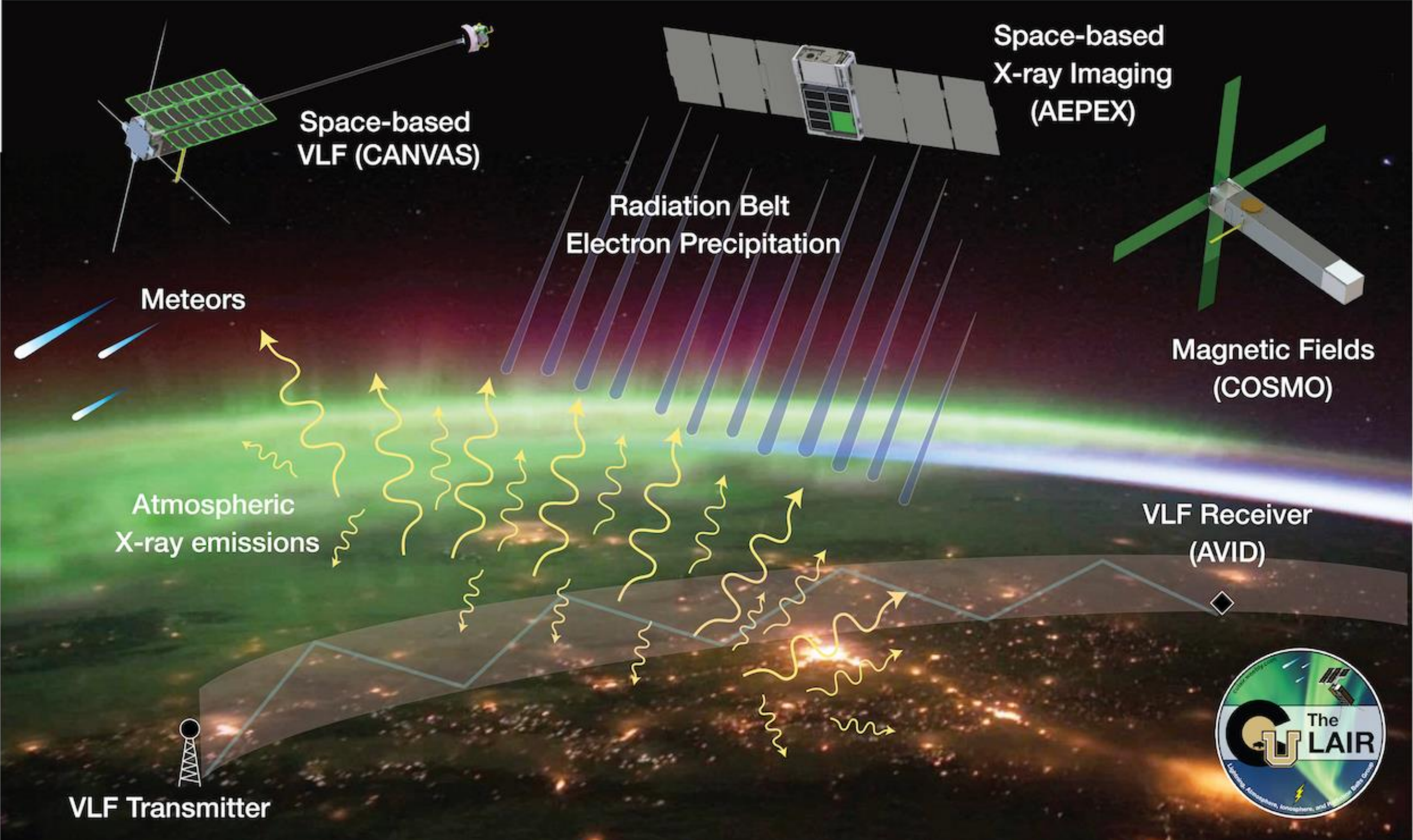




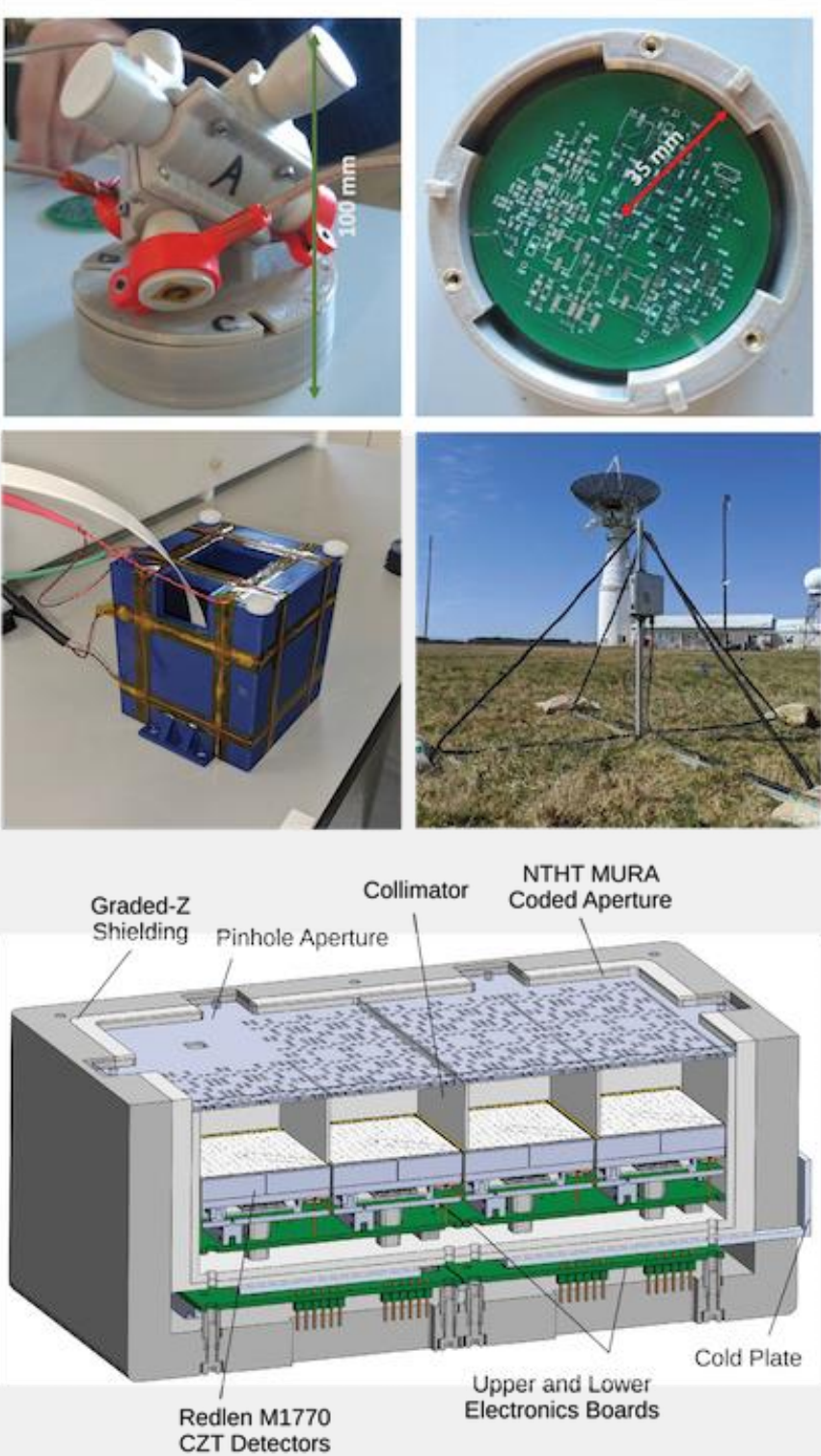
# The LAIR Research Overview



Modeling, Simulation,  
and Data Analysis



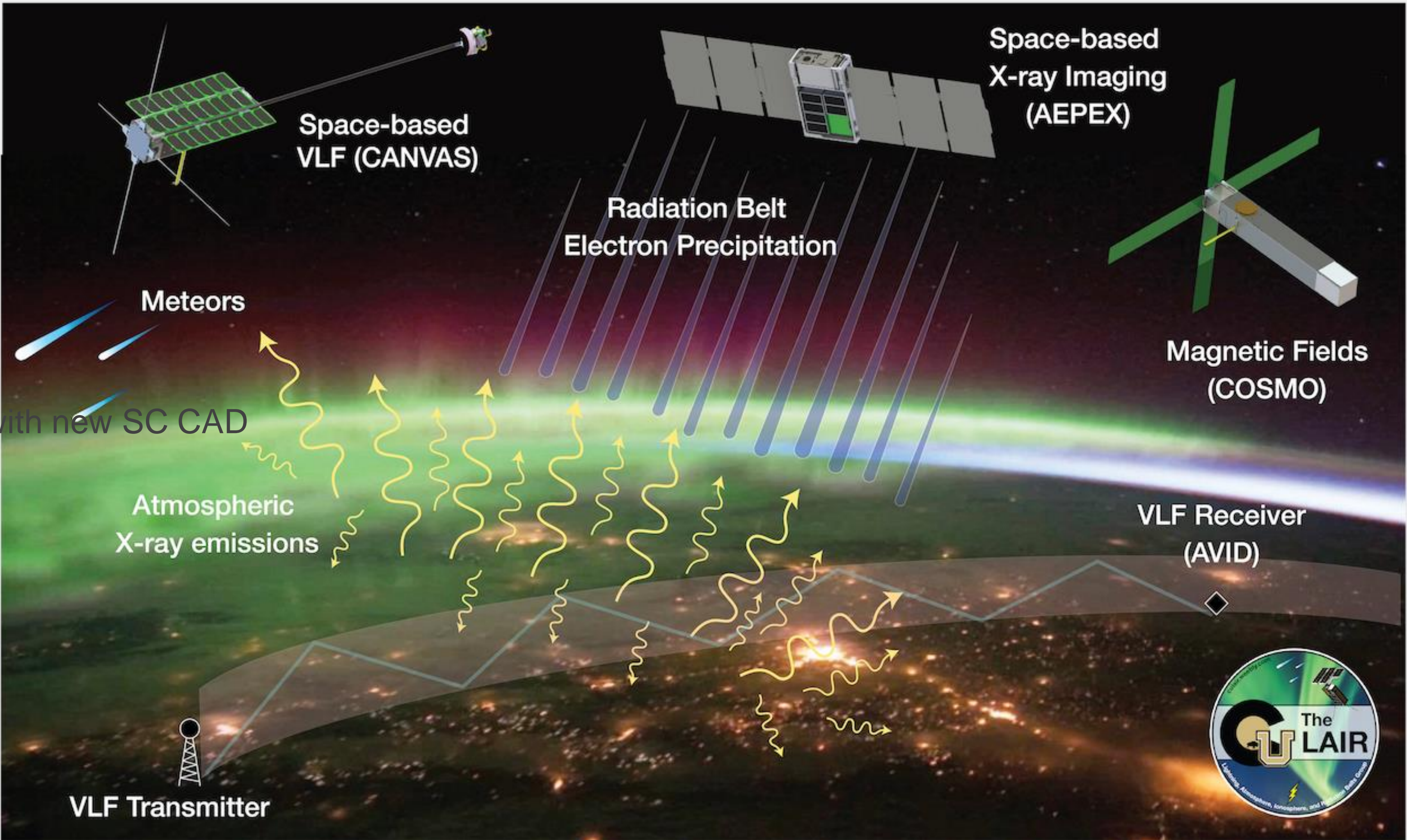
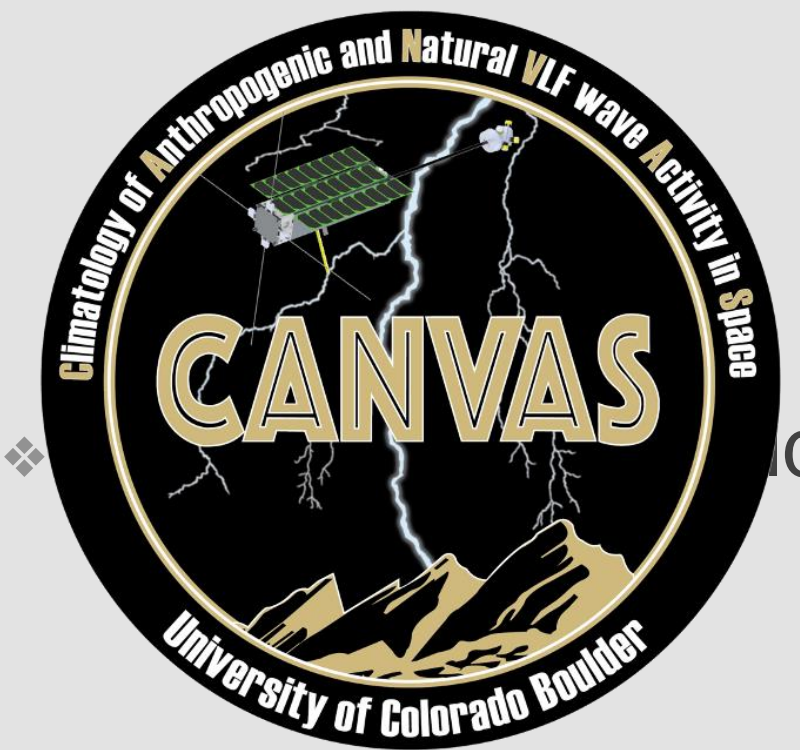
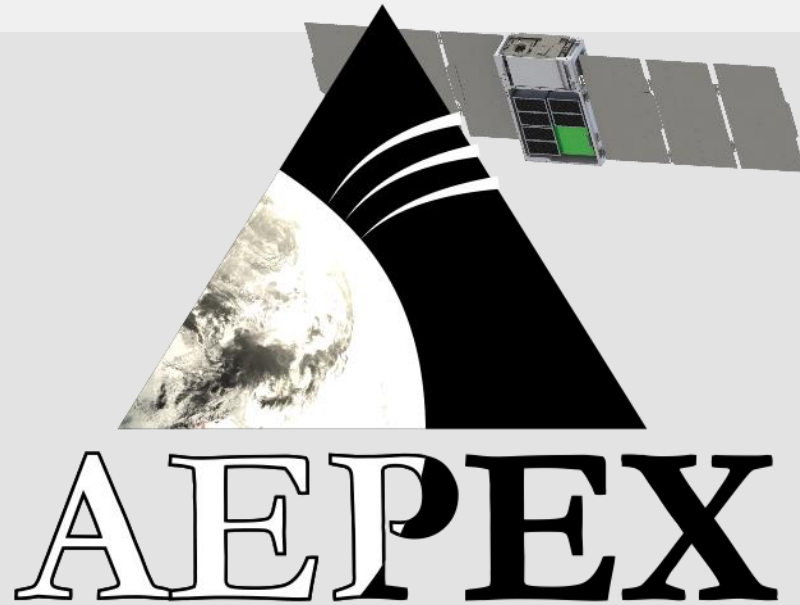
CubeSats for Space Science



Instrumentation



# CubeSats for Space Science





# Ionosphere Lectures: Goals

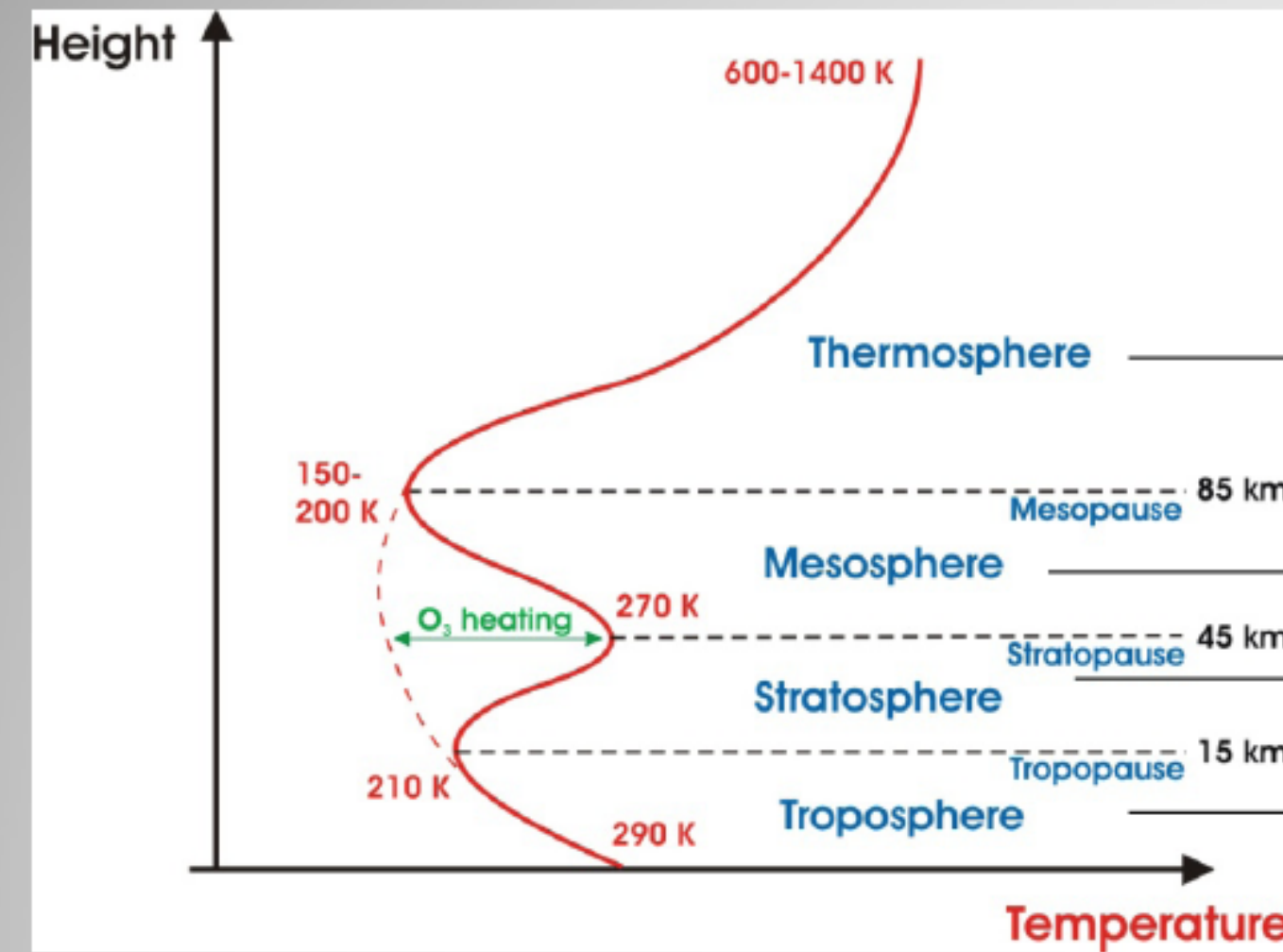
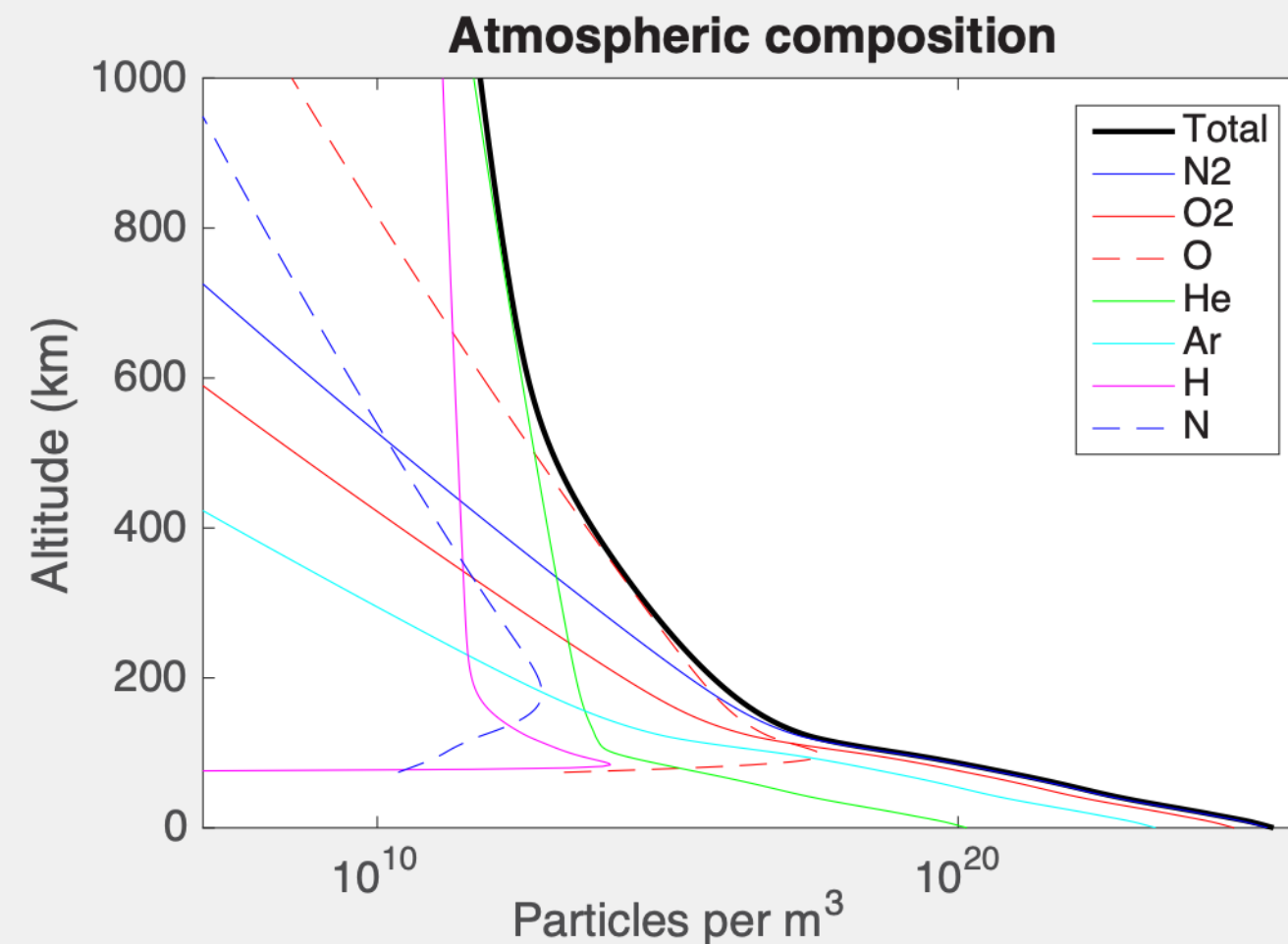
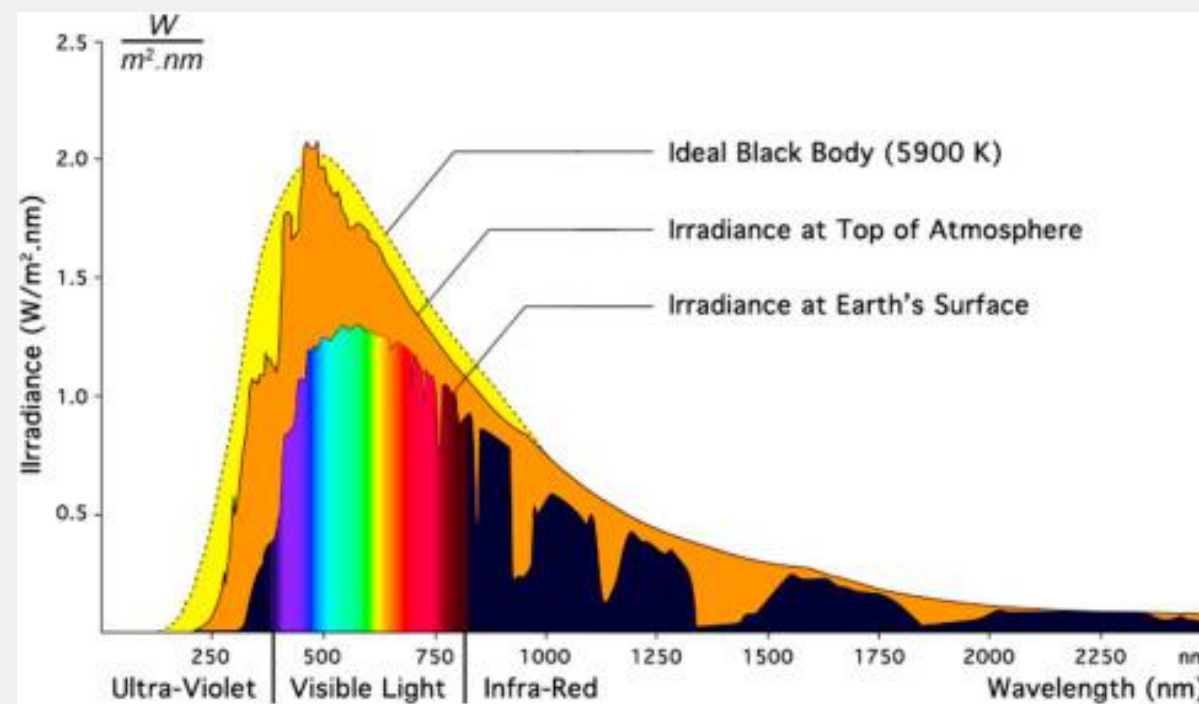
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- ❖ **Understand basic physics of the Earth's ionosphere**
  - ❖ Origin, composition, layers
  - ❖ Variations: diurnal, seasonal, solar cycle, plus other anomalies
- ❖ **Effects of the Ionosphere on Spacecraft and technology**
  - ❖ Radio communications and GPS
- ❖ **Comparative Ionospheres: Jupiter and Mars**



# Origin of the Ionosphere

- ❖ The Ionosphere is a product of two regions: the **Sun** and the **Atmosphere**



## Troposphere:

- Energy sources:
  - Planetary surface absorption (IR, visible), convection & conduction to atmosphere
  - Atmospheric absorption of terrestrial and solar IR
  - Latent heat release by  $H_2O$
- Energy sinks:
  - IR radiation
  - Evaporation of  $H_2O$

## Thermosphere:

- Energy sources:
  - Absorption of EUV (20-100 nm; photoionizing O,  $O_2$ ,  $N_2$ ) and UV (120-200 nm), photodissociating  $O_2$ , leading to chemical reactions and particle collisions, liberating energy
  - Joule heating by auroral electrical currents
  - Particle precipitation from the magnetosphere
  - Dissipation of upward propagating waves (tides, planetary waves, gravity waves)
- Energy sinks:
  - Thermal conduction into the mesosphere, where energy is radiated by  $CO_2$ ,  $O_3$  and  $H_2O$
  - IR radiation by  $CO_2$ , NO, O

## Mesosphere:

- Energy sources:
  - Some UV absorption by  $O_3$  (lower heights)
  - Heat transport down from thermosphere (minor, upper heights only)
  - Chemical heating
- Energy sinks:
  - IR radiation by  $CO_2$ ,  $H_2O$ , OH

## Stratosphere:

- Energy sources:
  - Strong absorption of UV by ozone (causing stratopause temperature peak)
- Energy sinks:
  - IR radiation by  $O_3$ ,  $CO_2$ ,  $H_2O$



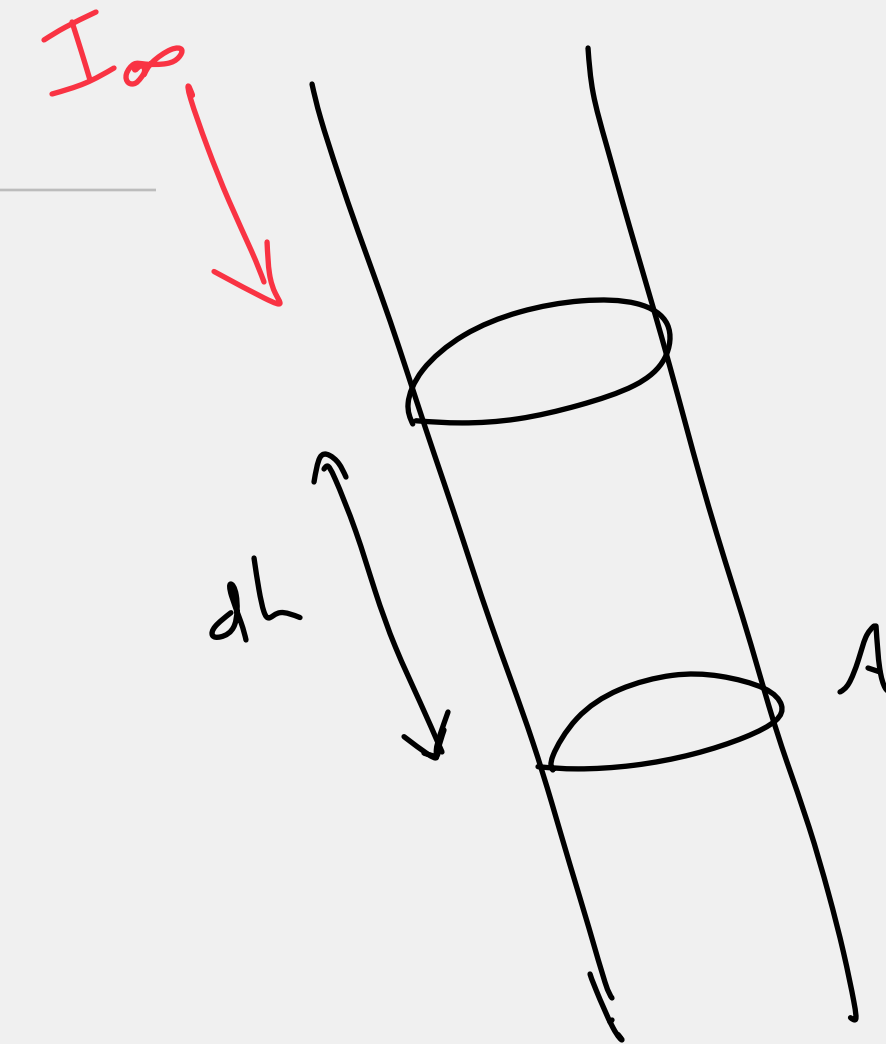
# Absorption in Earth's Atmosphere

$$I = \text{brightness} = \text{flux} = \text{J}/\text{cm}^2/\text{sec} = \text{W}/\text{cm}^2$$

$$- dI \sim I dh$$

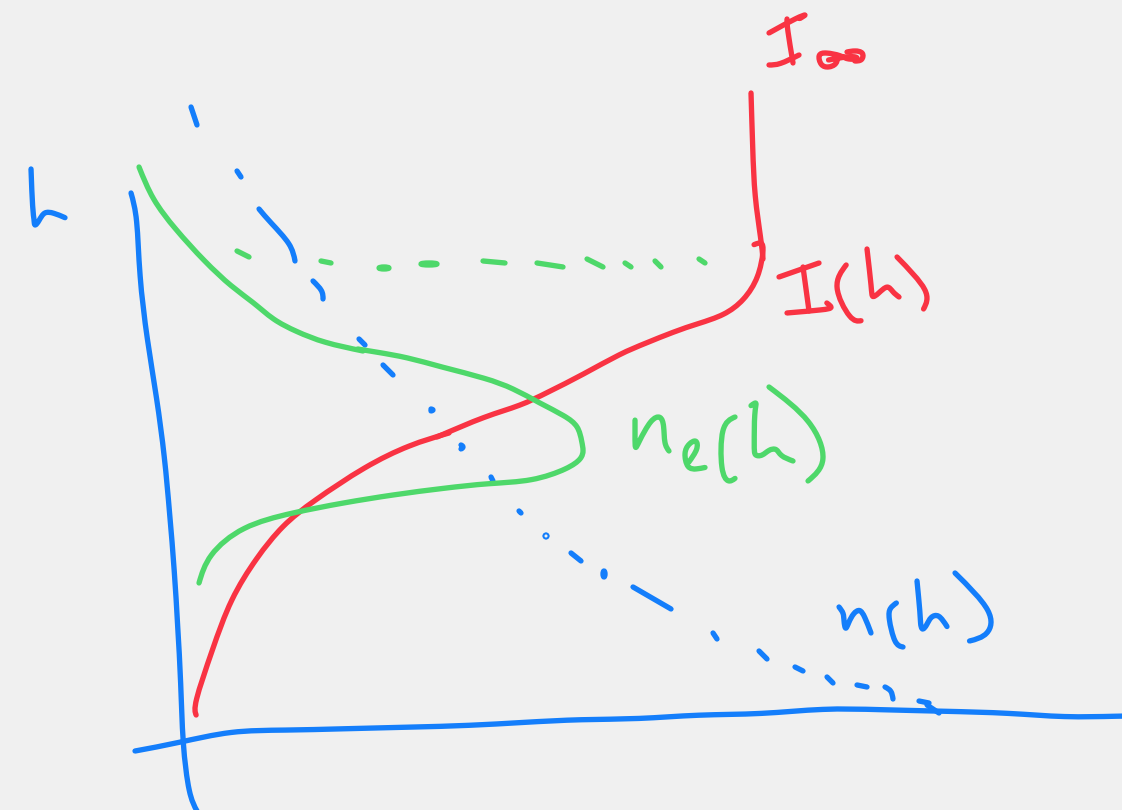
$$\underline{dI = -\sigma n I dh}$$

$\uparrow$  number density,  $\text{cm}^{-3}$   
 $\uparrow$  absorption cross section,  $\text{cm}^2$   
 molecule,  $\lambda$ -dependent



$$\frac{dI}{I} = -\sigma n dh \rightarrow \ln I \Big|_{\infty}^h = - \int_{\infty}^h \sigma(h) n(h) dh$$

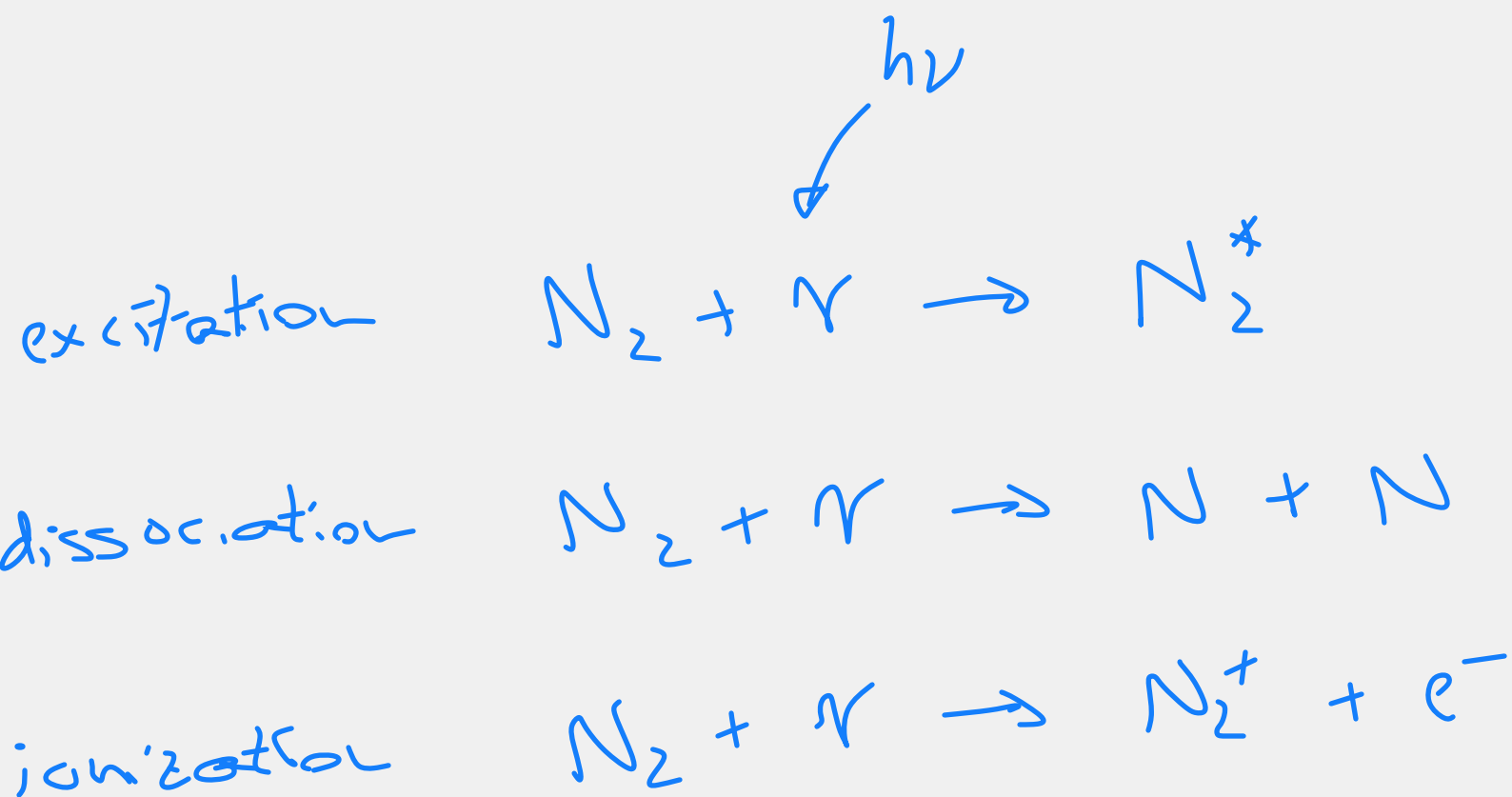
$$I(h) = I_{\infty} e^{-\tau} \rightarrow \text{optical dept}$$



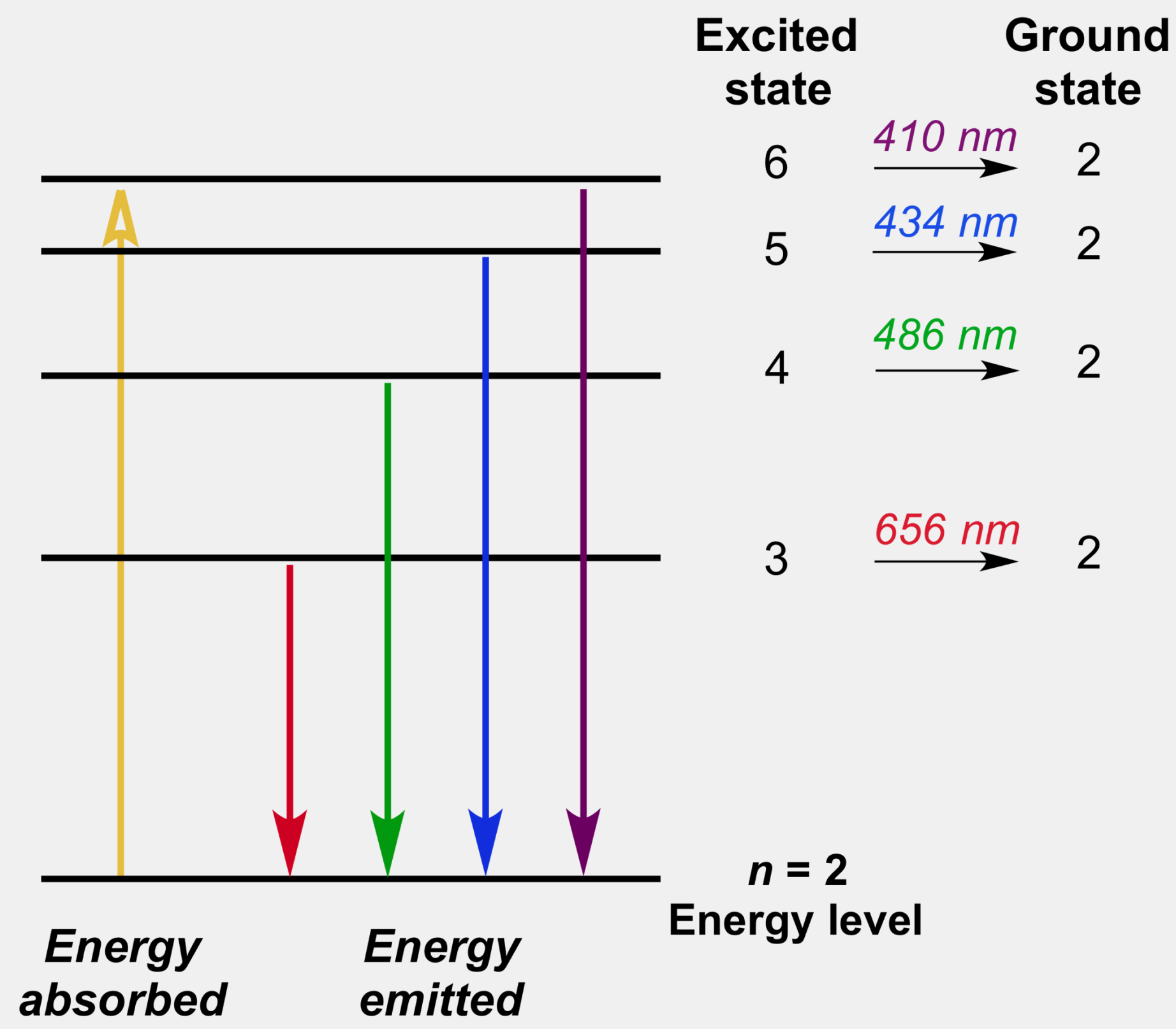


# Atmospheric Heating

- ❖ Though less than 1.5% of TSI, wavelengths < 300 nm are primary source of atmospheric heating from 15–500 km.
- ❖ Excitation; dissociation; ionization
- ❖ Relaxation, association, recombination → heat



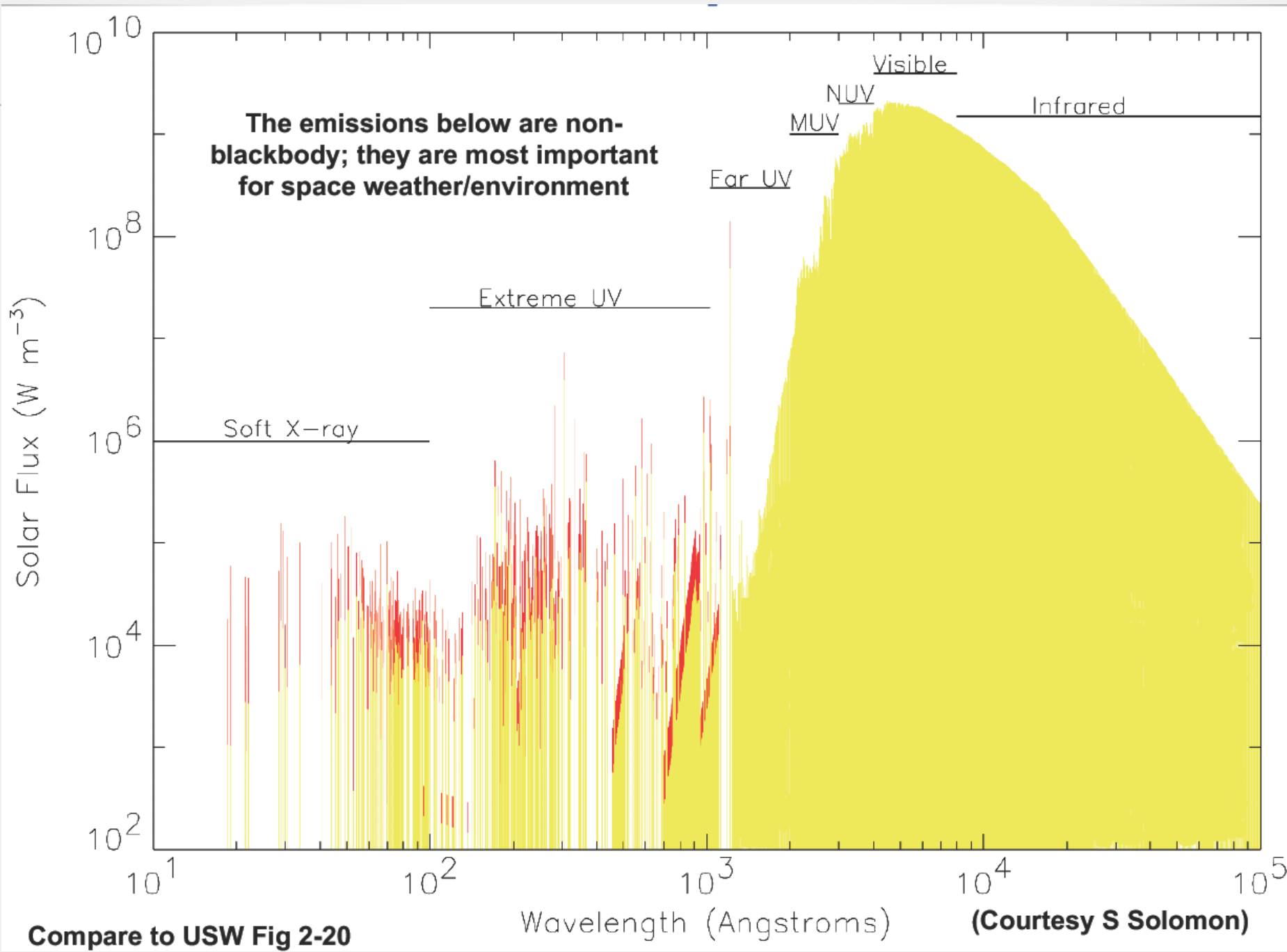
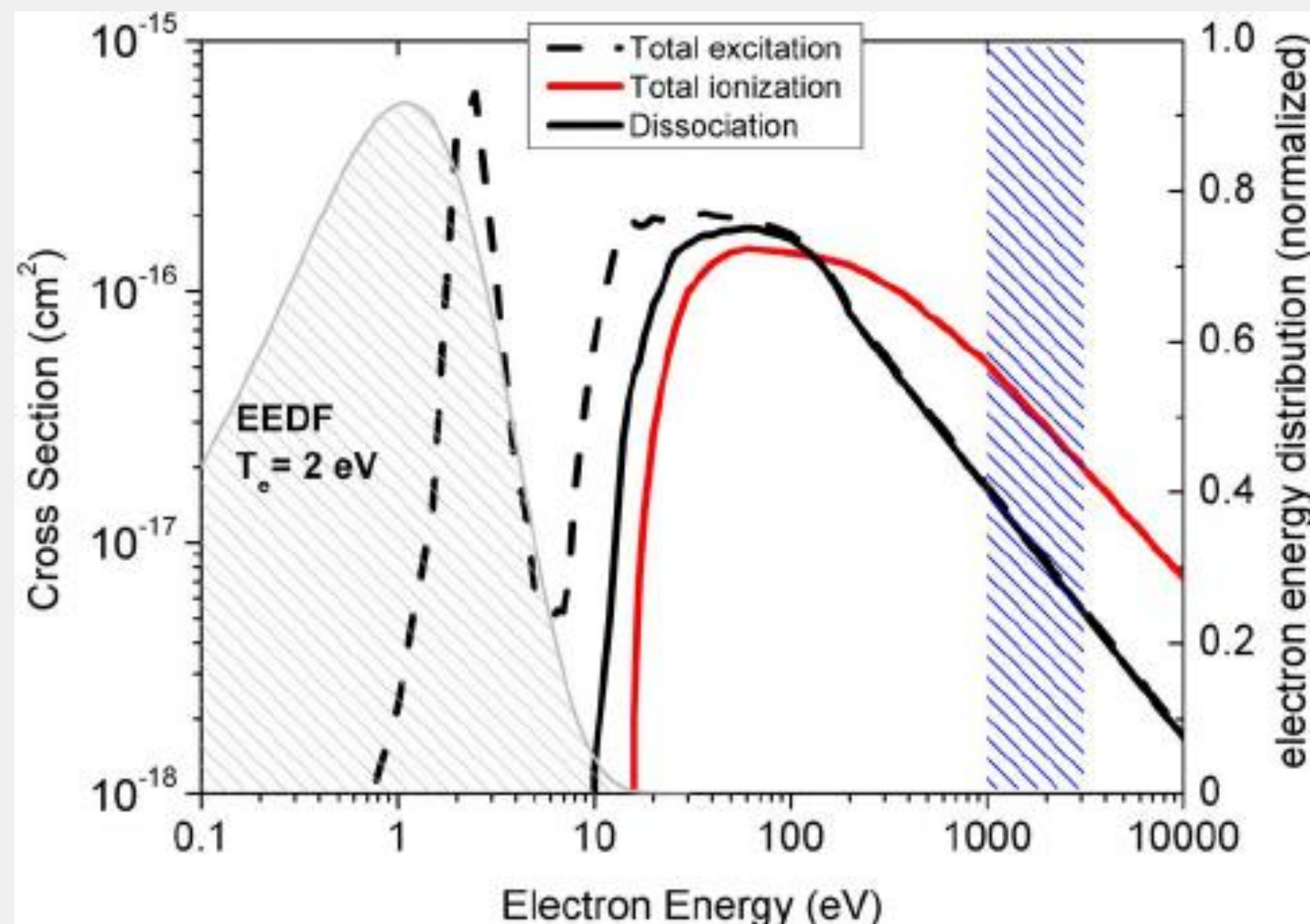
free electron





# Ionization thresholds

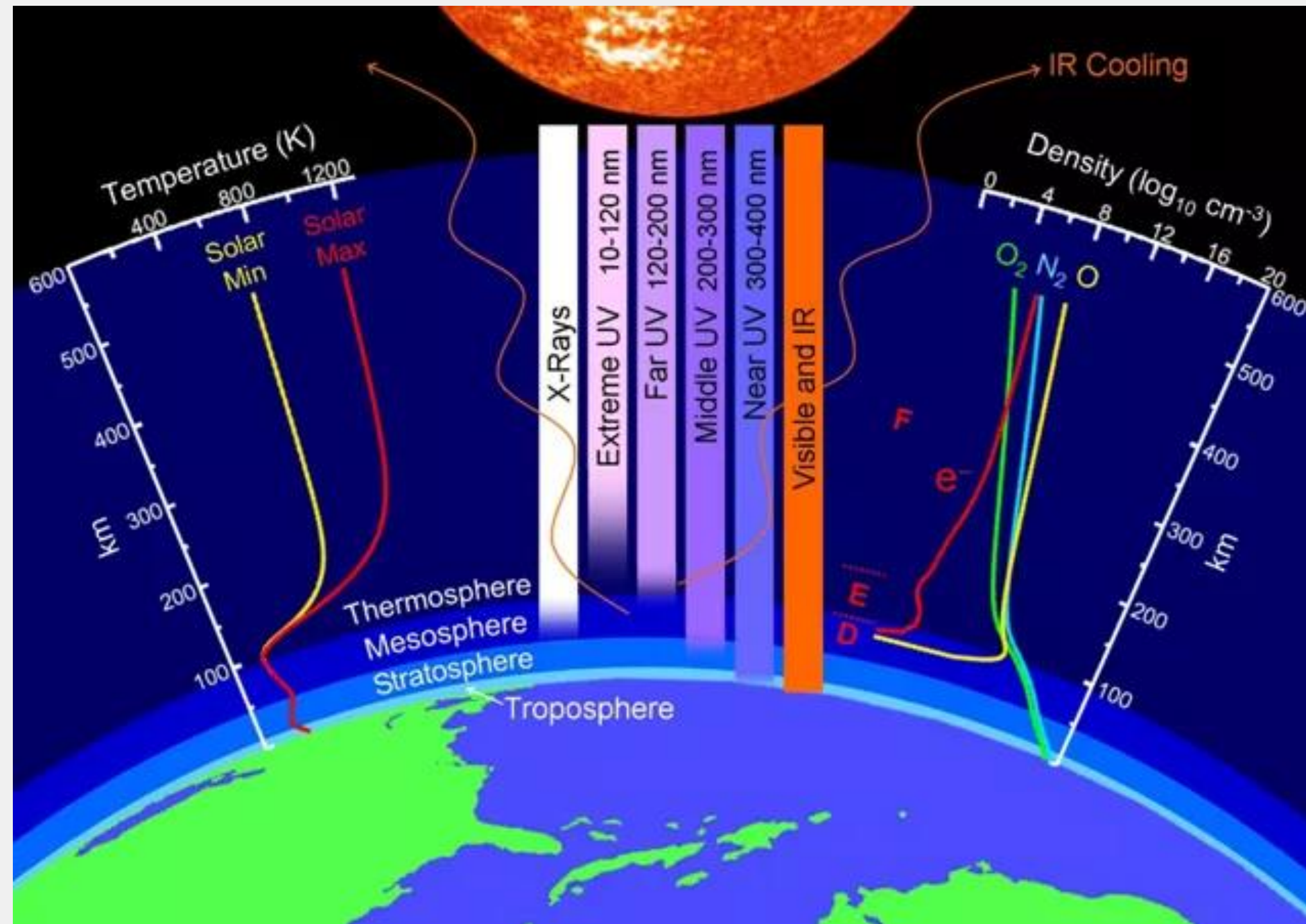
- ❖ Require a minimum energy to free an electron from an atom or molecule
- ❖ Require a photon with at least this minimum energy: “**ionizing radiation**” or sometimes just “**radiation**”
- ❖ **Ionization cross section** provides energy-dependent picture of ionization probability



	Ionization Energy	Minimum photon wavelength
H	13.6 eV	91 nm (910 Å)
He	24.6 eV	50 nm
O	13.62 eV	91 nm
Ar	15.76 eV	79 nm
N2	15.6 eV	80 nm
O2	12.1 eV	103 nm

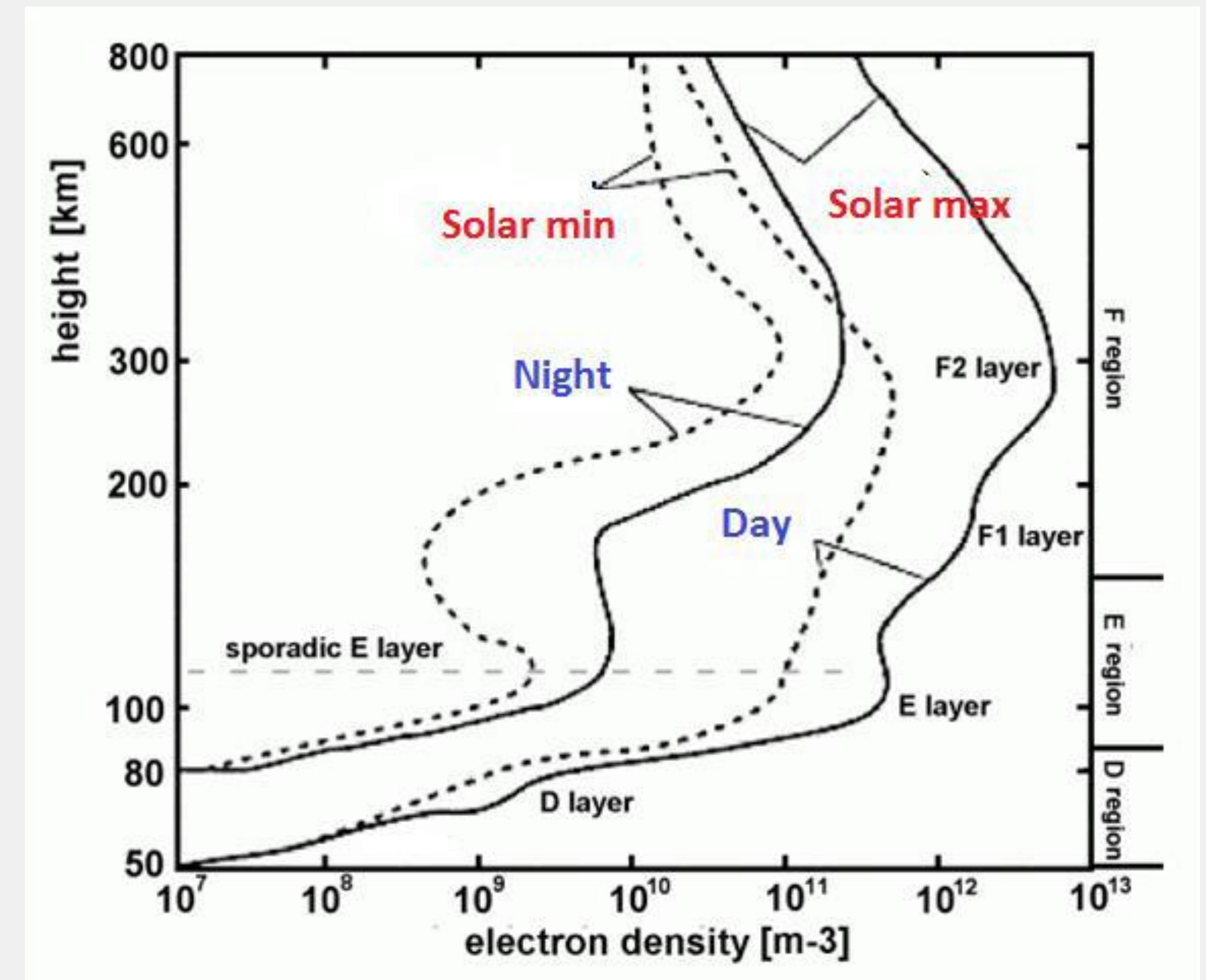


# Earth's Ionosphere



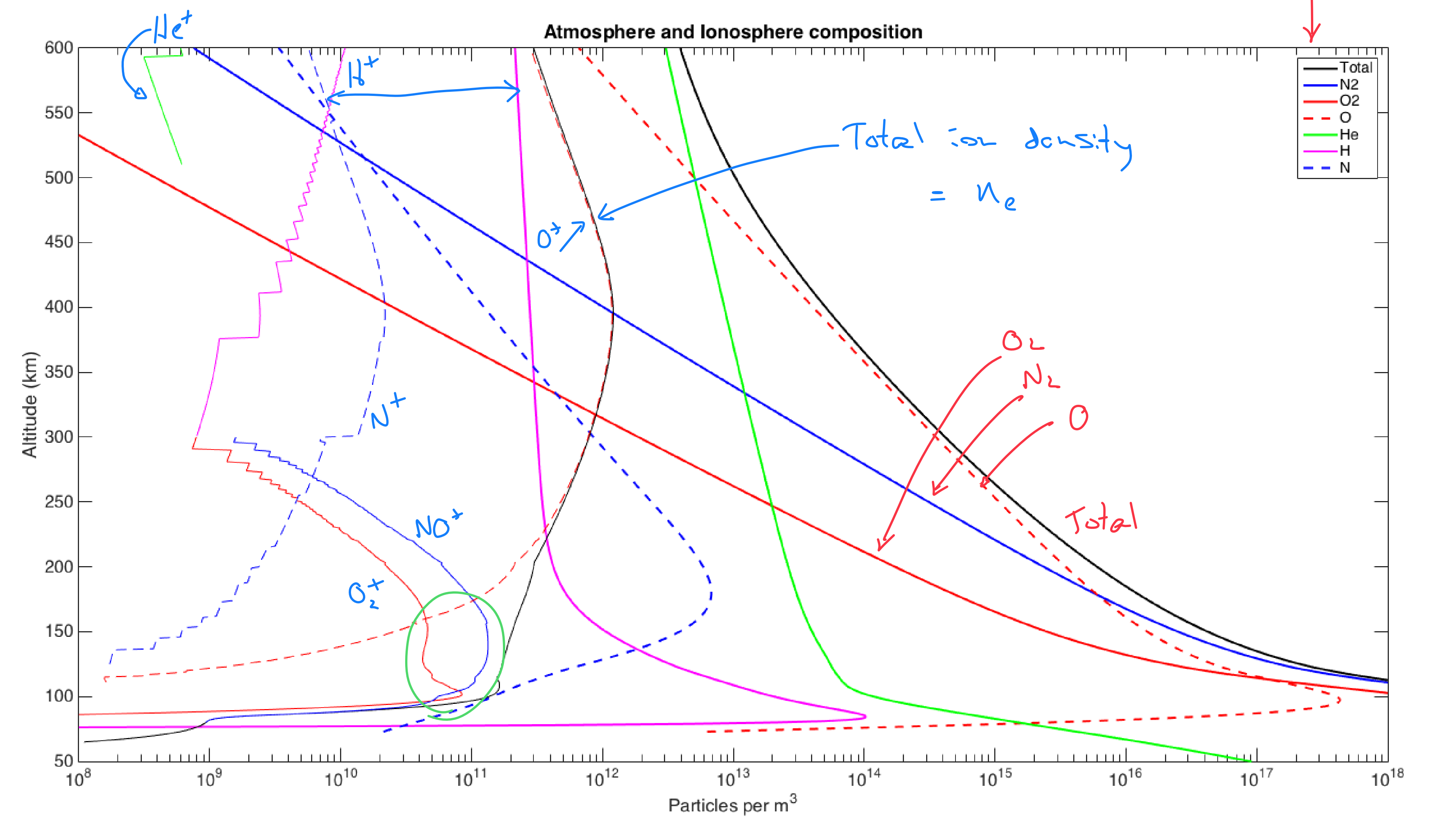
- ❖ Right: ionization density changes by 100x day vs night, and 10x or more with solar cycle

- ❖ Ionosphere altitudes and layers have a lot to do with where solar radiation is absorbed!





# Ionosphere Composition and Density





# Why is the Ionosphere finite in altitude?

- ❖ The atmosphere is exponentially increasing all the way to the ground.  
What about the ionosphere?

$$dI = -\sigma n(h) I dh$$

$$= \sigma n(z) I dz \sec \chi$$

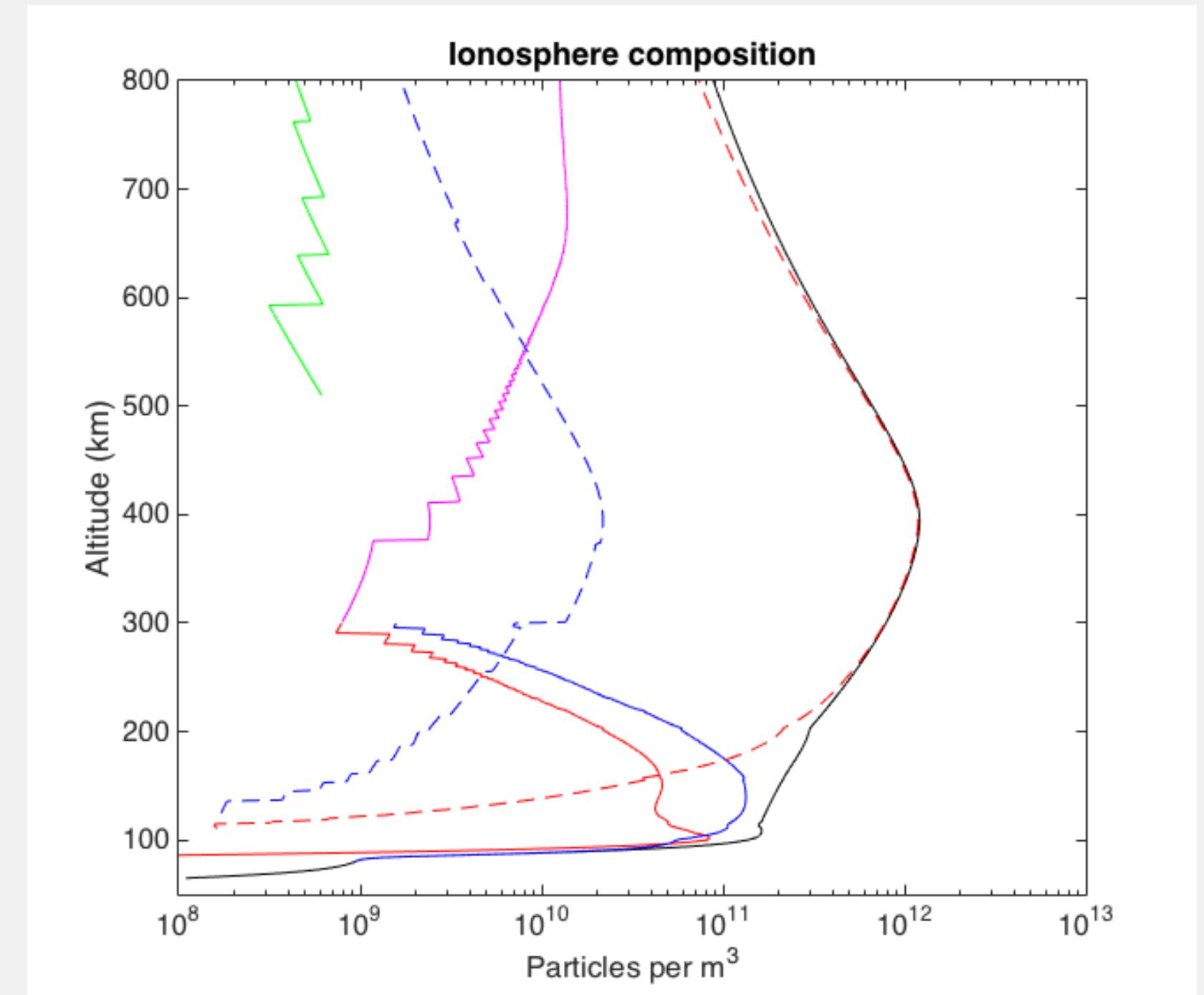
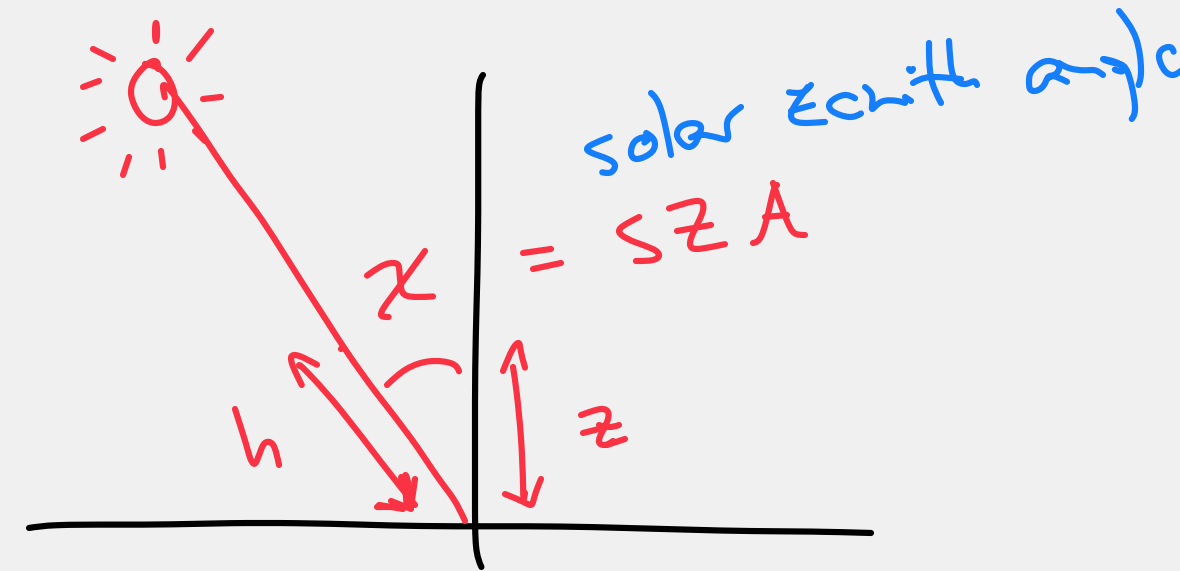
$$I(z) = I_{\infty} e^{-\int_a^z n(z) \sigma \sec \chi dz}$$

$$\text{if } n(z) = n_0 e^{-z/H}$$

$$I(z) = I_{\infty} e^{-H n(z) \sigma \sec \chi}$$

$$I(z, \lambda, \chi) = I_{\infty}(\lambda) \exp \left[ -\int_a^z \sum_i n_i(z) \sigma_i(\lambda) \sec \chi dz \right]$$

$$= I_{\infty}(\lambda) e^{-\tau(z, \lambda, \chi)}$$





# Chapman Layer

Ionization Production Rate,  $P$  ( $\text{Q}$ ), pairs/ $\text{m}^3/\text{sec}$

$$P = I(z, \lambda, \chi) \cdot n(z) \cdot \underbrace{\sigma}_\sigma \cdot \eta_i$$

ionization efficiency, 0-1  
 $\sigma_i$  ( $\text{cm}^2$ ), ioniz. cross section

$$P = I_\infty e^{-Hn(z)\sigma \sec \chi} \cdot \sigma \eta_i \overset{n_0 e^{-z/H}}{n(z)}$$

$$P = I_\infty \sigma \eta_i n_0 e^{-z/H} \exp\left(-H\sigma \sec \chi n_0 e^{-z/H}\right)$$

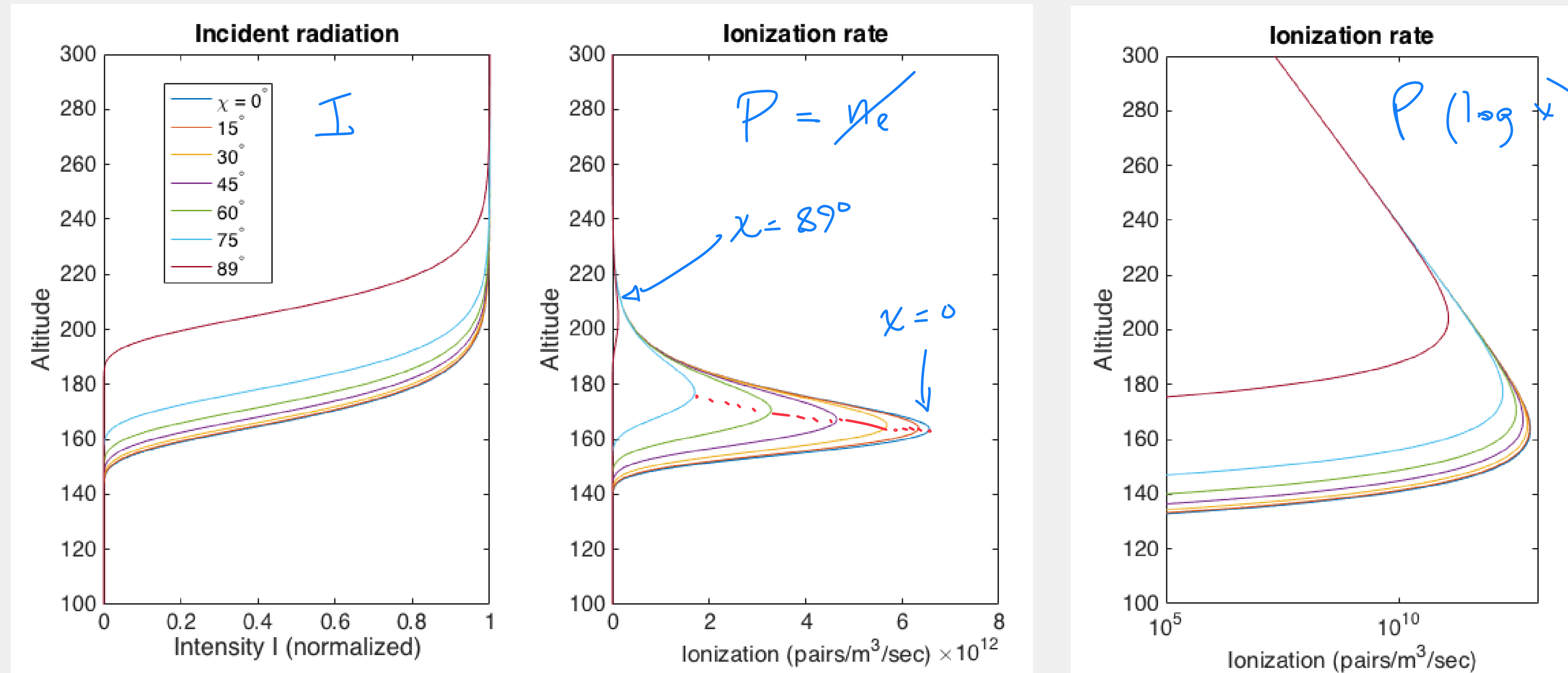


# Chapman Layer

- ❖ Production higher, and lower in altitude, for lower zenith angle (i.e. noon)
- ❖ Peak in production is near where intensity is about **half** the incident value

$$z_{max} = H \ln(n_0 \sigma H \sec \chi)$$

$$P_{max} = n_i \frac{I_0}{H} \cos \chi e^{-1}$$





# Ionization Chemistry

- ❖ Ionosphere is in equilibrium when ionization production and loss mechanisms balance
- ❖ Production: photoionization; energetic particle precipitation; collisions
- ❖ Loss: recombination; charge exchange; chemistry, transport

$$\frac{dn_e}{dt} = P - L$$

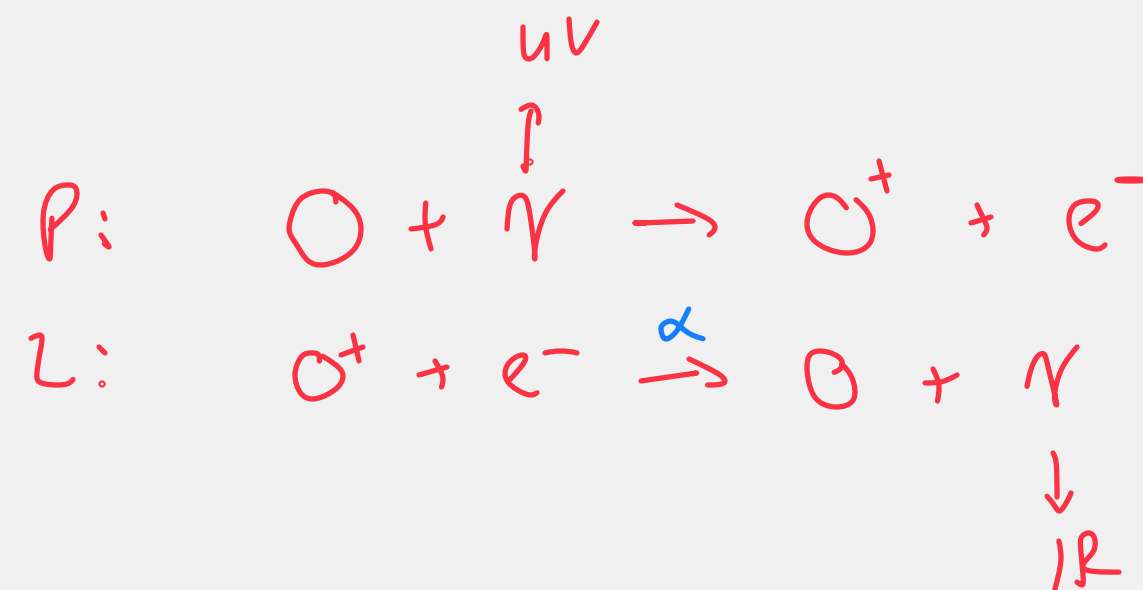
at equilibrium,  $\frac{dn_e}{dt} = 0$ ,  $P = L$

$$L = \alpha n_o n_e = \alpha n_e^2$$

$$P = L \Rightarrow P = \alpha n_e^2$$

$\Rightarrow$

$$n_e = \sqrt{\frac{P}{\alpha}}$$





# Electron Density Profile

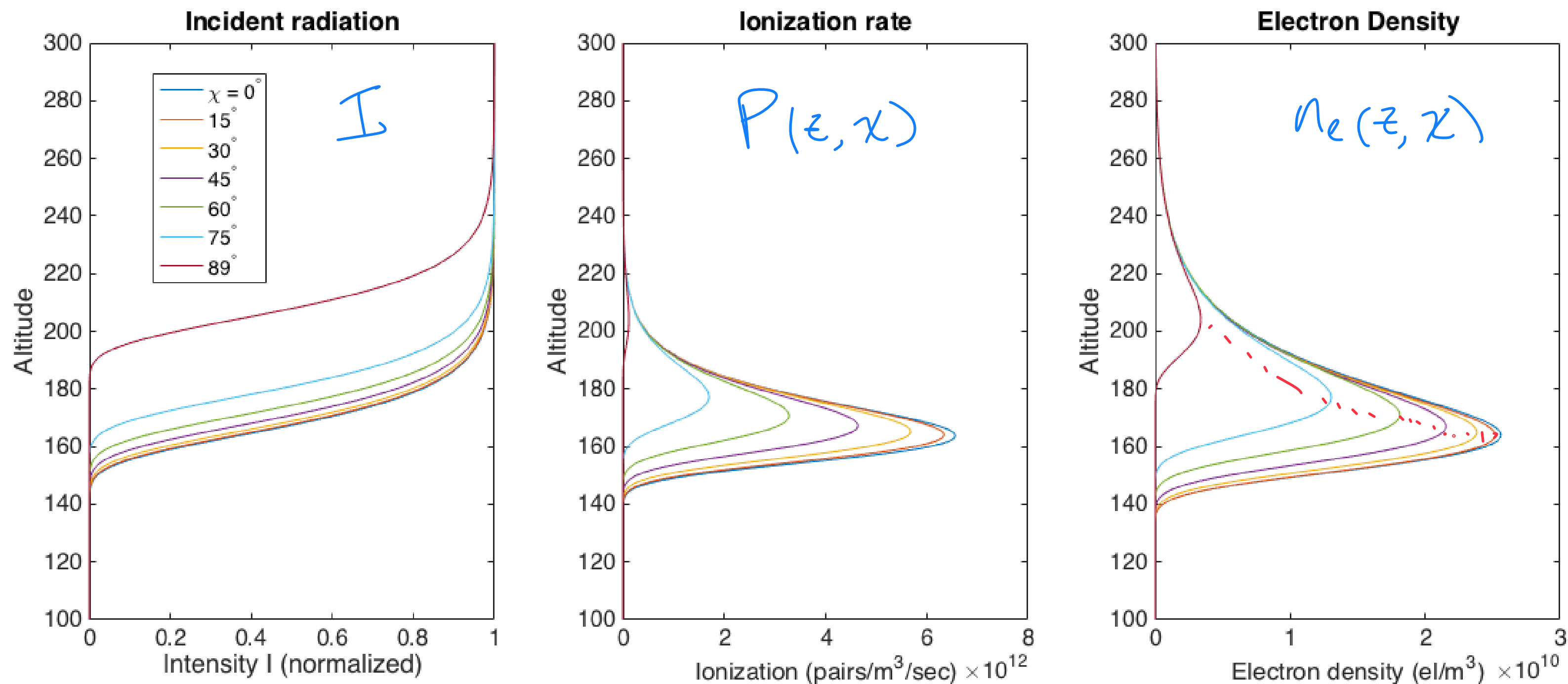
- ❖ Balancing production (ionization) with loss (recombination), we get an equilibrium electron (or ion) density below

- ❖ Higher, less dense for increasing zenith angle

- ❖ Reminder: this is for a single species, and single photon wavelength!

$$n_e = \sqrt{\frac{P}{\alpha}} = \sqrt{\frac{P_{\max}}{\alpha}} \exp\left(0.5(1 - z_1 - e^{-z_1})\right)$$

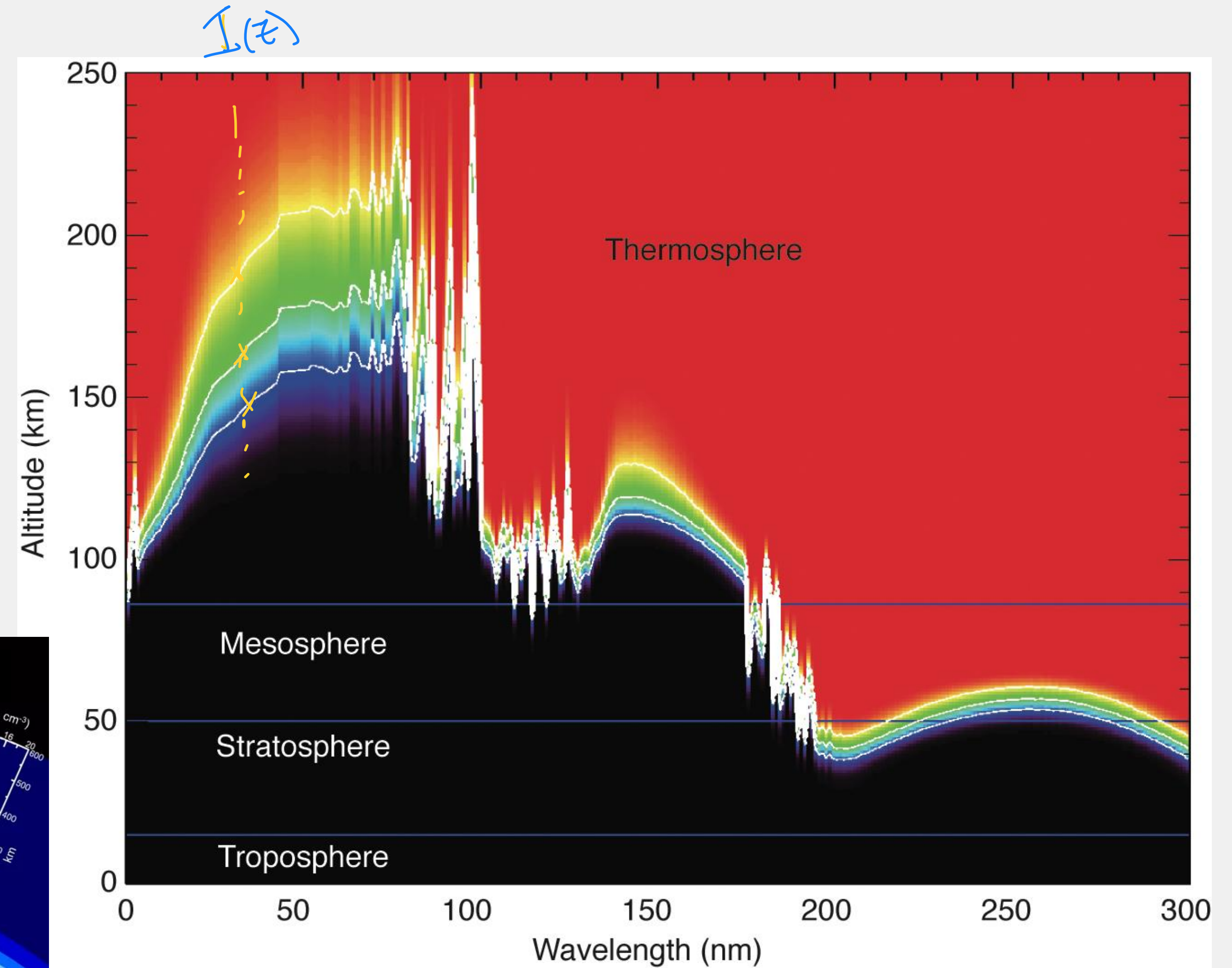
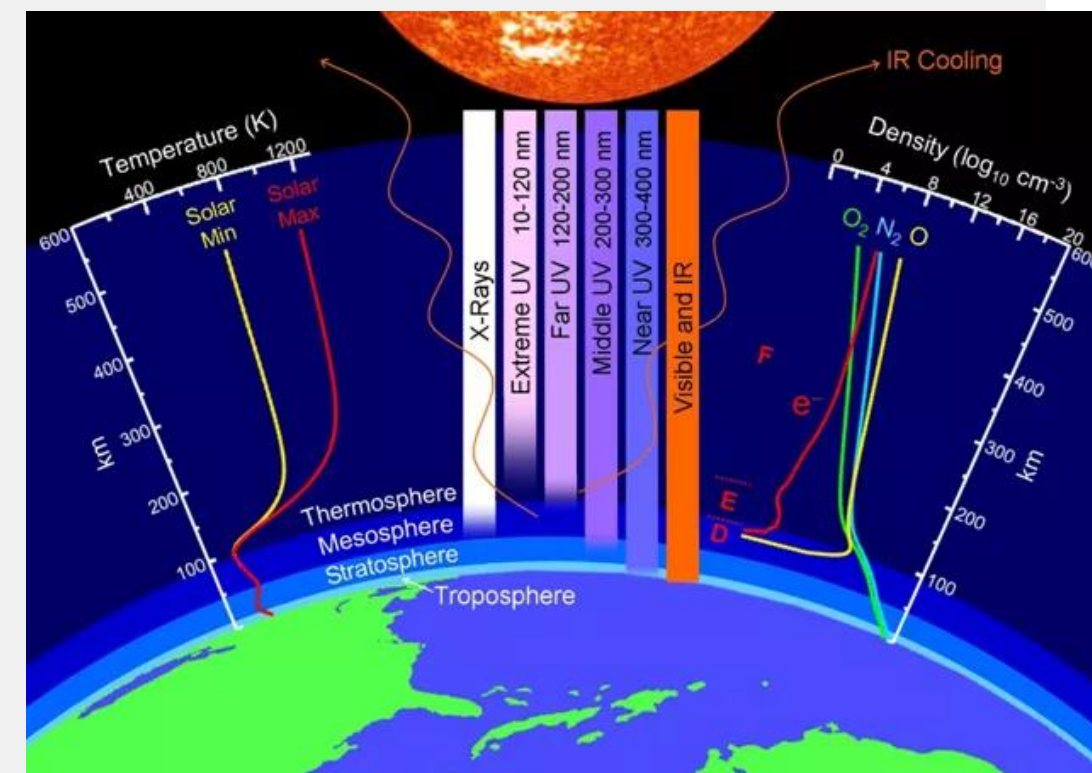
$$z_1 = \frac{z - z_{\max}}{H}$$





# Ionosphere Layers

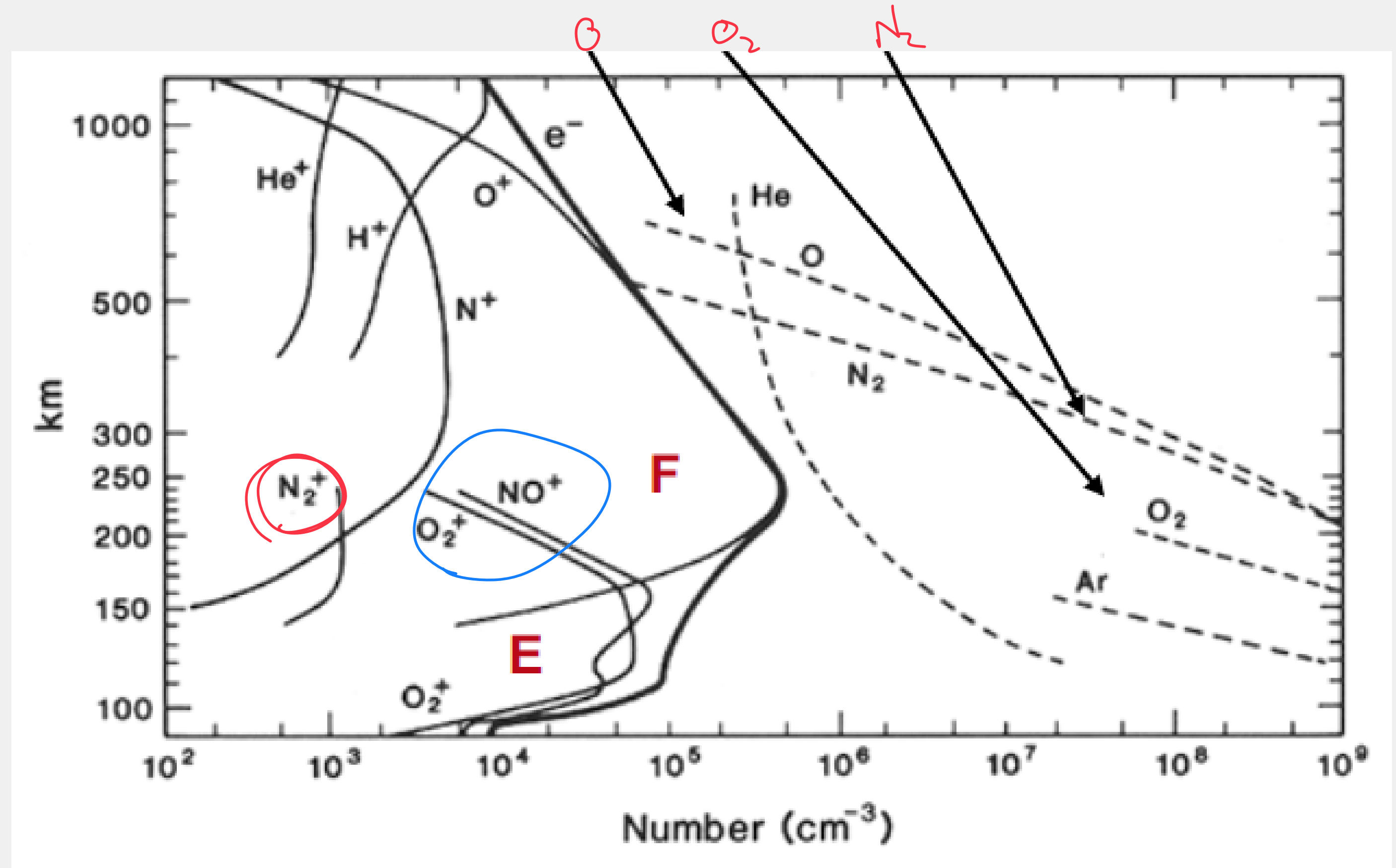
- ❖ Different wavelengths are absorbed at different altitudes, by different species
- ❖  $I(z)$  depends on wavelength-dependent absorption for each species
- ❖  $P(z)$  depends on wavelength-dependent ionization cross sections for each species
- ❖ Right: top white curve is  $I(z)$  decay by  $e^{-0.5}$ ; middle white curve by  $e^{-1}$ ; bottom white curve by  $e^{-1.5}$
- ❖ Red areas:  $I(z)$  is basically  $I_\infty$   
Black areas:  $I(z)$  is basically zero





# Another way of looking at it

- ❖ Ionosphere layers depend on composition (atmosphere) and radiation (solar spectrum and flux)
- ❖ D, E, and F regions are dominated by different ions, depending on the neutral species

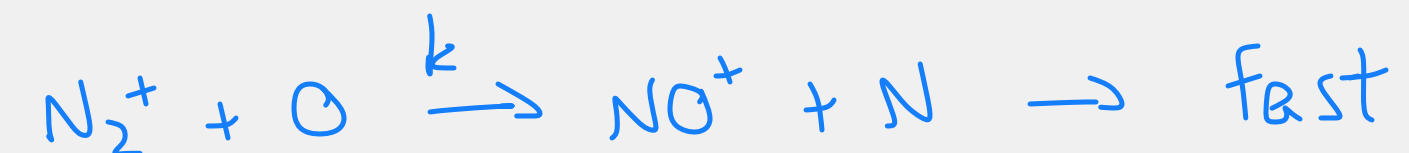




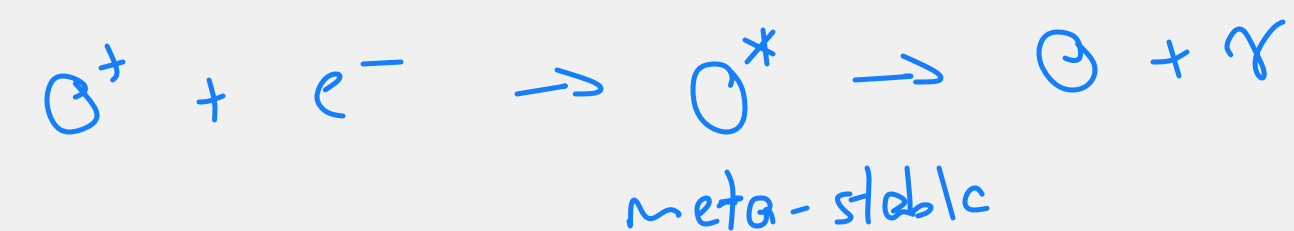
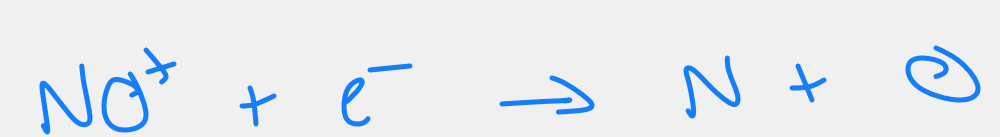
# Primary Production / Loss channels



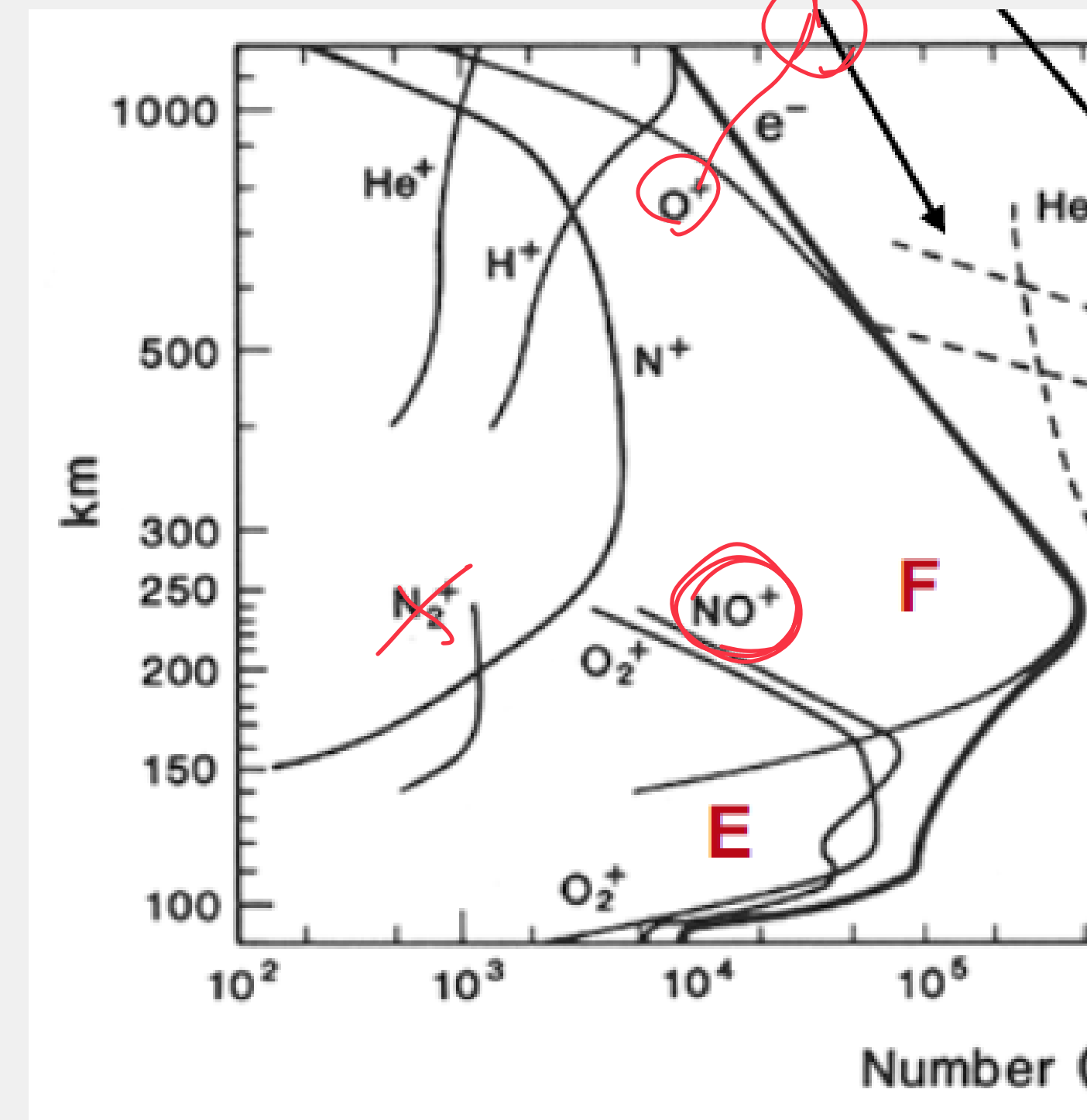
## Charge Transfer



## Recombination



↓ protons

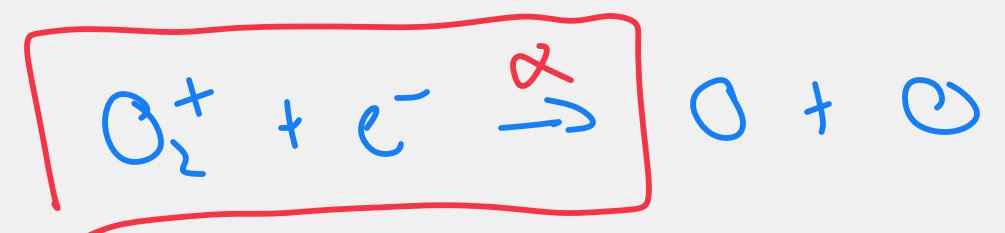




# E-region

→ Chapman

Below 150 km,  $[O_2] \gg [O]$ , so E-region dominated by



$$L = \alpha n_{O_2^+} n_e \approx \alpha n_e^2$$

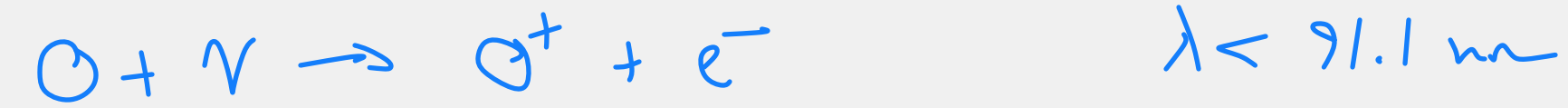
$$\text{if } P=L, \quad n_e = \sqrt{\frac{P}{\alpha}}$$





# F-region

: F/



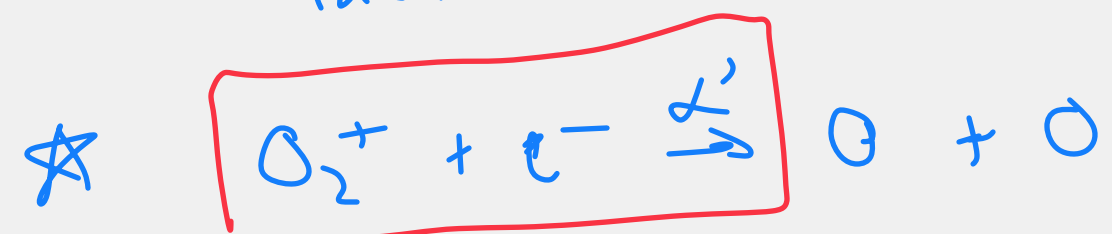
(some  $N_2$  ionization)



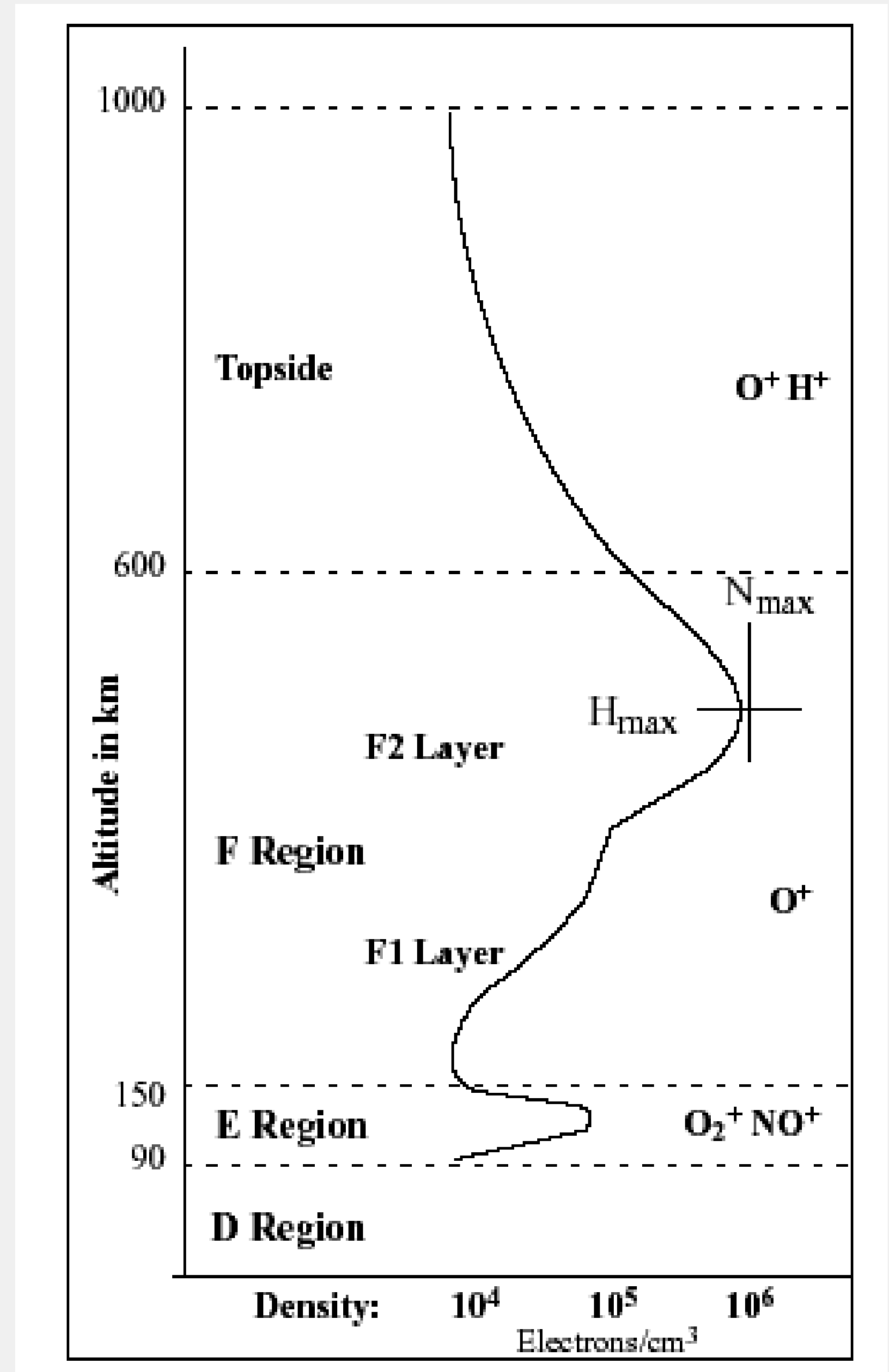
instead



then:



$$L = \alpha' n_{O_2^+} n_e + \alpha_2 n_{NO^+} n_e \approx \alpha n_e^2, \text{ Chapman!}$$

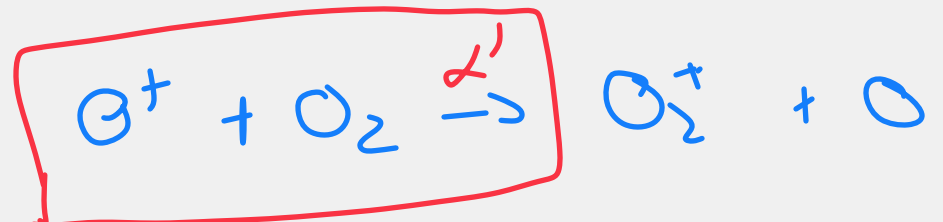


# F-region

: F2



charge exchange



$$\text{Loss} = \alpha' n_{\text{O}^+} n_{\text{O}_2} \approx \alpha' n_{\text{O}_2} n_e \neq \alpha n_e^2$$

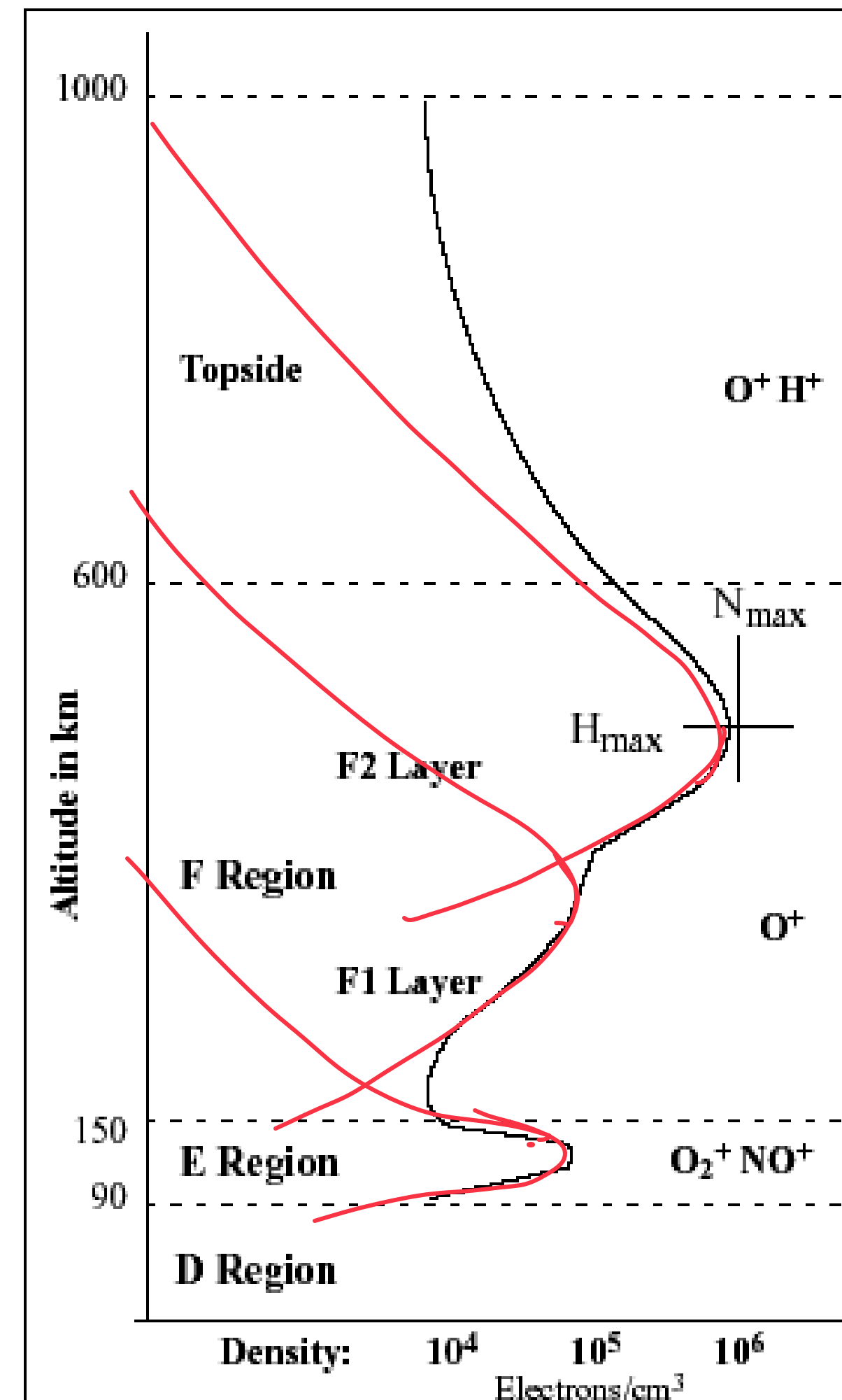
other factors

\* dynamics : vertical transport

- diffusion

\* electrostatic forces

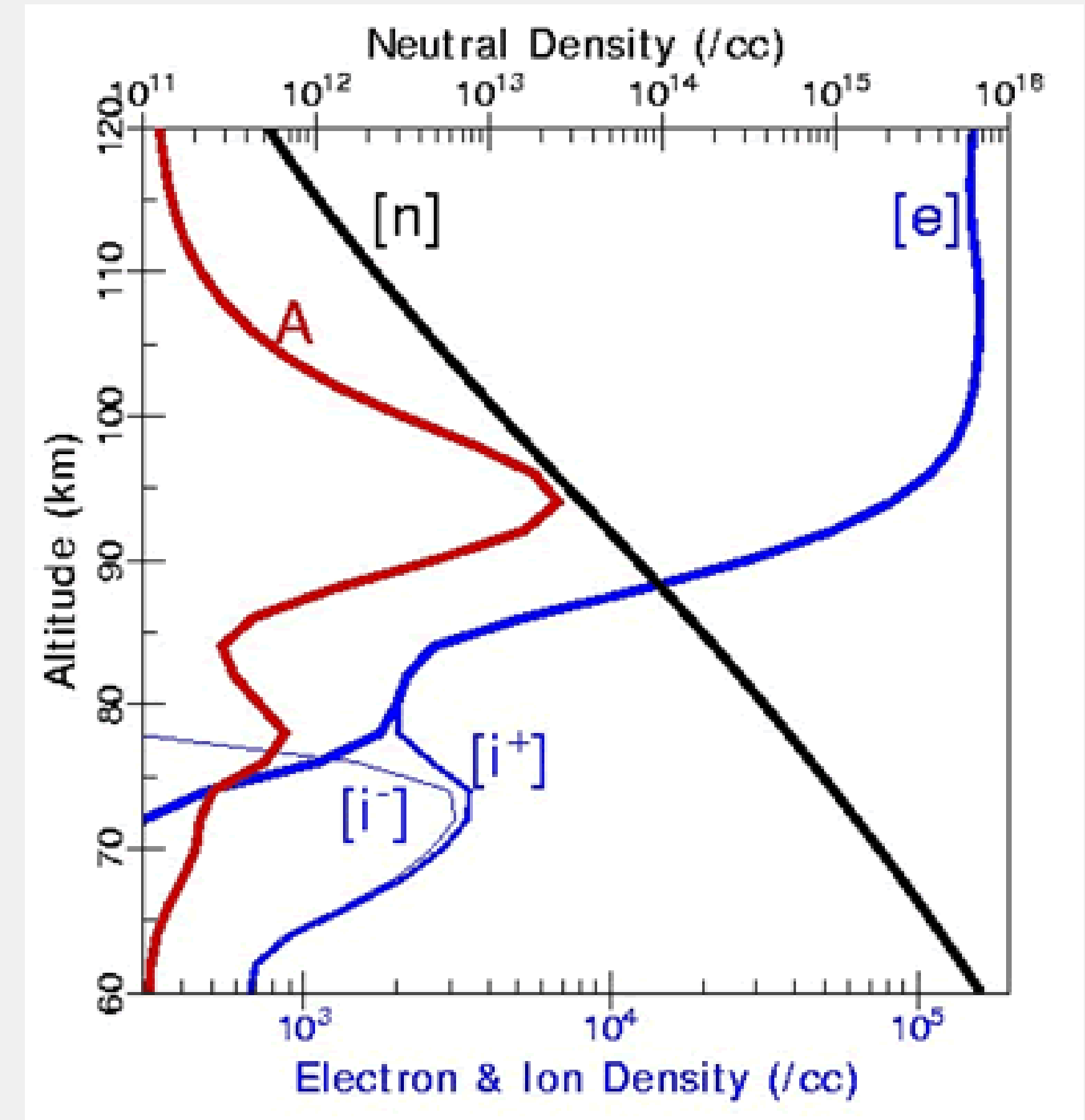
3 chapters





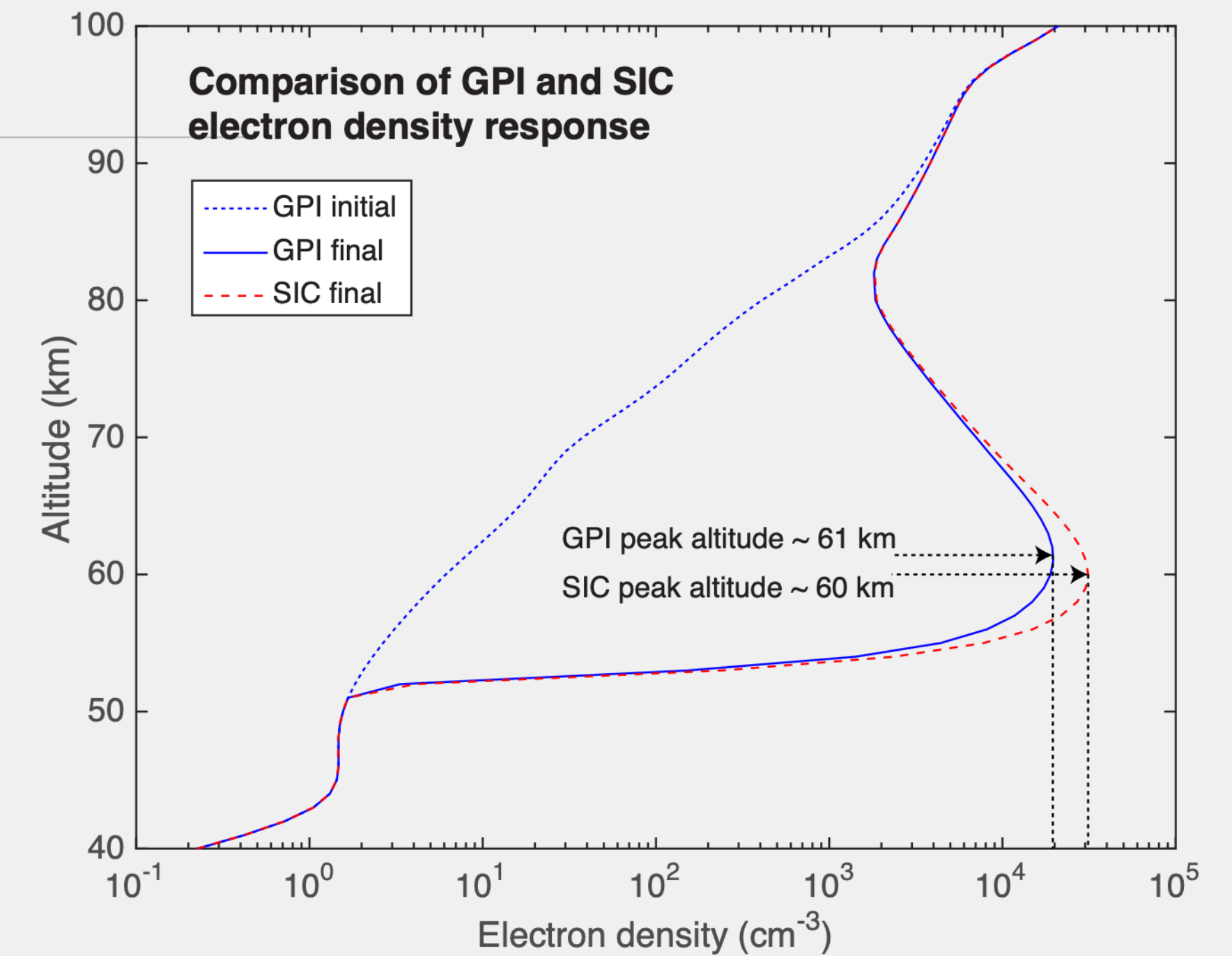
# D-region

- ❖ D-region is known for low electron densities, light and heavy positive and negative ions, and complex chemistry.
- ❖ Production:
  - ❖  $\text{N}_2 + \gamma \rightarrow \text{N}_2^+ + e^-$
  - ❖  $\text{O}_2 + \gamma \rightarrow \text{O}_2^+ + e^-$
  - ❖  $\text{NO} + \gamma \rightarrow \text{NO}^+ + e^-$
- ❖ Negative ions formed by attachment processes:
  - ❖  $\text{O}_2 + e^- + \text{O}_2 \rightarrow \text{O}_2^- + \text{O}_2$
  - ❖  $\text{O}_2 + e^- \rightarrow \text{O}_2^- + \gamma$
- ❖ Detachment:
  - ❖  $\text{O}_2^- + \gamma \rightarrow \text{O}_2 + e^-$
  - ❖  $\text{O}_2^- + \text{O}_2 \rightarrow \text{O}_2 + e^- + \text{O}_2$



# D-region chemistry and “cluster ions”

- ❖ D-region also contains heavy water cluster ions of the form  $(\text{H}_2\text{O})_n\text{H}^+$
- ❖ Requires more complex chemistry models to evaluate  $n_e$  profiles

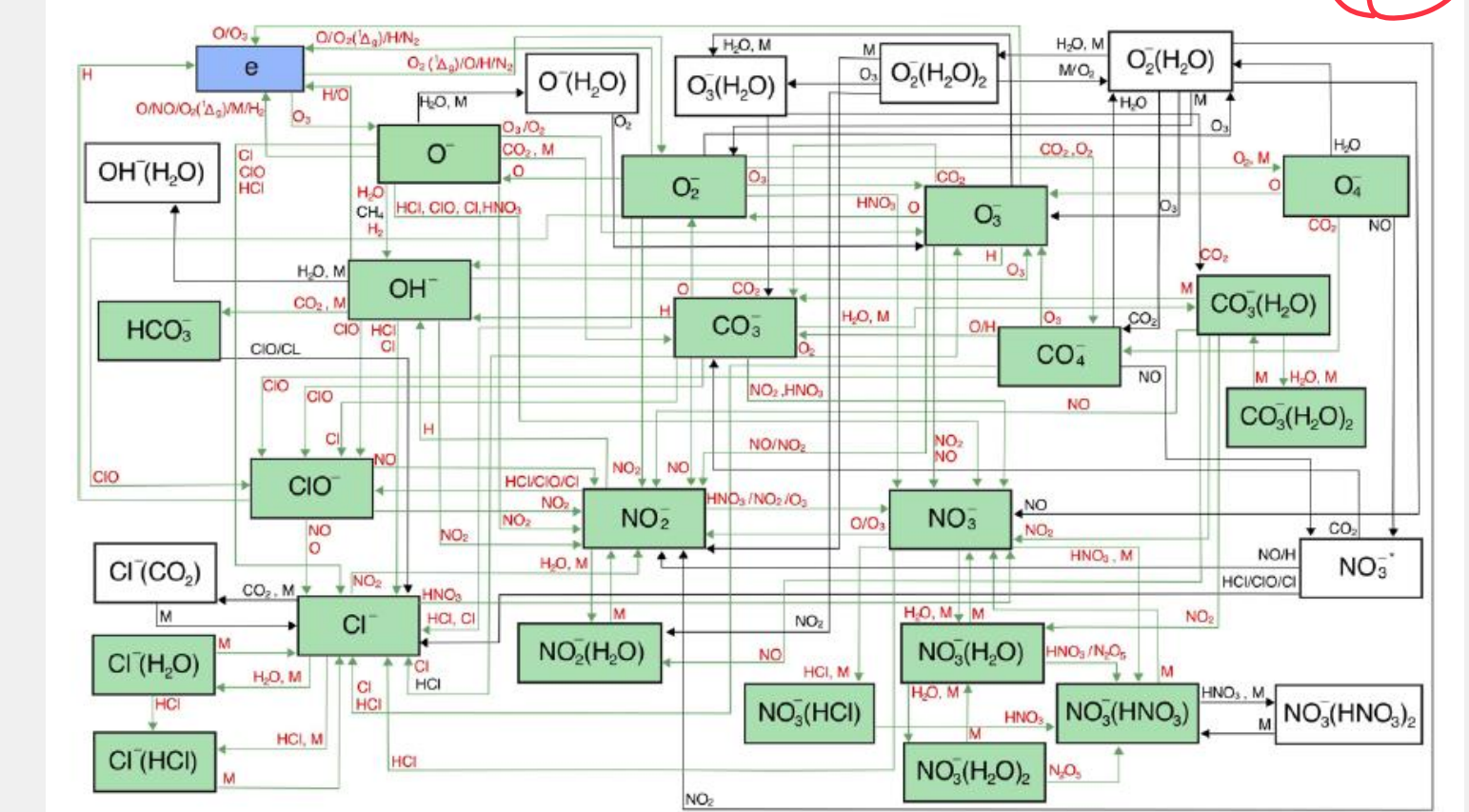
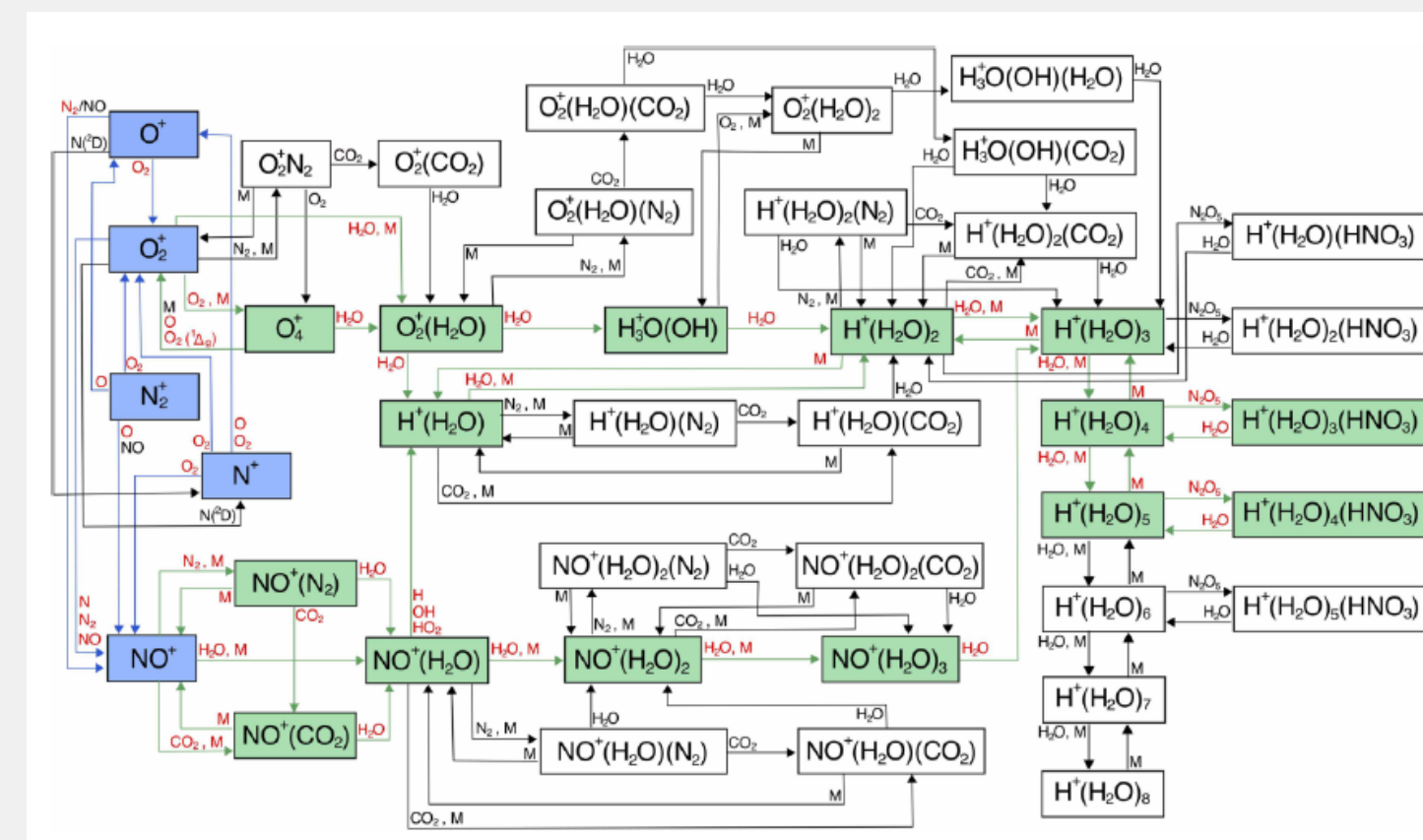


## Glukhov Pasko Inan (GPI) 2009 model

$$\begin{aligned} \frac{dN_e}{dt} &= Q - \beta N_e + \gamma N^- + \gamma_x N_x^- - (\alpha_d N^+ + \alpha_d^c N_x^+) N_e \\ \frac{dN^-}{dt} &= \beta N_e - \gamma N^- - \alpha_i (N^+ + N_x^+) N^- - A N^- \\ \frac{dN_x^-}{dt} &= -\gamma_x N_x^- - \alpha_i (N^+ + N_x^+) N_x^- + A N^- \\ \frac{dN^+}{dt} &= Q - \alpha_d N_e N^+ - \alpha_i (N^- + N_x^-) N^+ - B N^+ \\ \frac{dN_x^+}{dt} &= \alpha_d^c N_e N_x^+ - \alpha_i (N^- + N_x^-) N_x^+ + B N^+ \end{aligned}$$

$$\frac{dn_e}{dt} = P - L$$

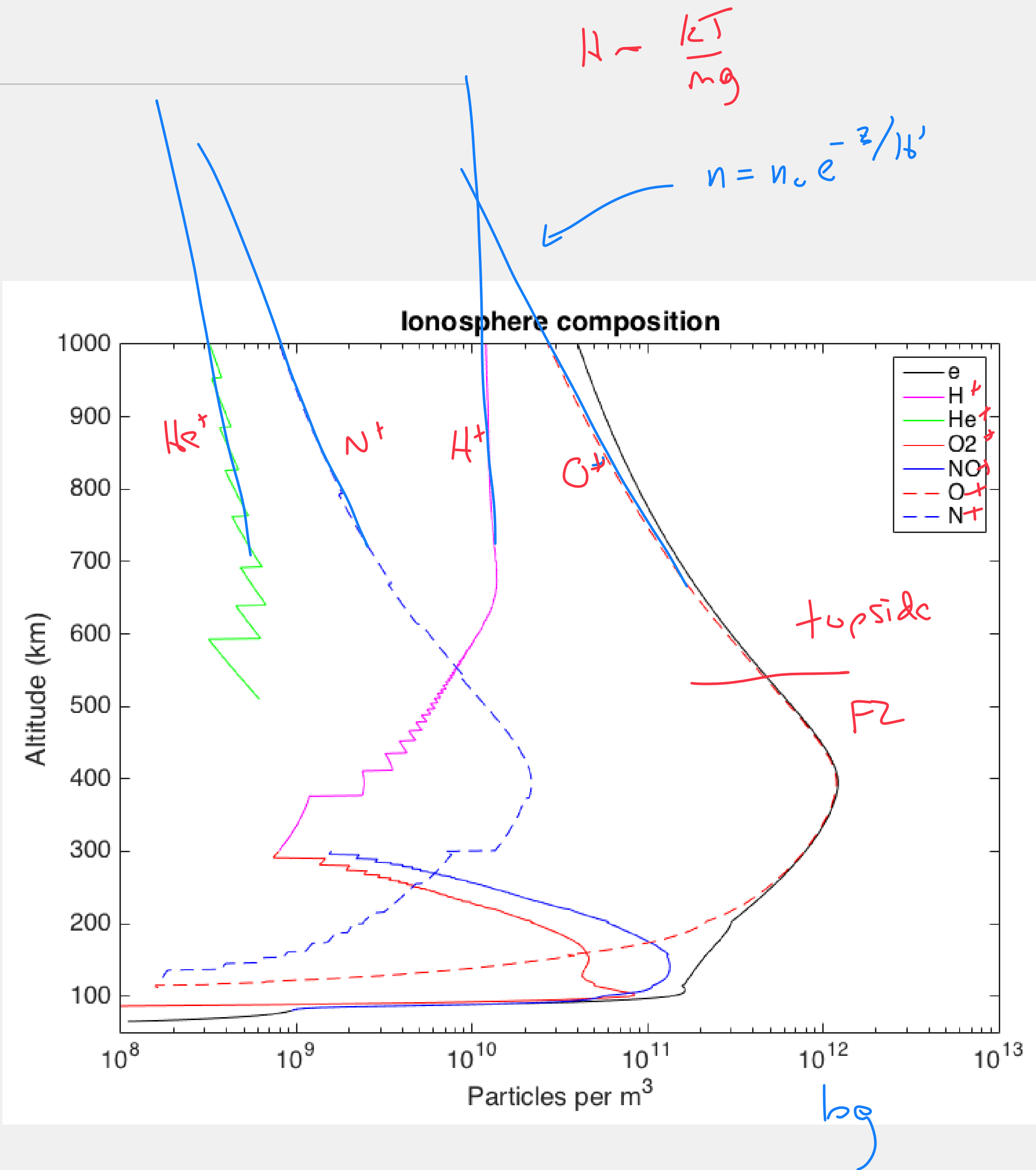
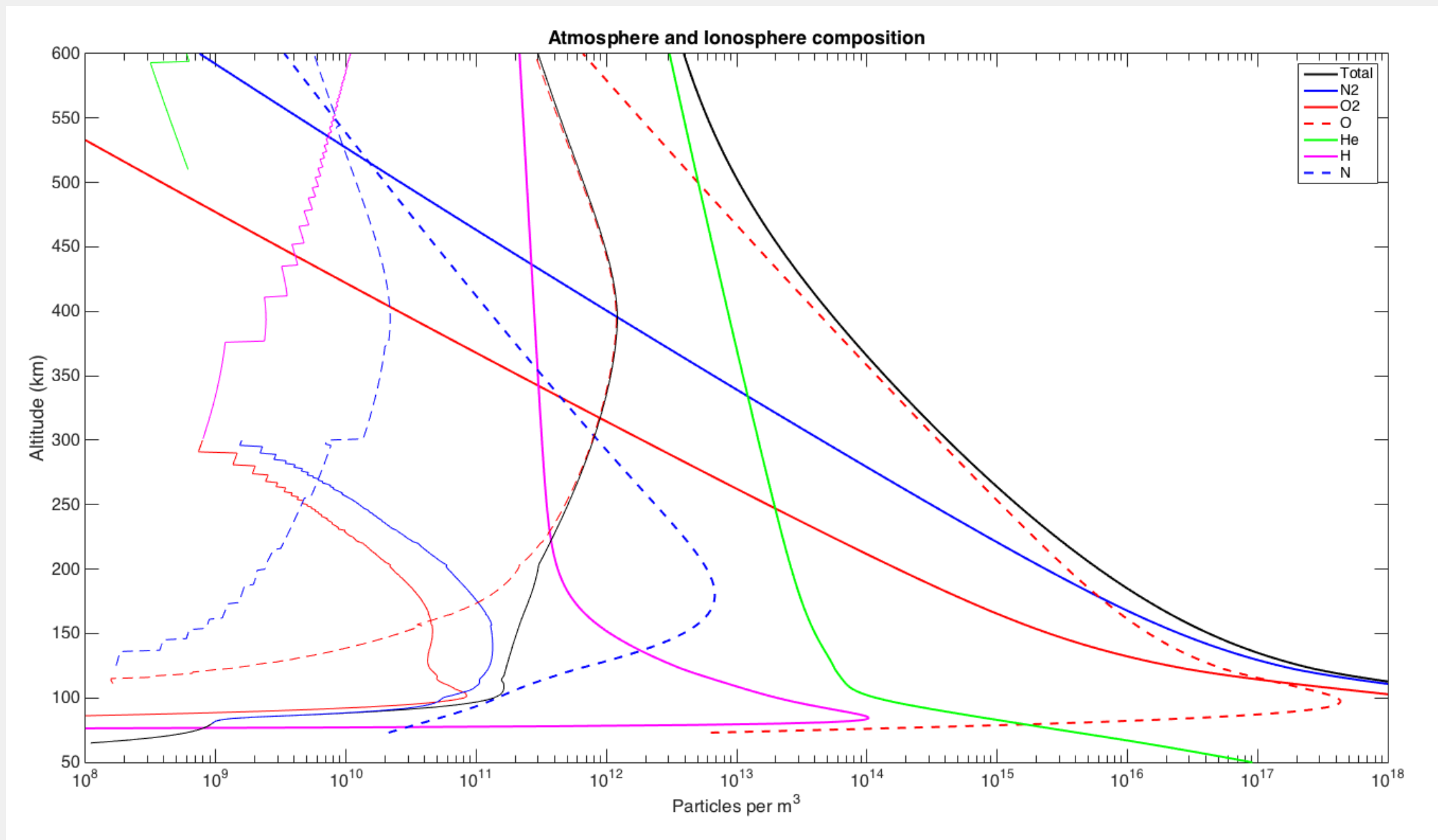
### Sodankylä Ion and Neutral Chemistry (SIC) model:





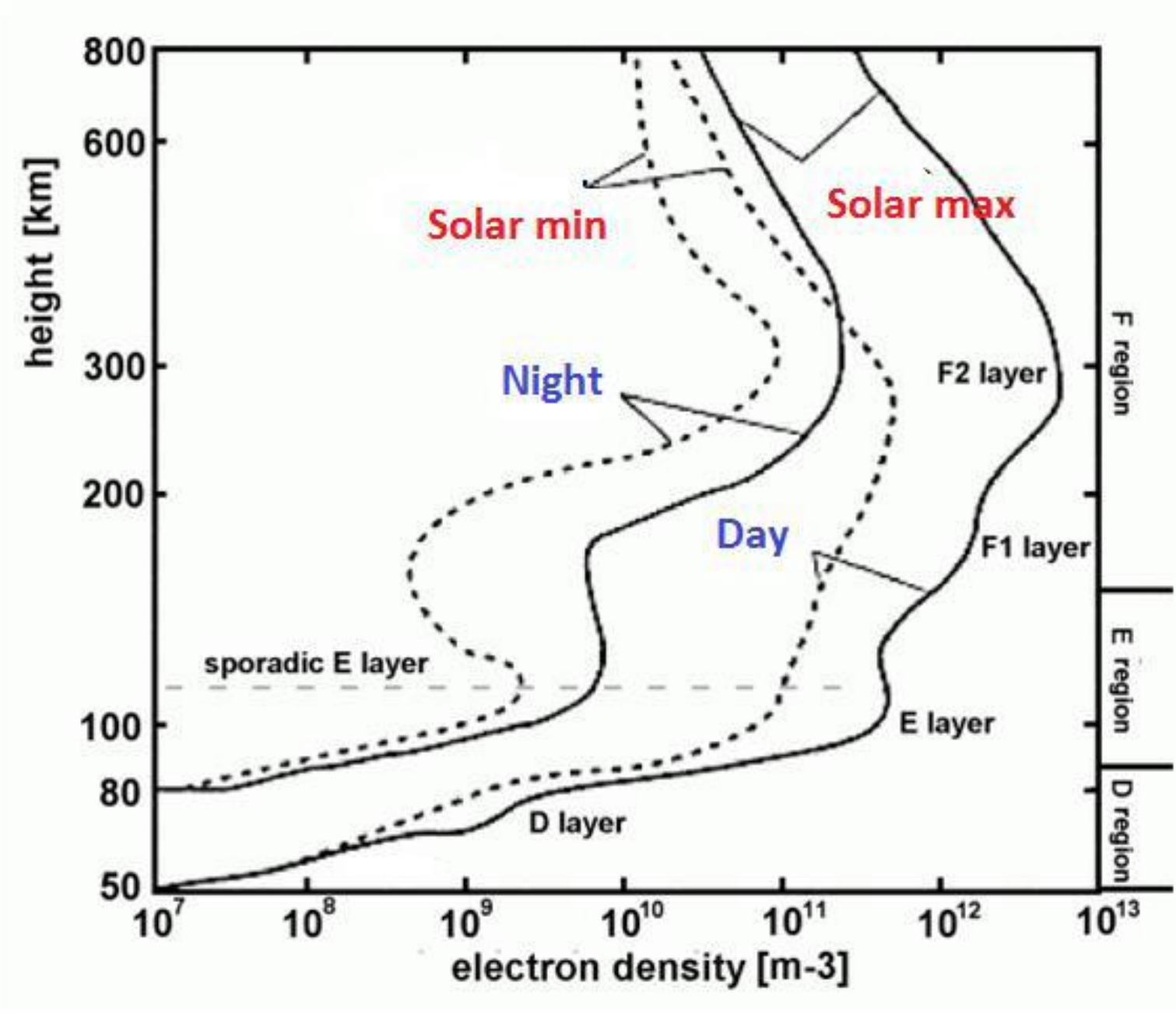
# Topside Ionosphere

- Above ~350 km, densities are so low that ions are not dominated by chemistry, but **diffusive equilibrium**



# Summary of Layers

- ❖ Layers are dominated by different ions
- ❖ Ion densities controlled by balance between production and loss; depends on chemical reactions in each altitude range
- ❖ Decay of layers at night depends on recombination rates and densities: low densities at high altitudes mean few collisions



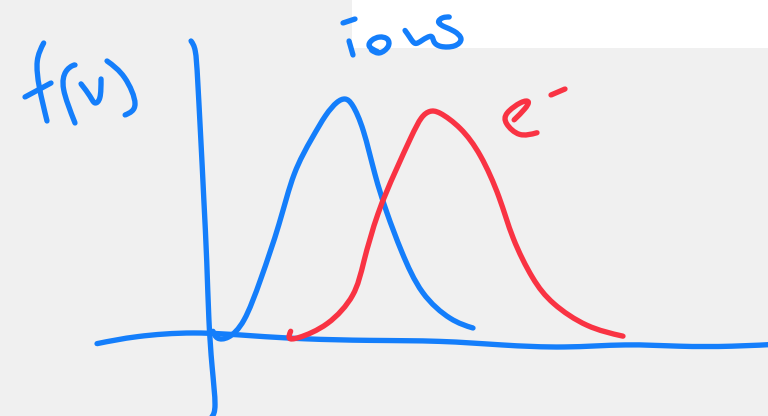
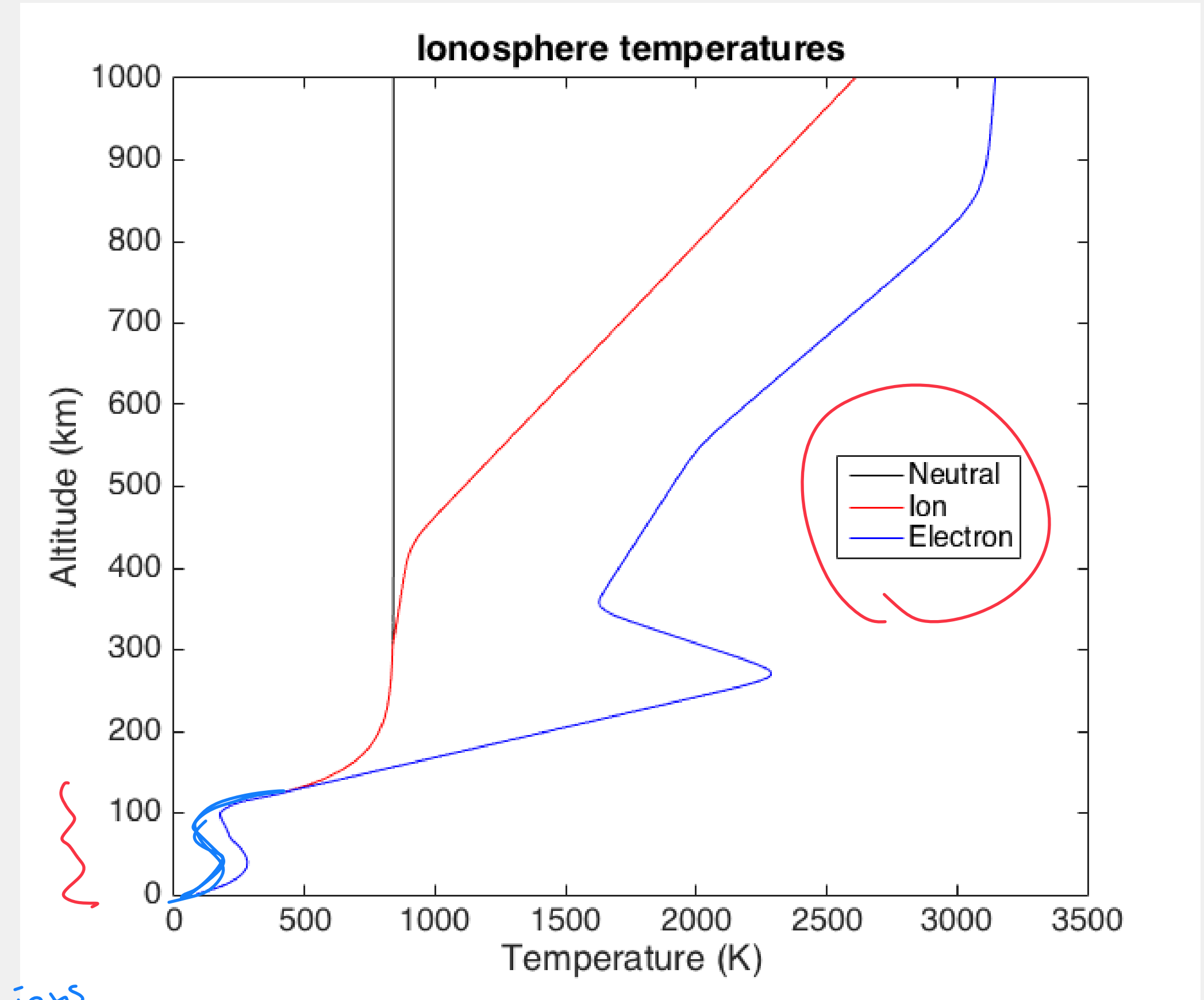
Ionospheric Layer	Altitude Range (km)	Major Constituents	Notable Characteristics
D	70–90	NO+ O <sub>2</sub> + (molecular)	Disappears (recombines) very rapidly—minutes after sundown
E	90–140	O <sub>2</sub> + (molecular) NO+	Recombines rapidly—often disappears before midnight
F1	140–200	O+ (atomic) NO+	Mostly recombines after sundown, but pockets of ionization may remain
F2	200–400	O+ (atomic)	Persistent because of low collision rates, but density decreases after sundown
Topside	> 400	O+ (atomic) H+	Merges into the plasmasphere, atomic oxygen dominates at lower altitudes, and hydrogen dominates at higher altitudes.



# Ionosphere Temperatures

collisions  
(nu)  $\leftrightarrow$  B-field

- ❖ Below 110 km, temperatures are made equal by collisions
- ❖ Above ~110 km, collisions are rare, so each species gets its temperature through different heating processes (radiation absorption, convection, etc)
- ❖ Above ~110 km: ions, electrons, and neutrals have different temperatures
- ❖ Remember: this simply means they have different velocity / energy distributions



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# Ionosphere Variability



# Transport

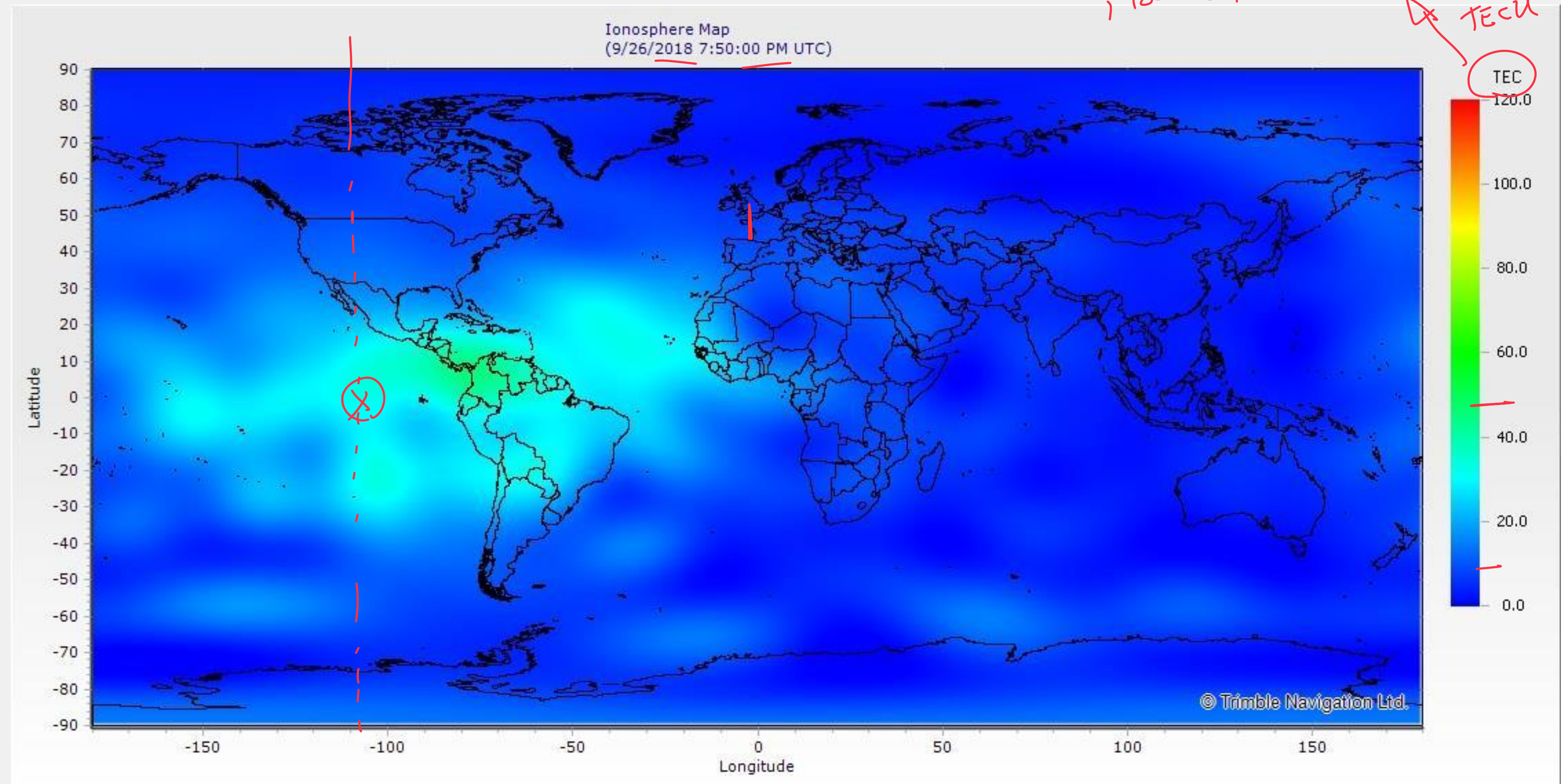
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- ❖ Variety of processes move plasma in the ionosphere:
  - ❖ **Winds**: neutral winds drag ions along with them, if collision frequency is high enough
  - ❖ **Drifts**: various forces cause plasma to “drift”: electric and magnetic fields; gravity; pressure; etc.
- ❖ **These contribute to complex spatial and temporal variations in the ionosphere**

# Global variation: Snapshots

$$\text{TEC} = \text{Total Electron Content} = \int_0^{\infty} n_e(z) dz, \quad e^-/\text{m}^2$$

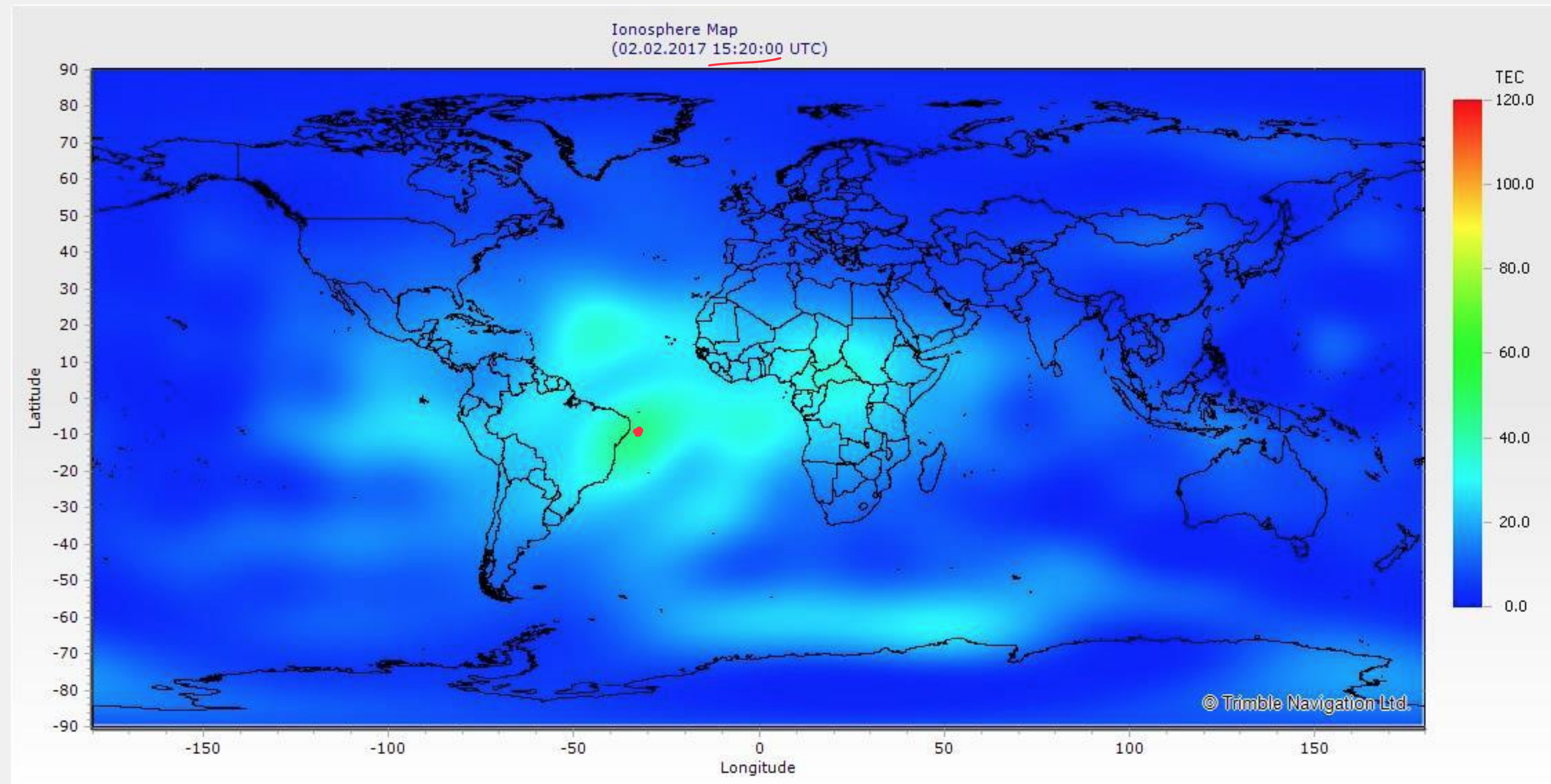
$1 \text{ TECU} = 10^{16} e^-/\text{m}^2$





# Global variation: Snapshots

- ❖ TEC = Total electron content; integrated in altitude, 1 TECU =  $10^{16}$  el/m<sup>2</sup>





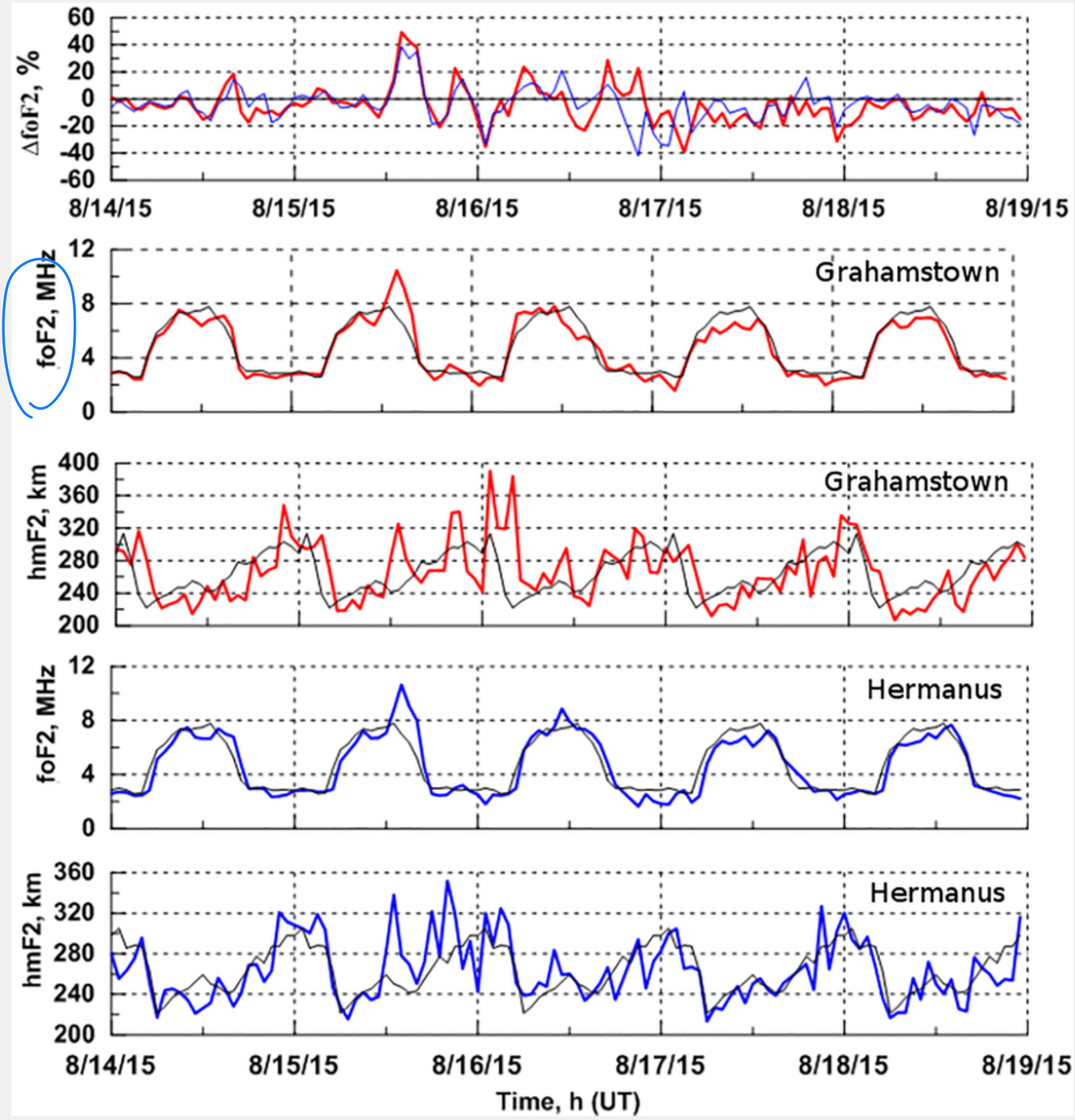
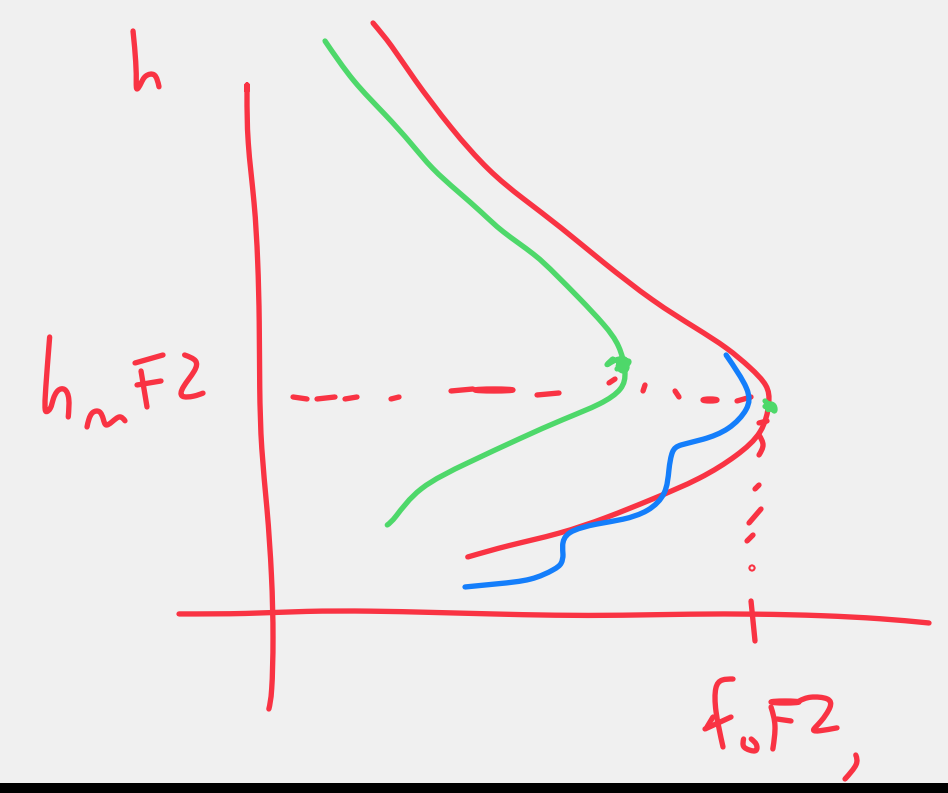
# foF2 and hmF2

❖ We often characterize the ionosphere by its peak density, foF2, and the altitude where that occurs, hmF2

❖ foF2 is a frequency in MHz. related to electron density:

$$\omega_{pe} = \sqrt{\frac{n_e q_e^2}{m_e \epsilon_0}} \sim \sqrt{n_e}$$
  
(kHz)  
$$f_{pe} = \frac{\omega_{pe}}{2\pi} \approx 9 \sqrt{n_e \text{ (cm}^{-3}\text{)}}$$

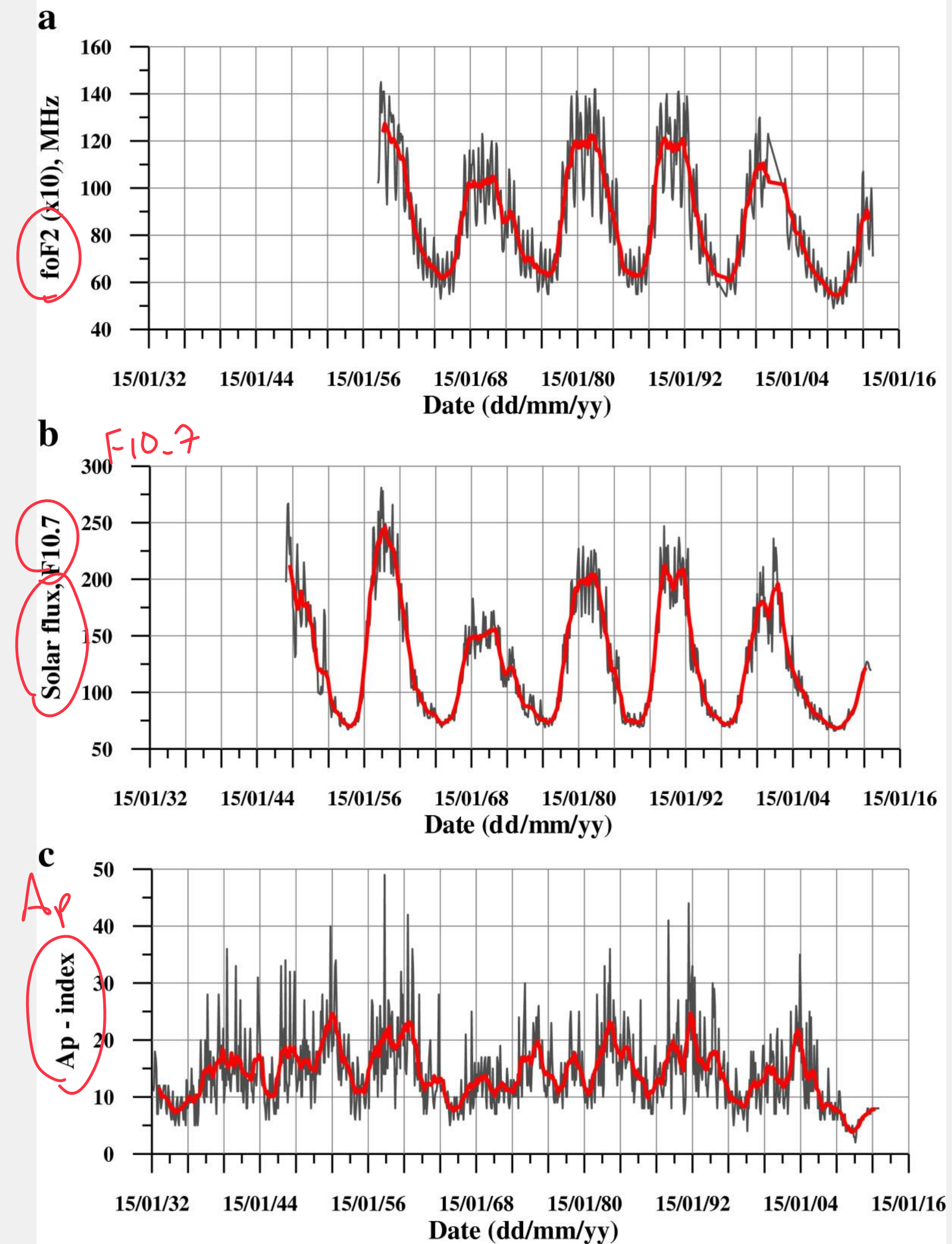
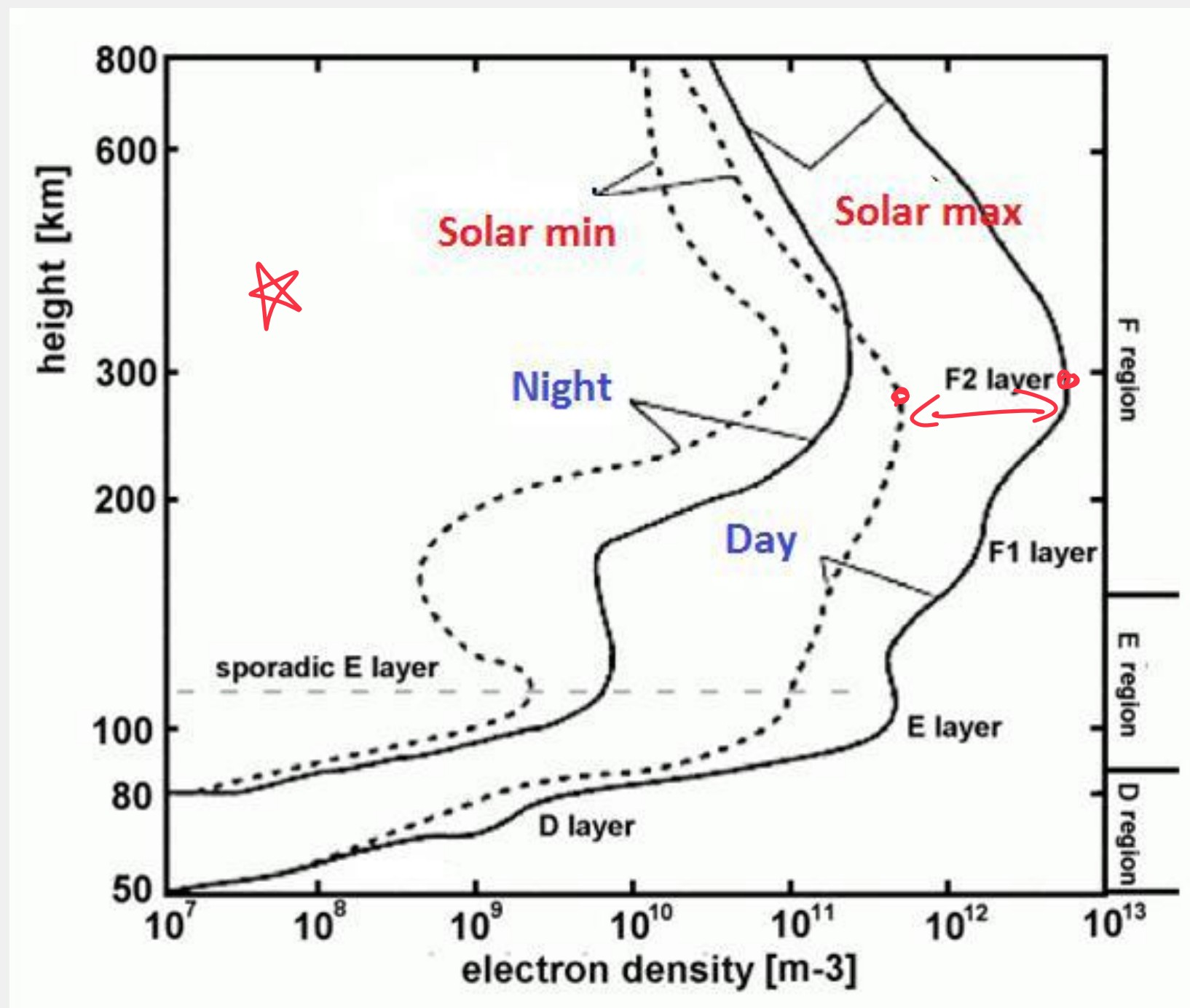
❖ hmF2 is simply altitude in km





# Solar Cycle Variation

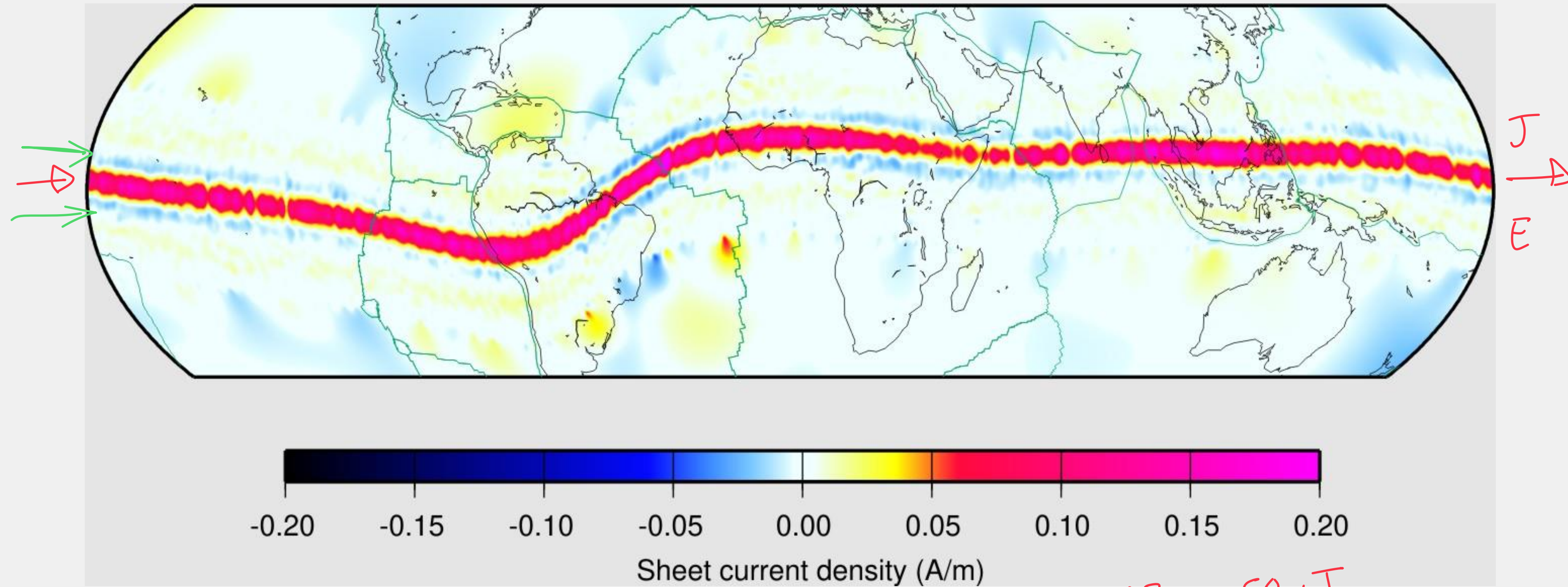
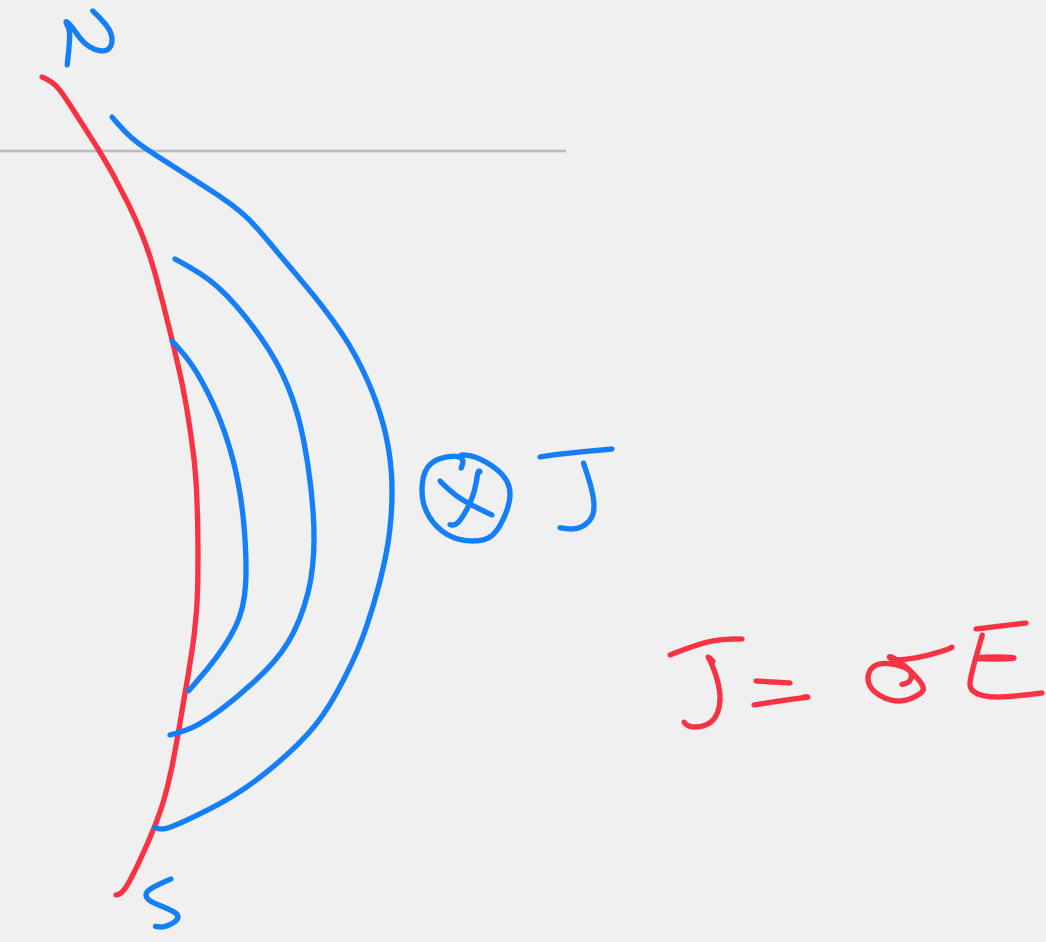
- ❖ Densities are much higher (order of magnitude) at solar maximum compared to solar minimum
- ❖ Higher EUV / X-ray fluxes lead to higher ionization rates





# Equatorial Electrojet

- ❖ Plasma physics involving B-field lead to an intense **current** that flows East in the dayside ionosphere
- ❖ Restricted to narrow region in latitude; 110-130 km altitude

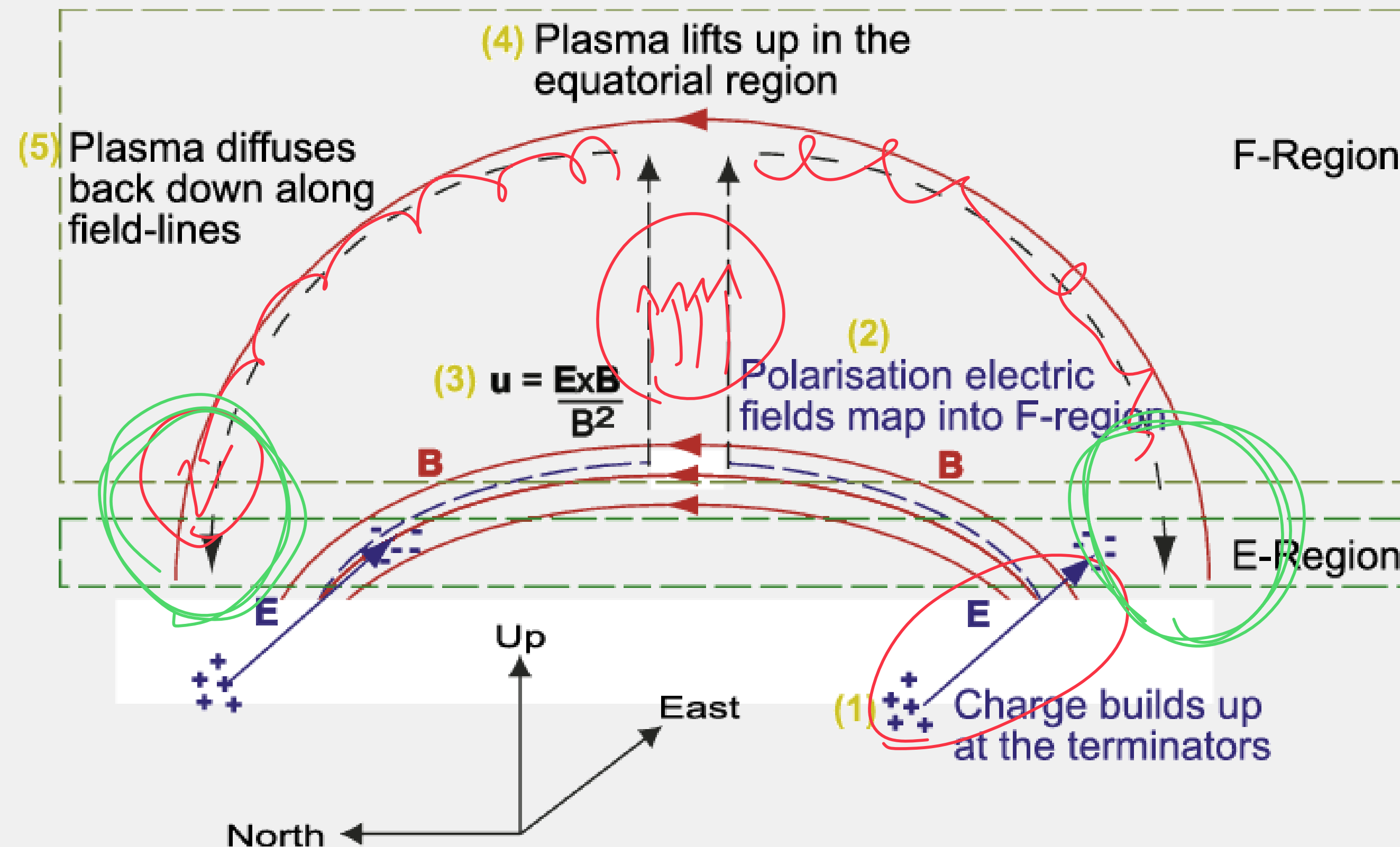


$\sim 100 \text{ kA}$   $\Delta B \sim 50 \text{ nT}$



# Equatorial Anomaly

- ❖ Due to the EEJ current, an electric field arises
- ❖  $E \times B$  leads to a **drift** (known as  $E \times B$  drift) in the vertical direction
- ❖ Plasma rises, but then above some altitude, falls back down along field lines
- ❖ “Fountain effect”

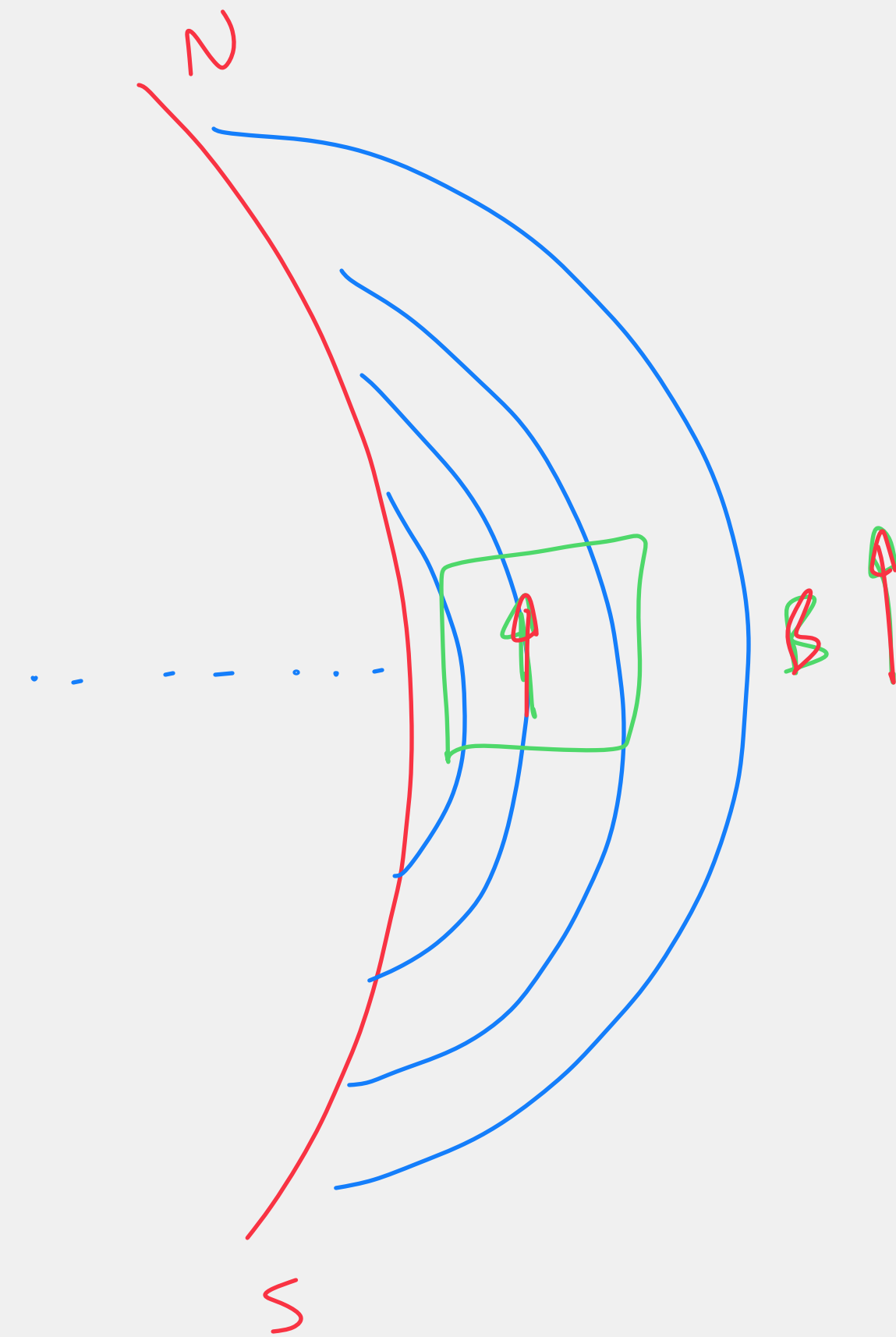
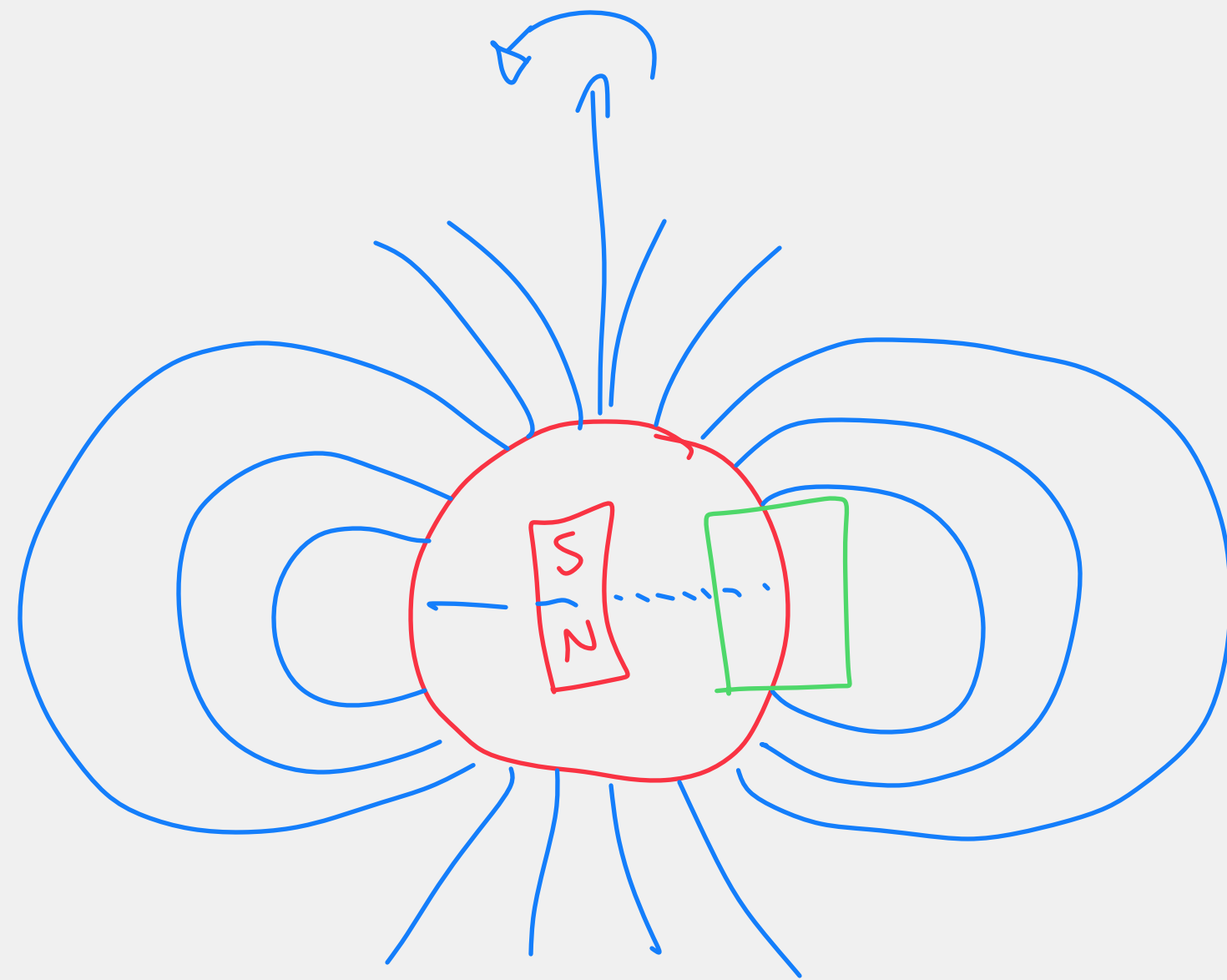


$$\bar{V}_d = \frac{\bar{F} \times \bar{B}}{qB^2}$$

$$\bar{F} = q\bar{E}$$

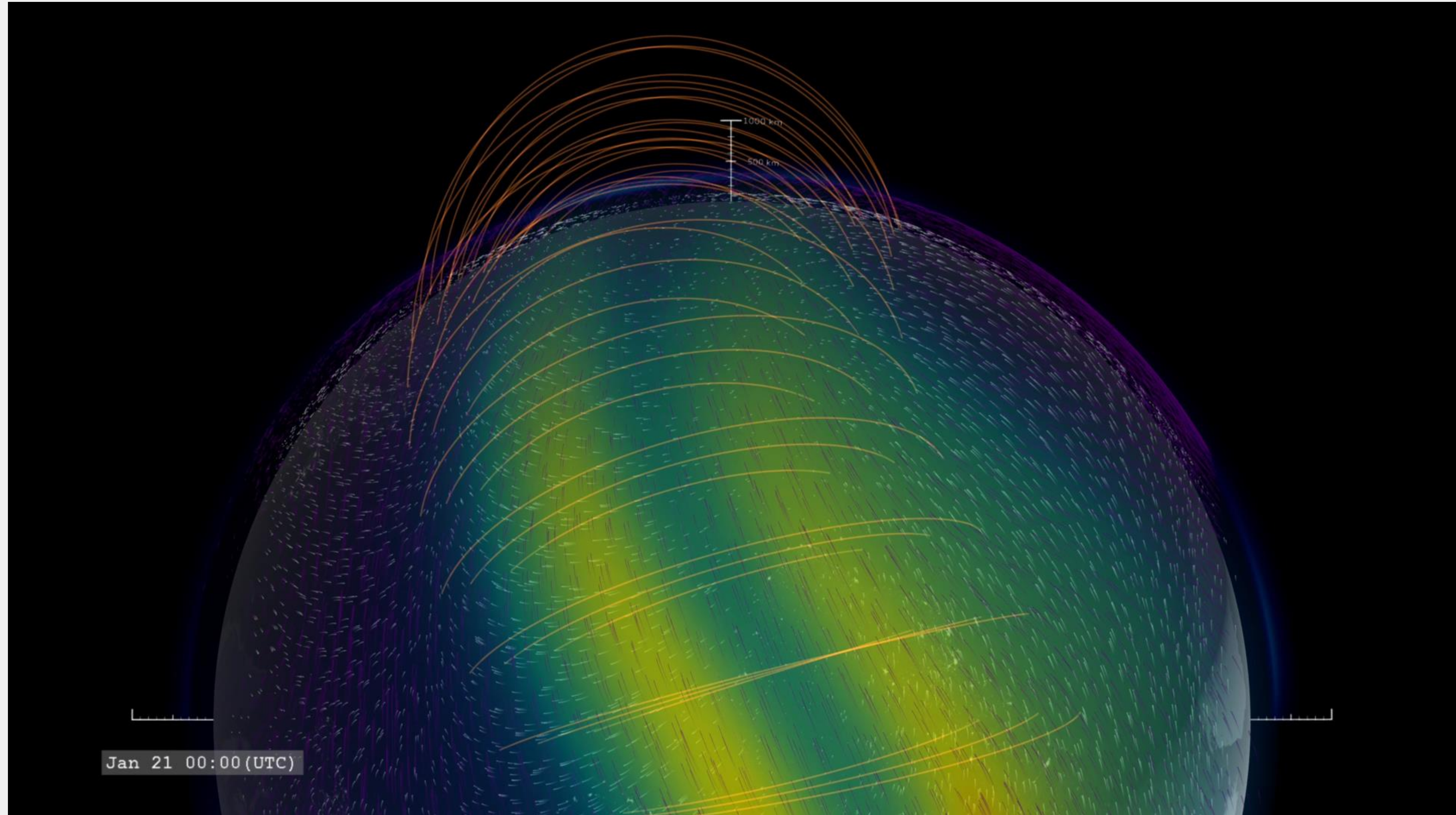
$$\bar{V}_d = \frac{\bar{E} \times \bar{B}}{B^2}$$

# Magnetic field





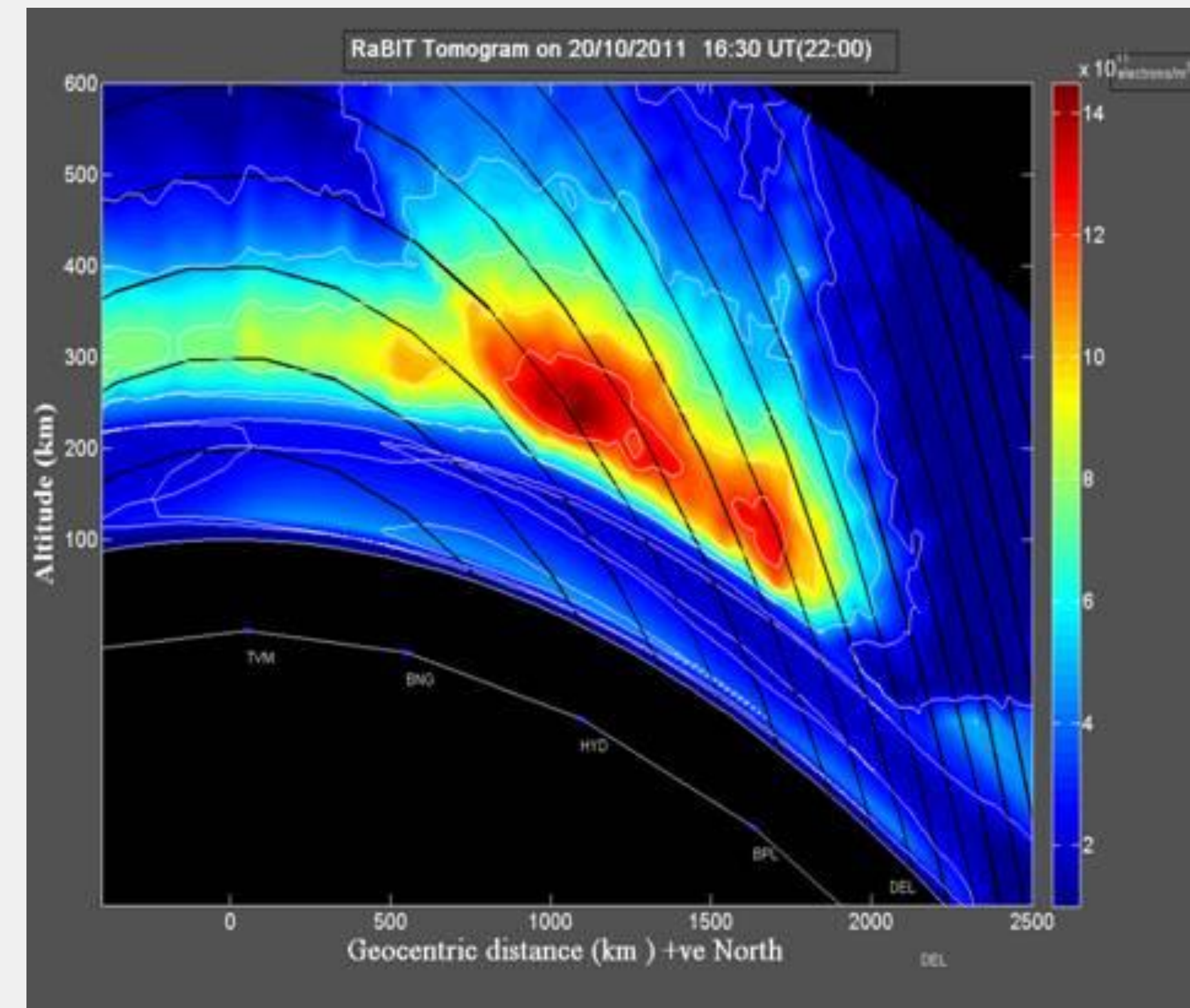
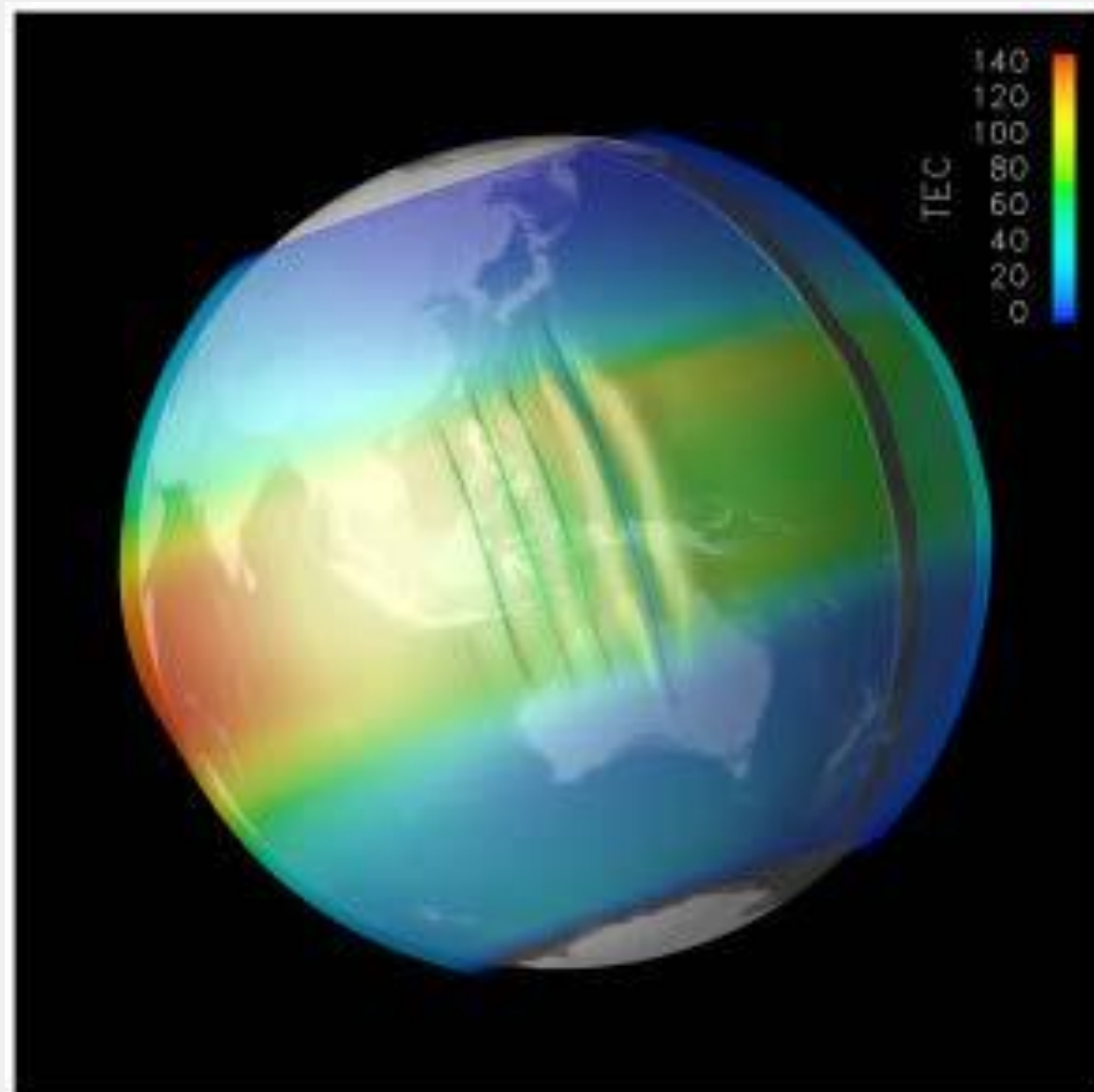
# Equatorial Anomaly





# Equatorial Spread-F

- ❖ Plasma instabilities that occur right after sunset cause the F-region to take on an array of structures
  - ❖ Times scales from seconds to hours
  - ❖ Spatial scales from cm to tens of km



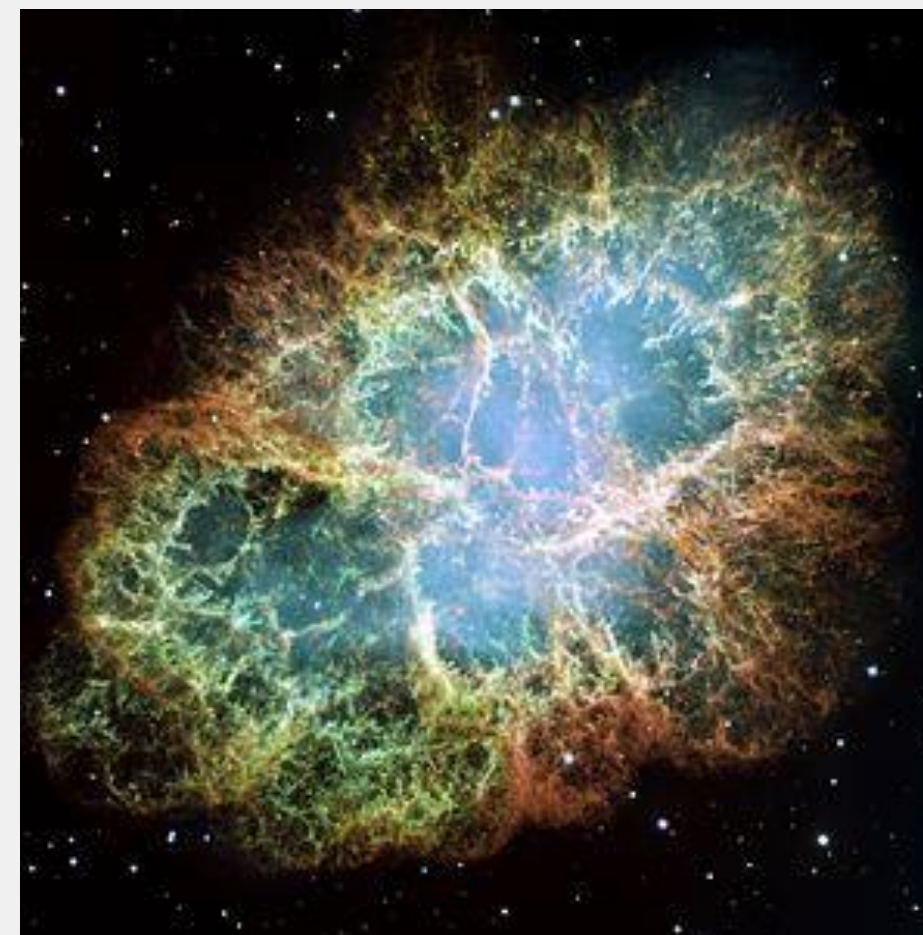
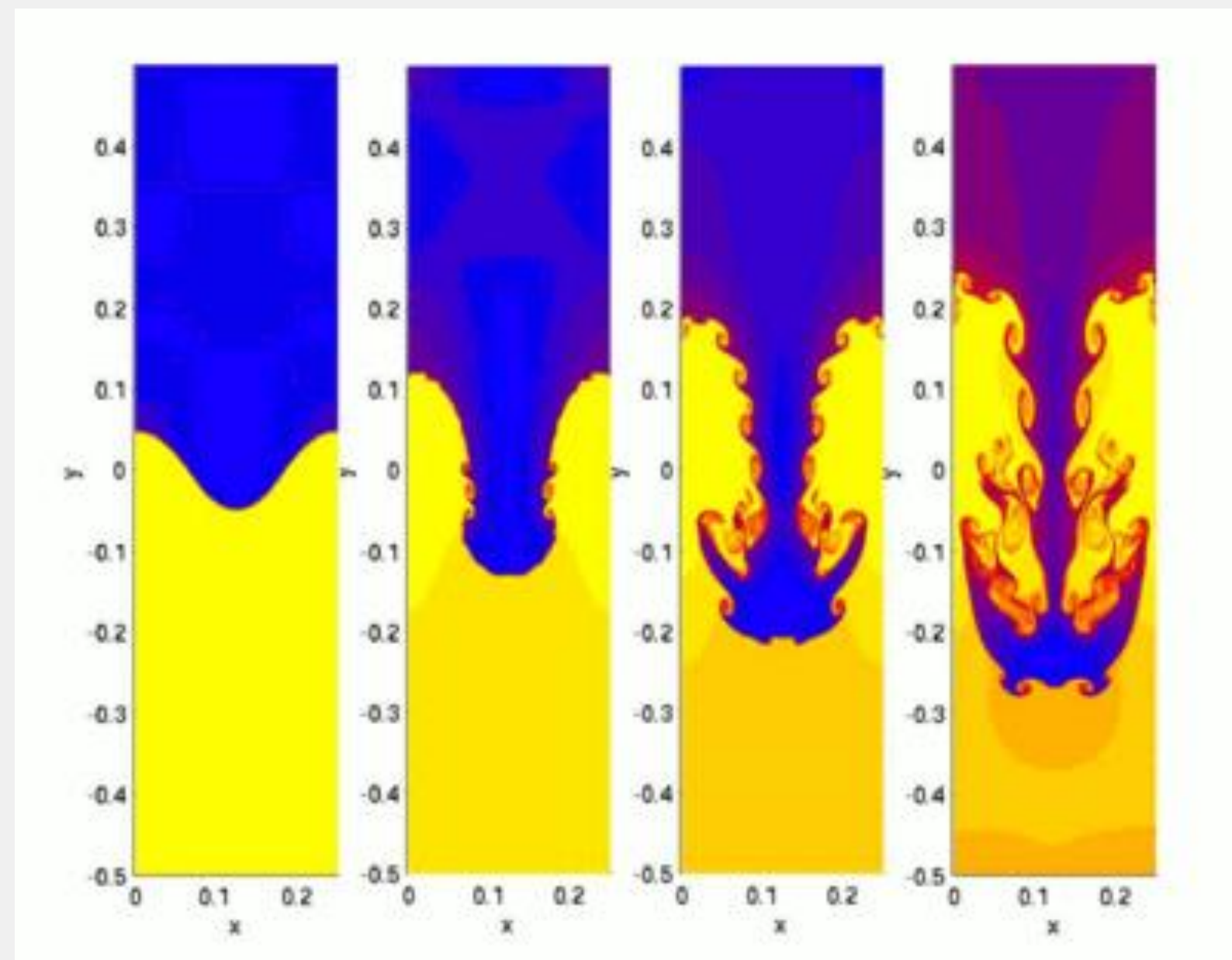


# Equatorial Plasma Bubbles

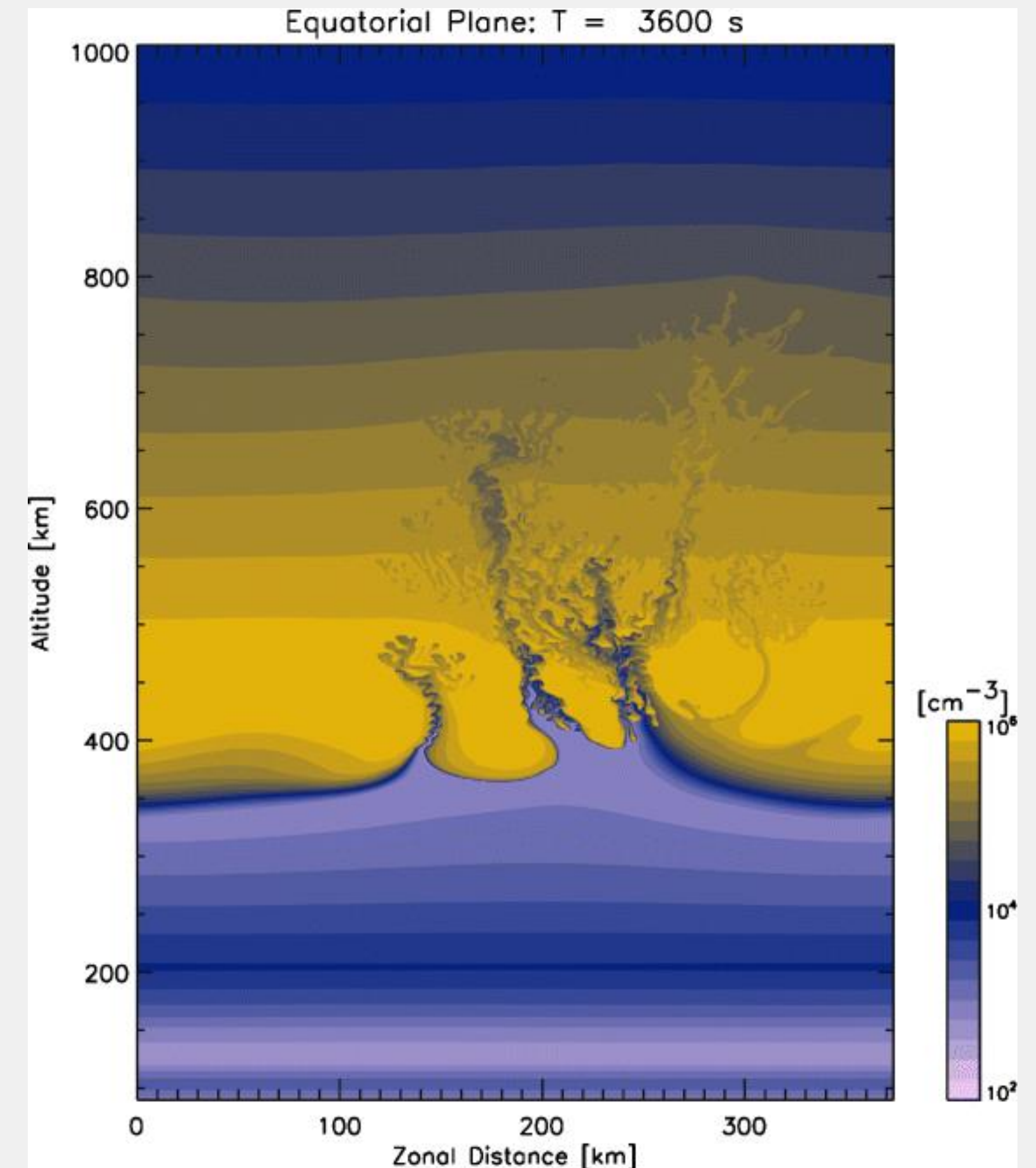
- ❖ Instability due to heavier fluid on top of lighter fluid:

*Rayleigh-Taylor Instability*

- ❖ Leads to rising bubbles with detailed structure and wide range of spatial scales, and large density variation

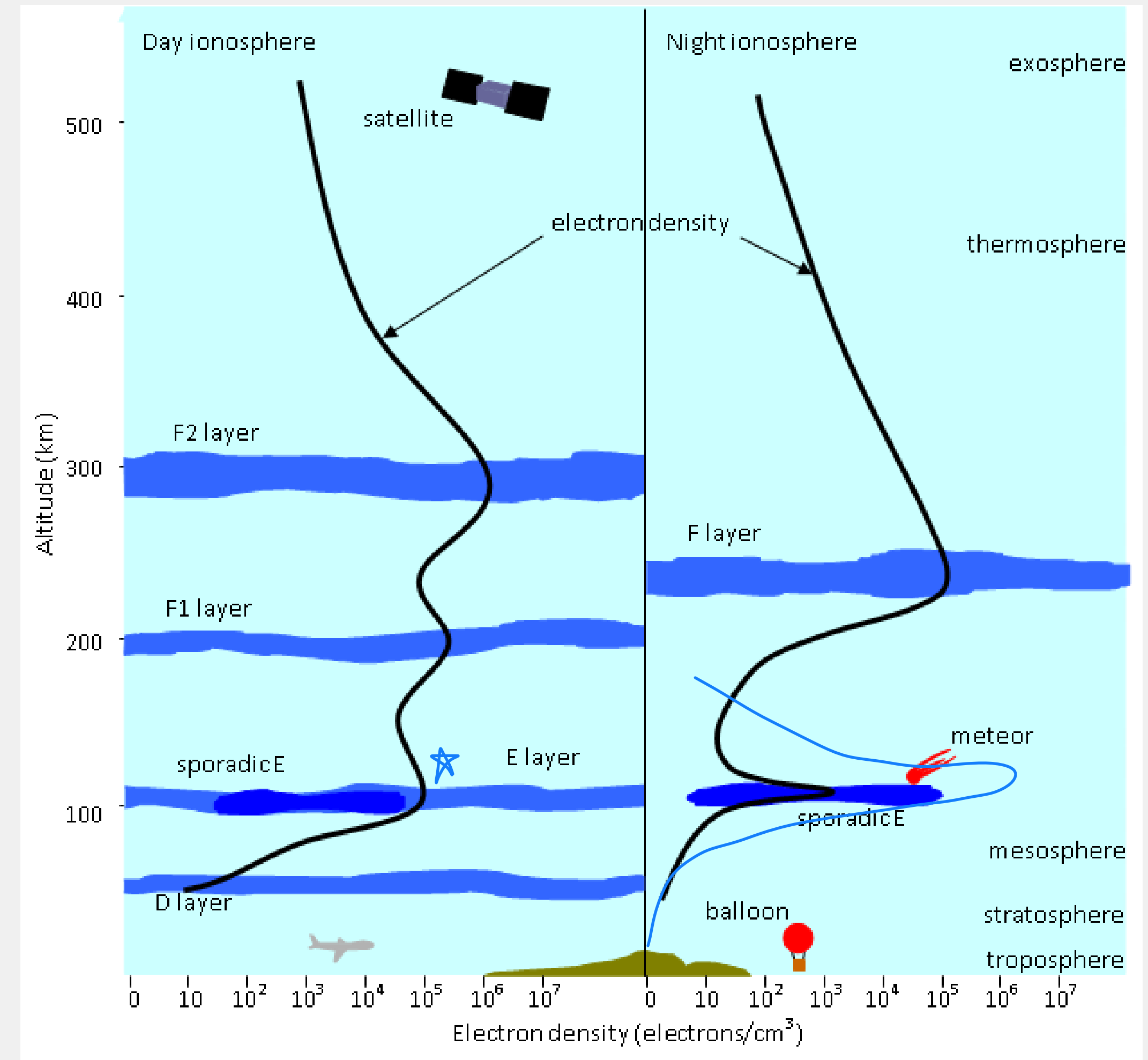
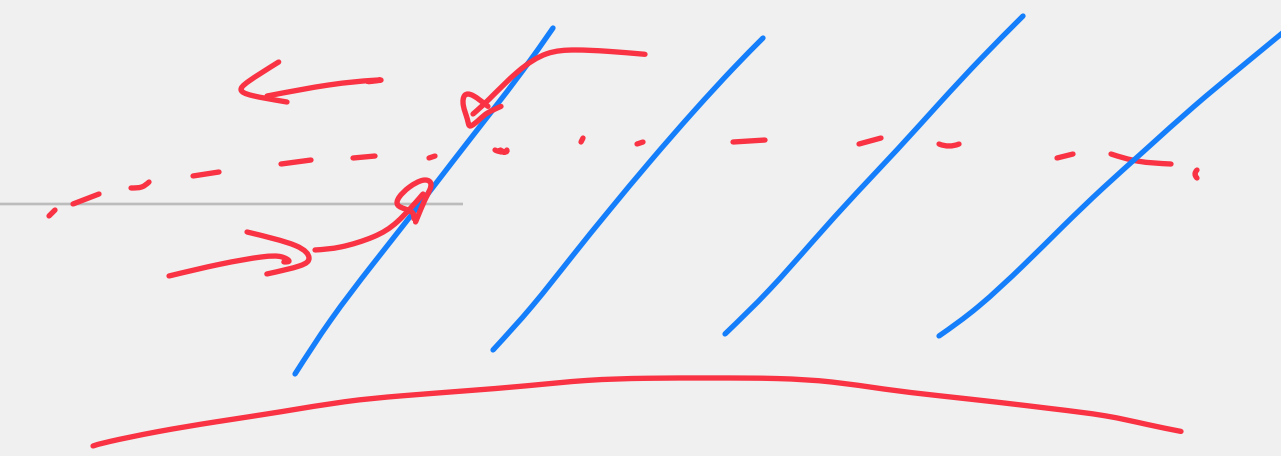


*Crab Nebula*



# Mid-latitudes: Sporadic E

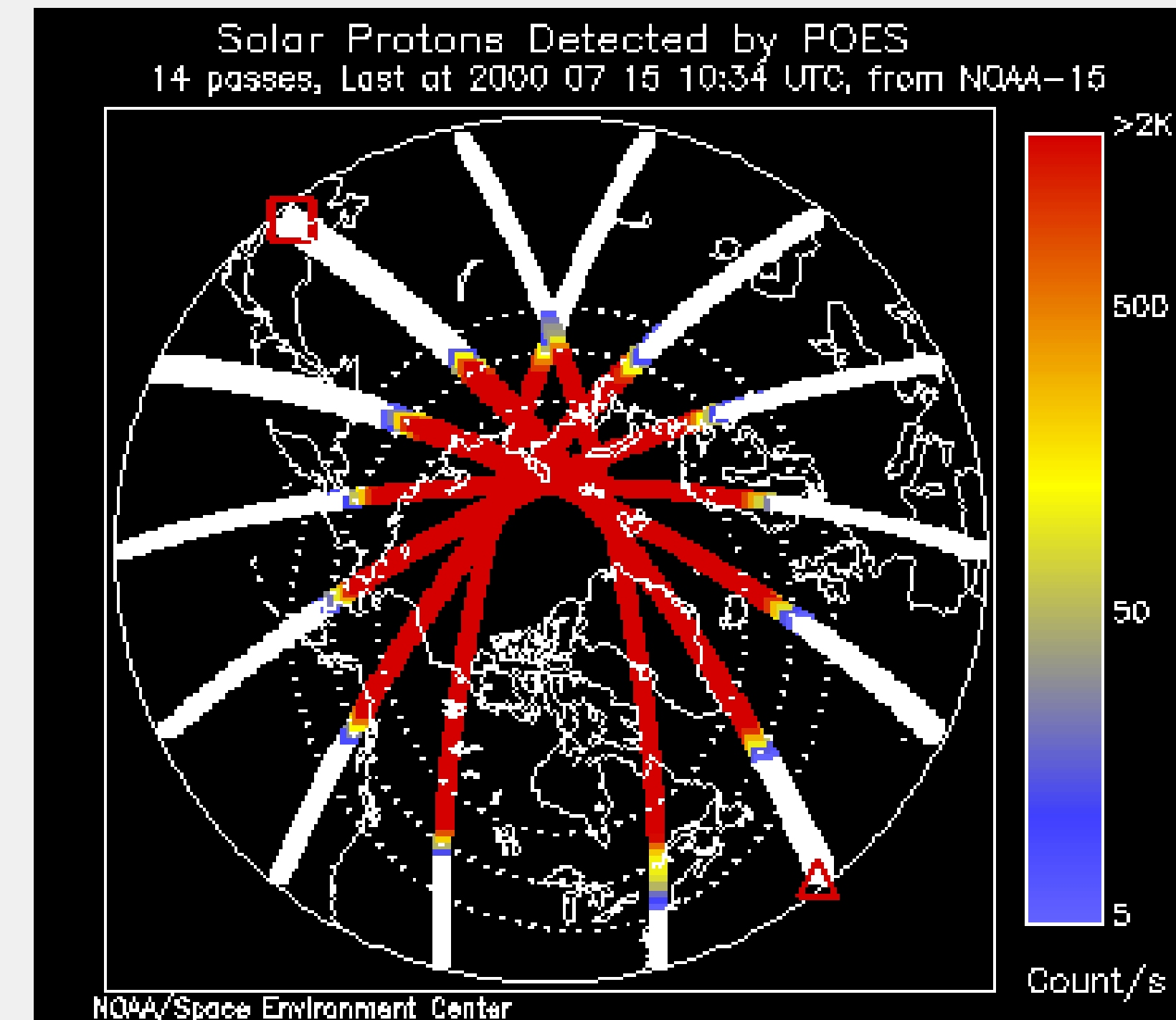
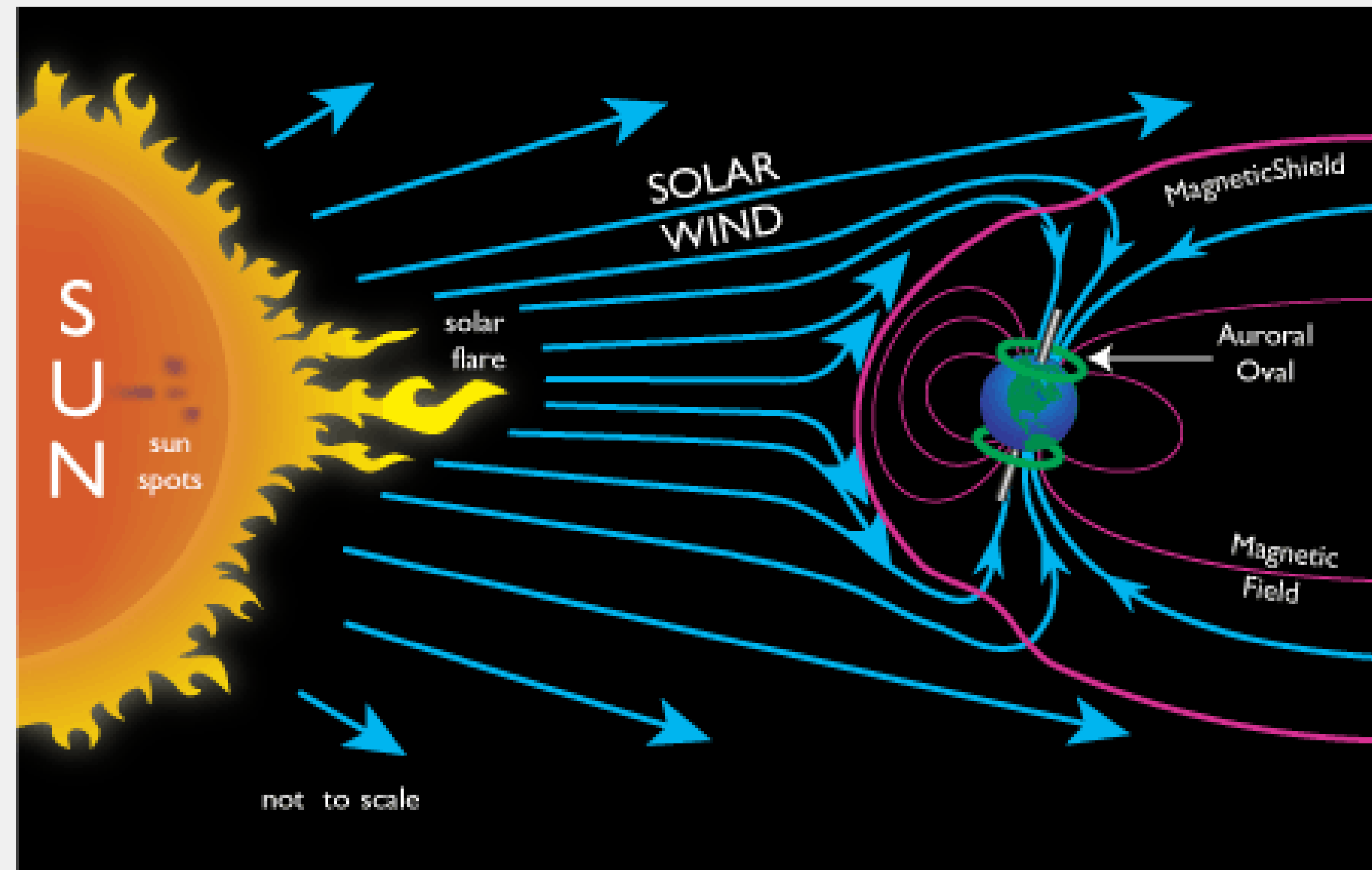
- ❖ Sporadic increase in E-region electron density, primarily at night, by orders of magnitude
- ❖ “Patch” of increased ionization
- ❖ Still not clear what the spatial scale is
- ❖ Observed by radio wave scattering
- ❖ Effect is most likely due to shear winds driving metal ions (from meteors) into thin layer





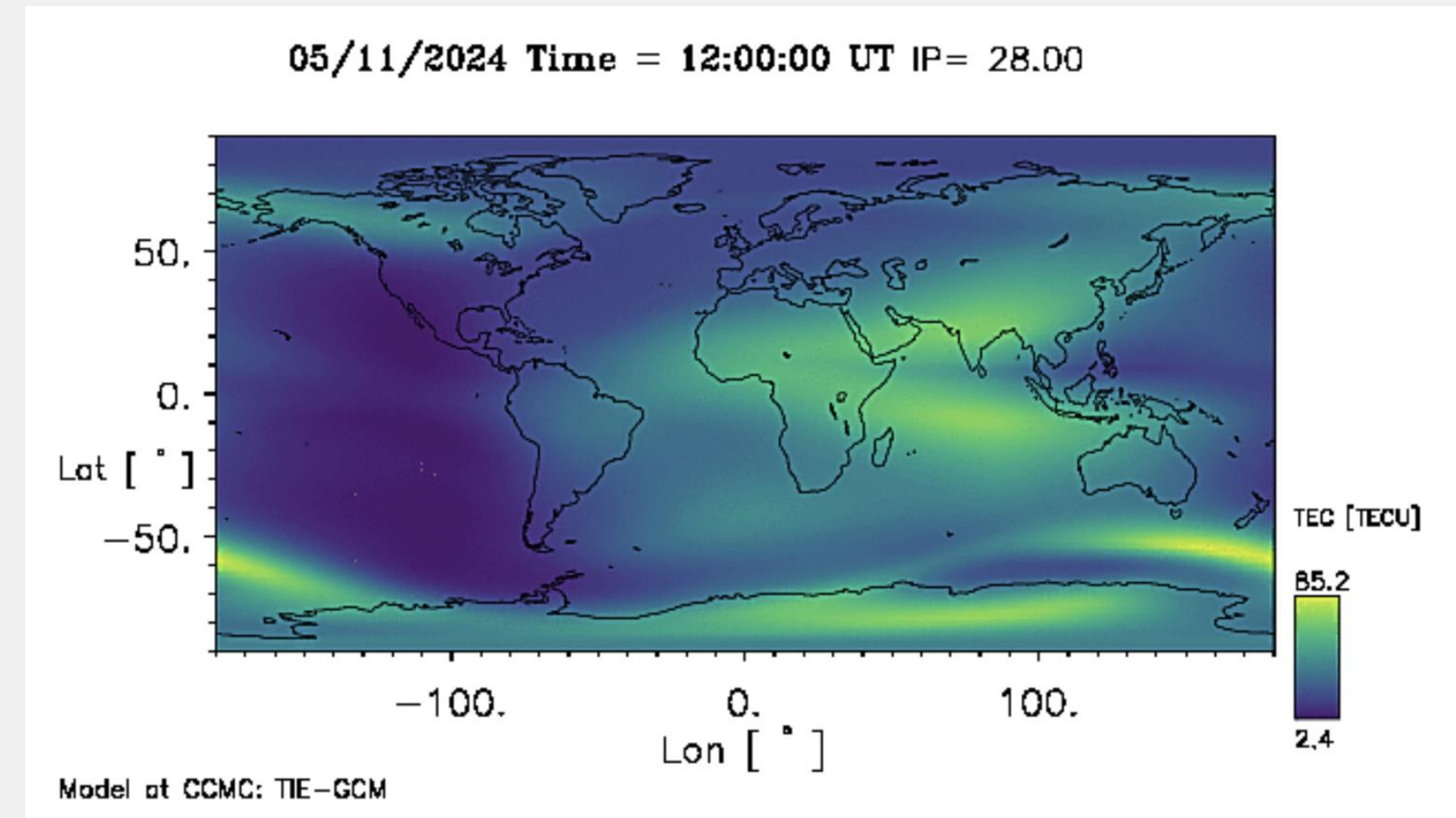
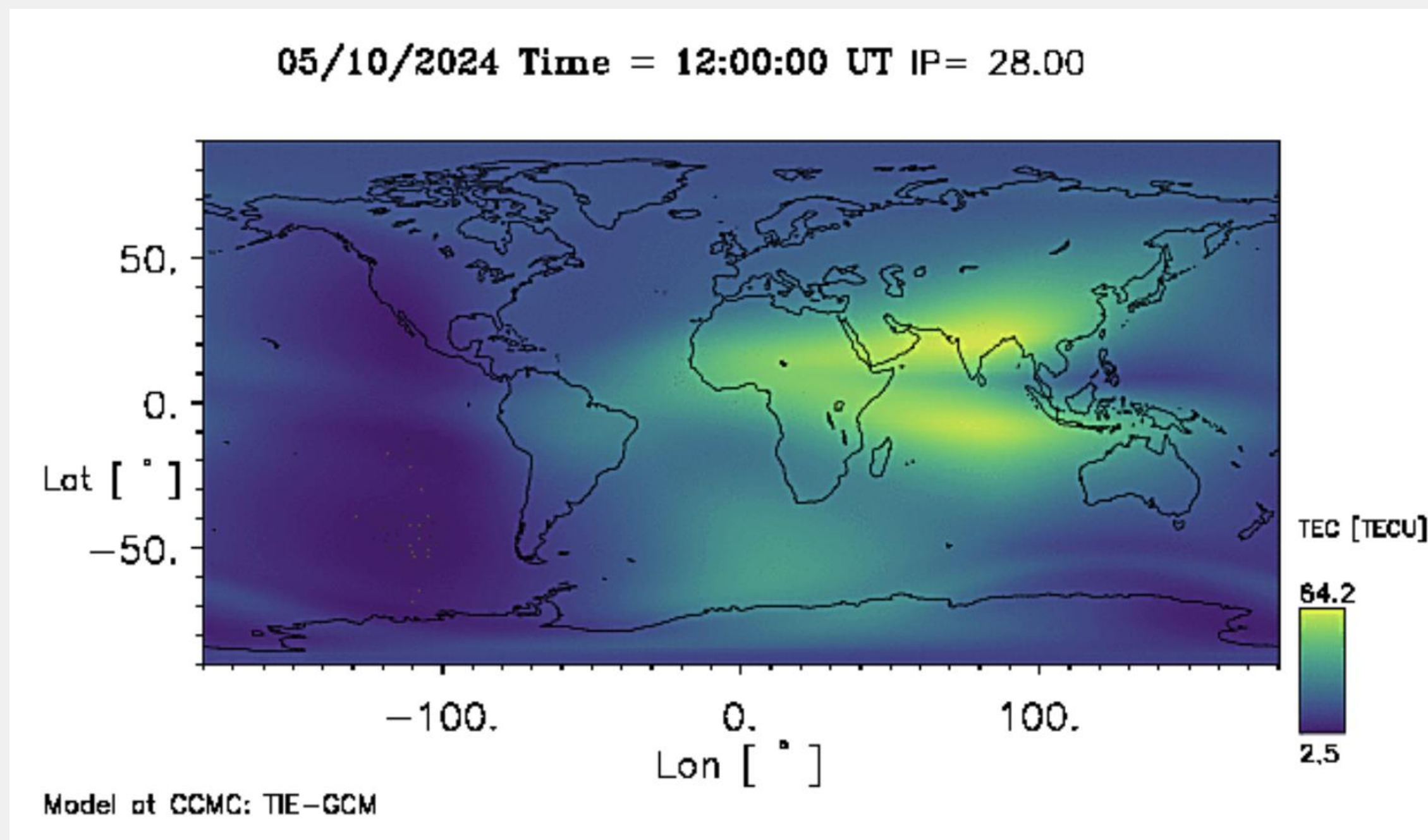
# High-Latitudes: Polar Cap Absorption

- ❖ Solar Energetic Protons (SEPs) deposit their energy in the D-region of the ionosphere
  - ❖ Flow along open magnetic field lines
- ❖ Increased D-region density adds to absorption of radio waves (discussed a bit later)



# Storm-time variability: Gannon Storm 2024

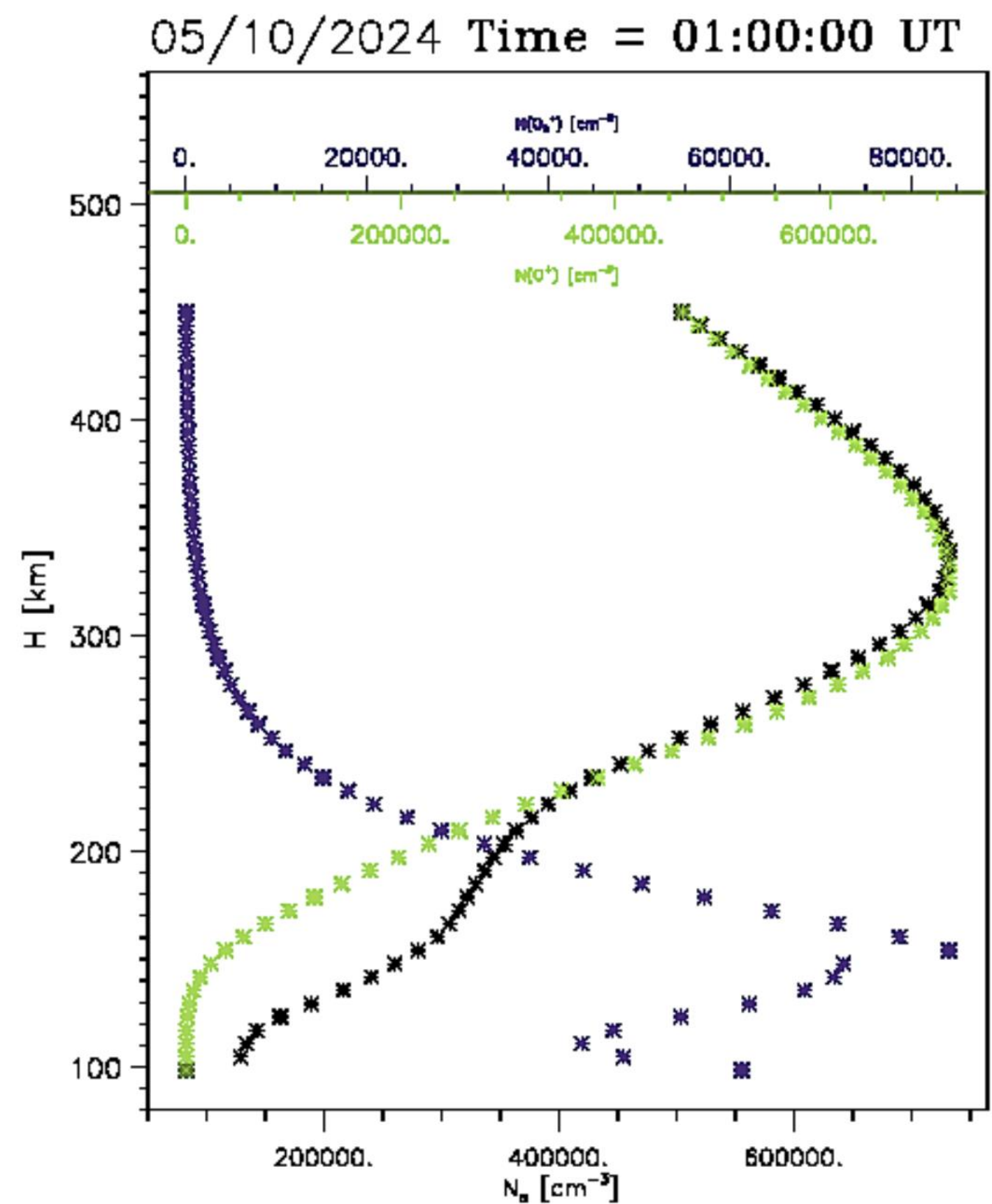
- ❖ TIE-GCM model runs
- ❖ Considerably higher TEC at high latitudes: energetic particle precipitation (EPP)
- ❖ TEC at low latitudes not significantly different here...
- ❖ Equatorial anomaly prominent in evening sector, less so in dawn / noon sector





# Storm-time variability: Gannon Storm 2024

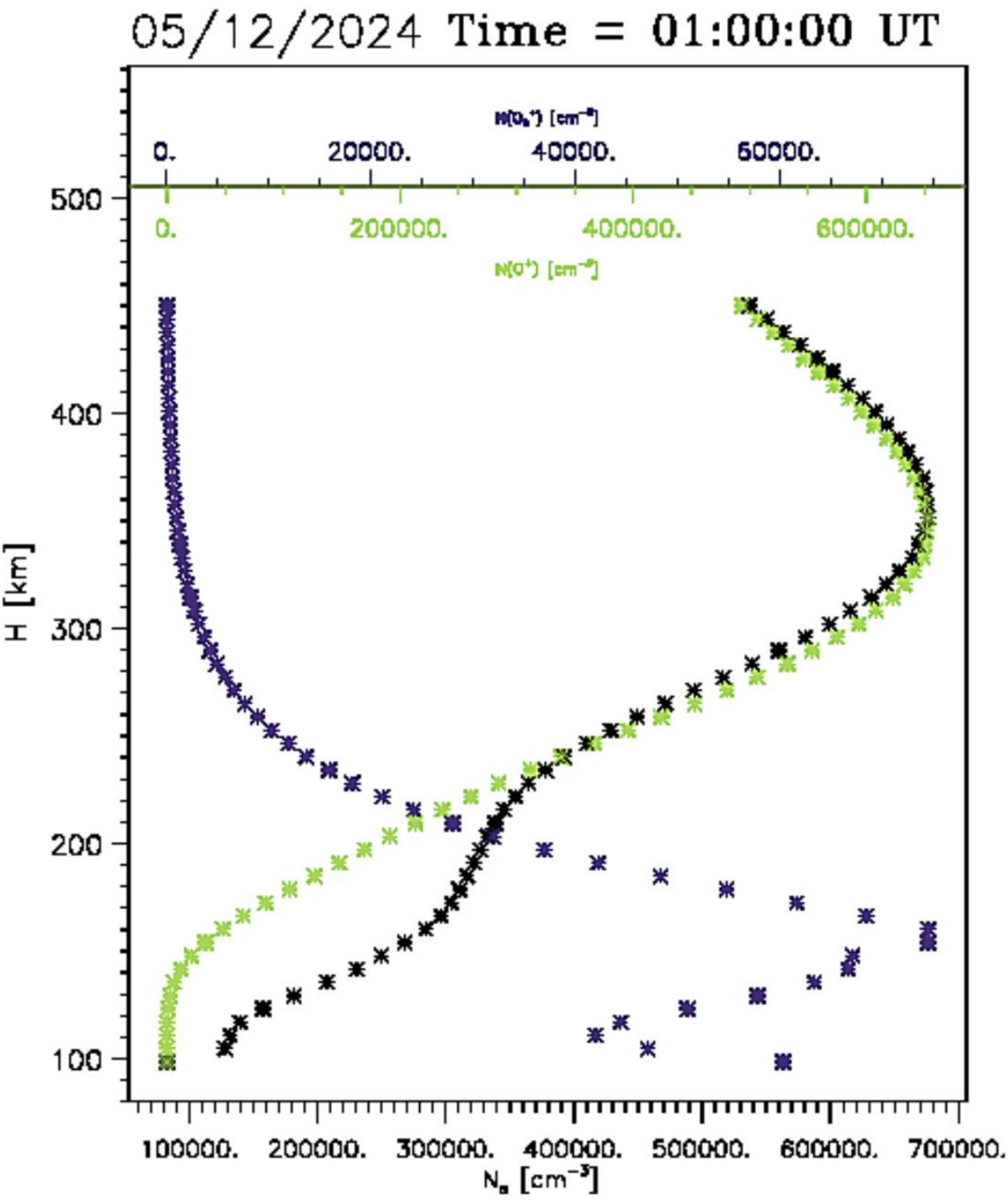
- ❖ TIE-GCM model runs
- ❖ Storm associated with increased EUV, X-ray: leads to higher ionization rates
- ❖ Higher temperature in the thermosphere raises the entire ionosphere



Lon [ ° ] = -175.000    Lat [ ° ] = 40.0000  
Model at CCMC: TIE-GCM

**Figure: Simulation of the ionosphere/thermosphere of the Earth.**  
[EPS image \(684.44 KB\)](#)

**Model: TIE-GCM**  
**Run: TIEGCM-Heelis-01\_2024-05-TP-02\_071624\_IT\_1**



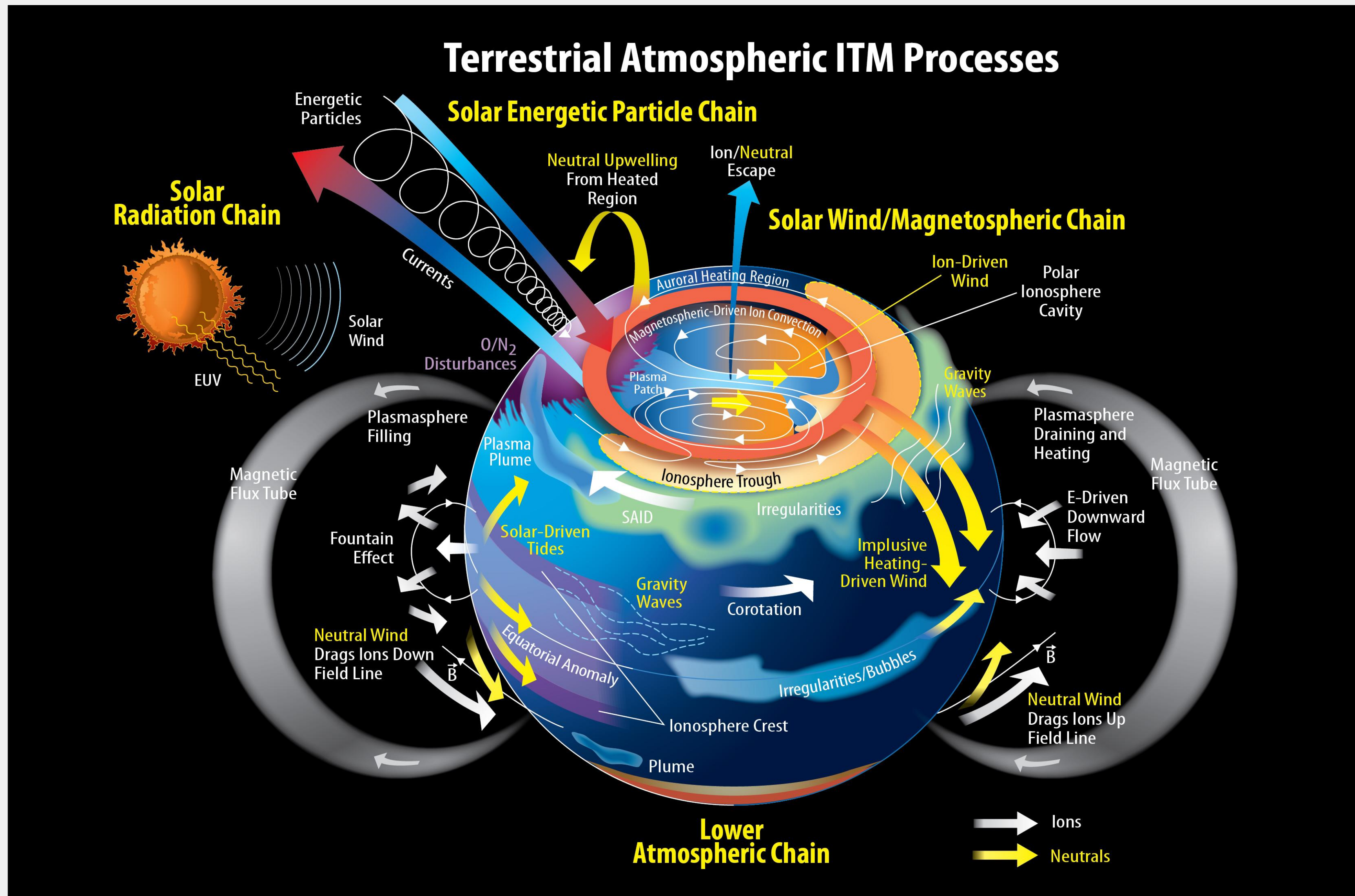
Lon [ ° ] = -175.000    Lat [ ° ] = 40.0000  
Model at CCMC: TIE-GCM

**Figure: Simulation of the ionosphere/thermosphere of the Earth.**  
[EPS image \(688.14 KB\)](#)

**Model: TIE-GCM**  
**Run: TIEGCM-Heelis-01\_2024-05-TP-02\_071624\_IT\_1**



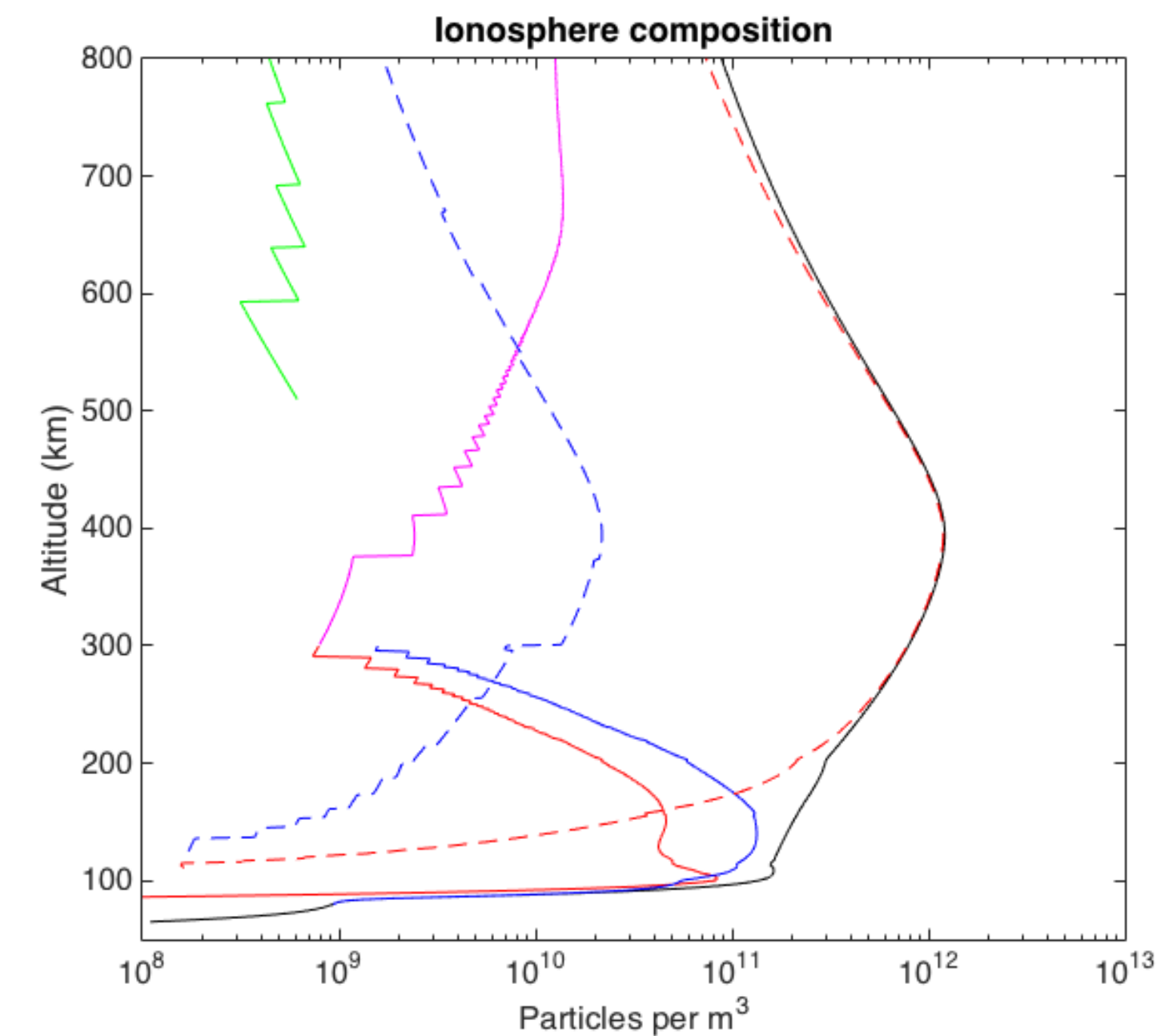
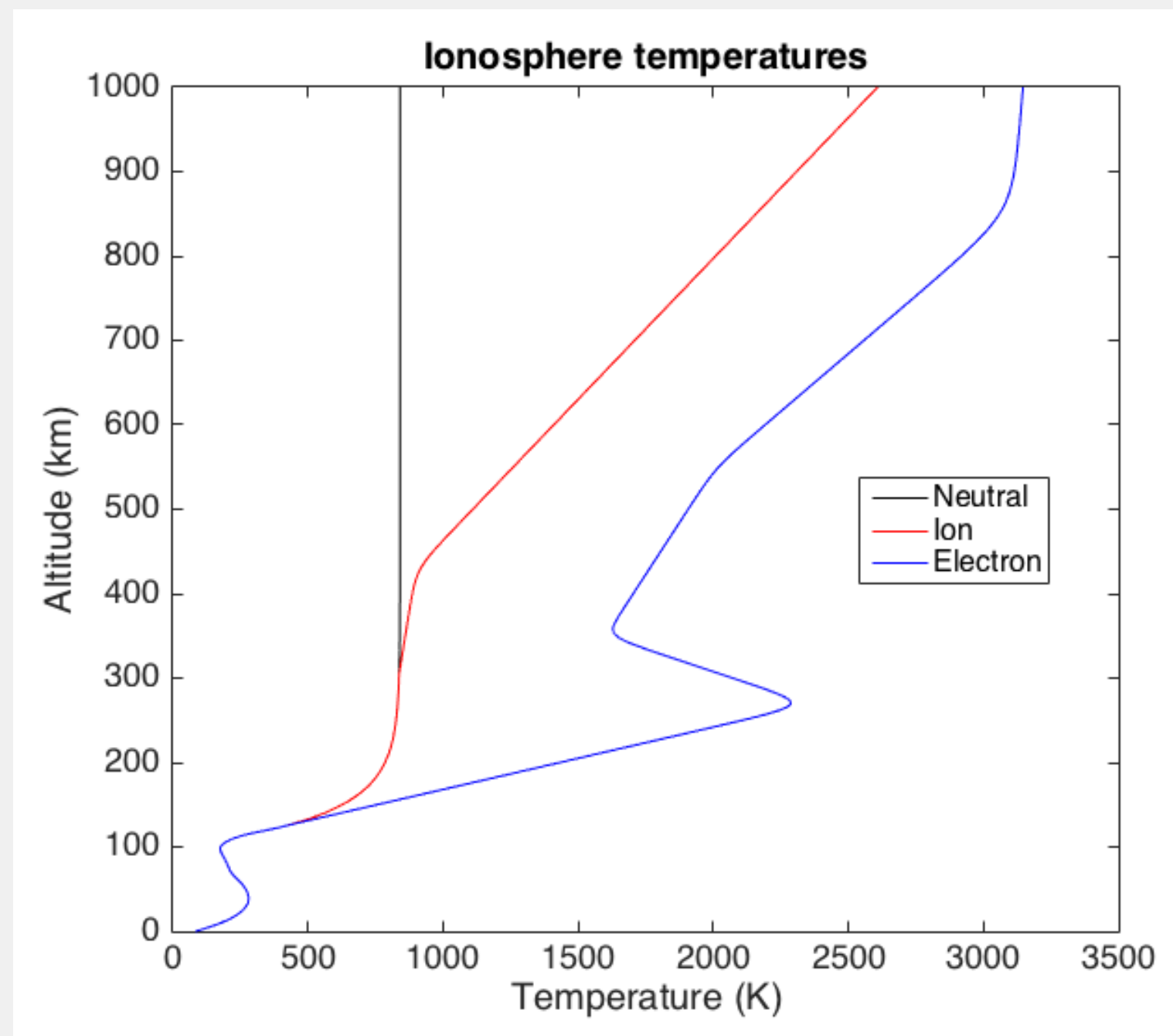
# Lots more to the Ionosphere / Atmosphere system...





# IRI model

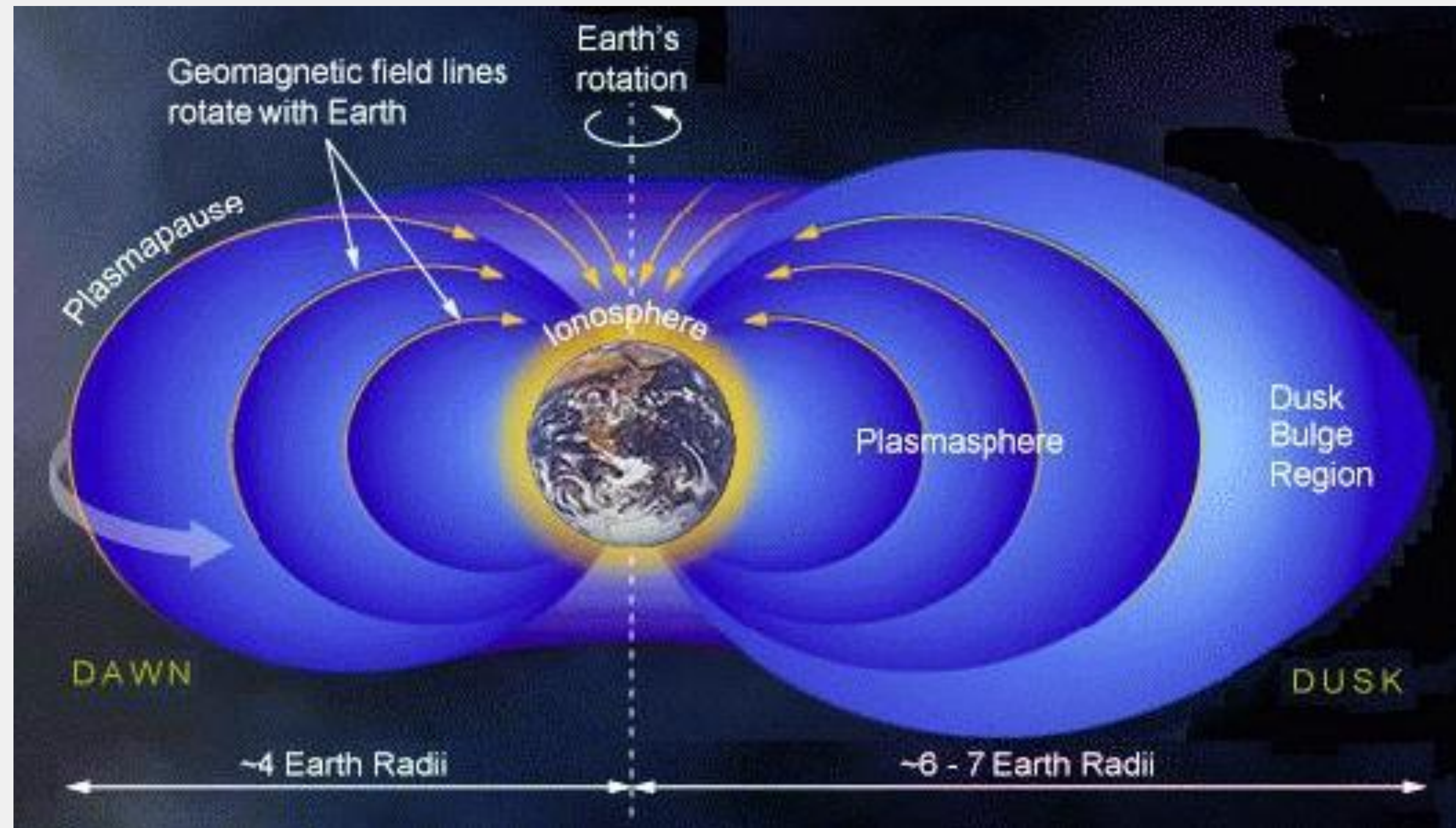
- ❖ International Reference Ionosphere: IRI
- ❖ [https://ccmc.gsfc.nasa.gov/modelweb/models/iri2012\\_vitmo.php](https://ccmc.gsfc.nasa.gov/modelweb/models/iri2012_vitmo.php)
- ❖ IRI is ionosphere equivalent to MSIS
- ❖ Empirical model; major data sources are the worldwide network of ionosondes, powerful incoherent scatter radars (Jicamarca, Arecibo, Millstone Hill, Malvern, St. Santin), ISIS and Alouette topside sounders (spacecraft), in situ instruments flown on many satellites and rockets.
- ❖ IRI is updated yearly during special [IRI Workshops](#) at COSPAR and URSI meetings





# Plasmasphere

- ❖ Boundary between Topside ionosphere and Plasmasphere: where thermal pressure and magnetic pressure are equal
  - ❖ Plasma becomes confined by B-field
- ❖ Sometimes defined by altitude where  $H^+$  (protons) become dominant ion





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# Ionosphere Effects: Radio Wave Propagation

# Radio Wave Propagation

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- ❖ Time for some (more) plasma physics!
  - ❖ Plasma oscillations
  - ❖ Plasma frequency
  - ❖ index of refraction (from Maxwell's equations)
  - ❖ Add collisions: absorption
  - ❖ MUF, LUF, X-ray effect



$$E = -\frac{q_e n_e}{\epsilon_0} x$$

$$ma = \vec{F} = q_e E$$

$$m_e \frac{dv}{dt} = m_e \frac{d^2 x}{dt^2} = -\frac{q_e^2 n_e}{\epsilon_0} x$$

$$\frac{d^2 x}{dt^2} + \underbrace{\frac{q_e^2 n_e}{m_e \epsilon_0}}_{\omega_p^2} x = 0$$

$$\Rightarrow x(t) = A \cos(\omega_p t)$$

$$\omega_p = \sqrt{\frac{q_e^2 n_e}{m_e \epsilon_0}} \approx k \sqrt{n_e}$$

$$V_p = \frac{c}{n} = \frac{c}{\sqrt{\epsilon_r}}$$

$$\epsilon \text{ (permittivity)} = \epsilon_0 \epsilon_r$$

plasma: 
$$n^2 = 1 - \frac{\omega_p^2}{\omega^2}$$

$$\text{at } \omega = \omega_p, n = 0$$

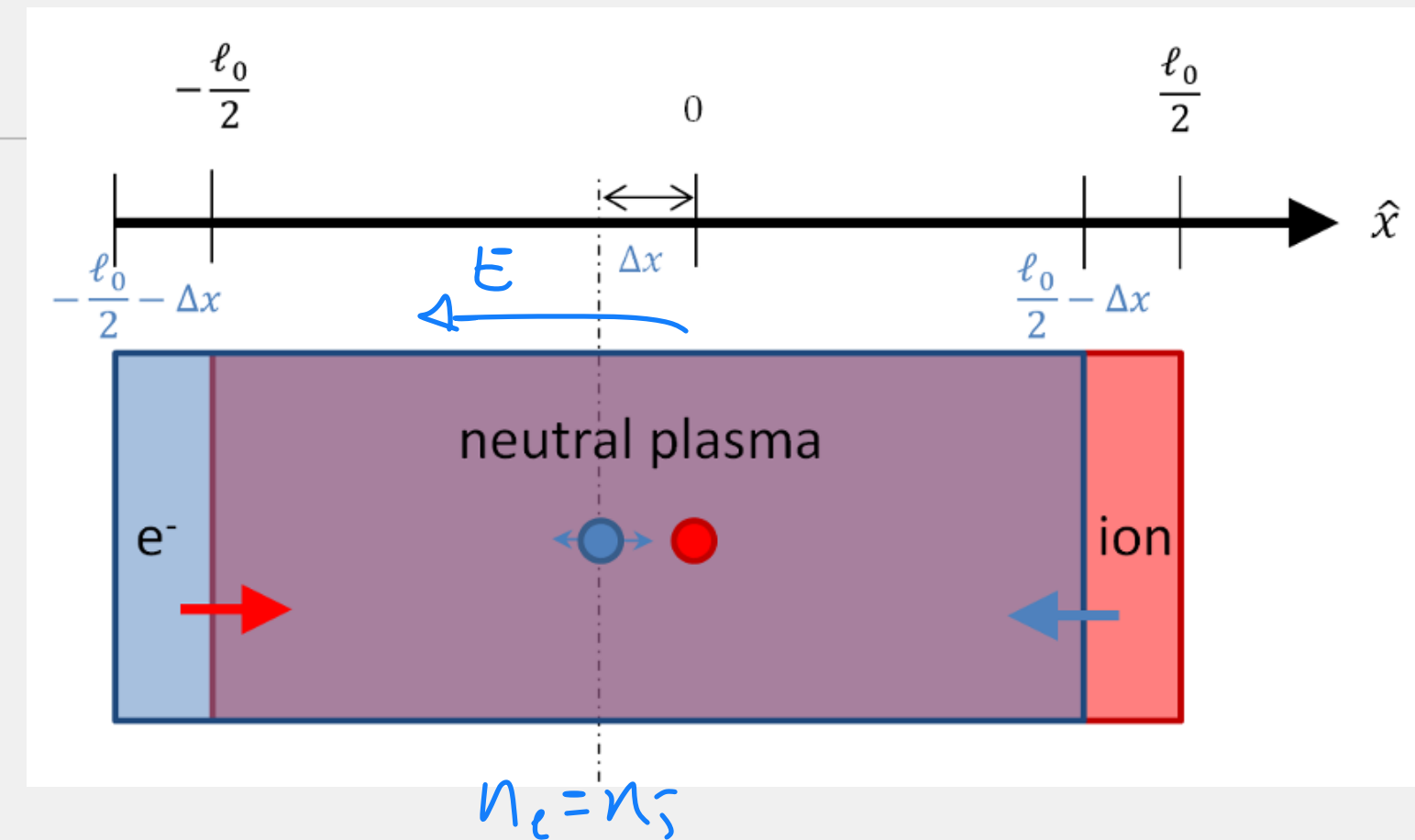
$$V_p \rightarrow \infty$$

$$\omega = 2\pi f = \text{radio wave freq}$$

$$\text{if } \omega < \omega_p$$

$$n = \text{complex}$$

$$n = \alpha + j\beta$$

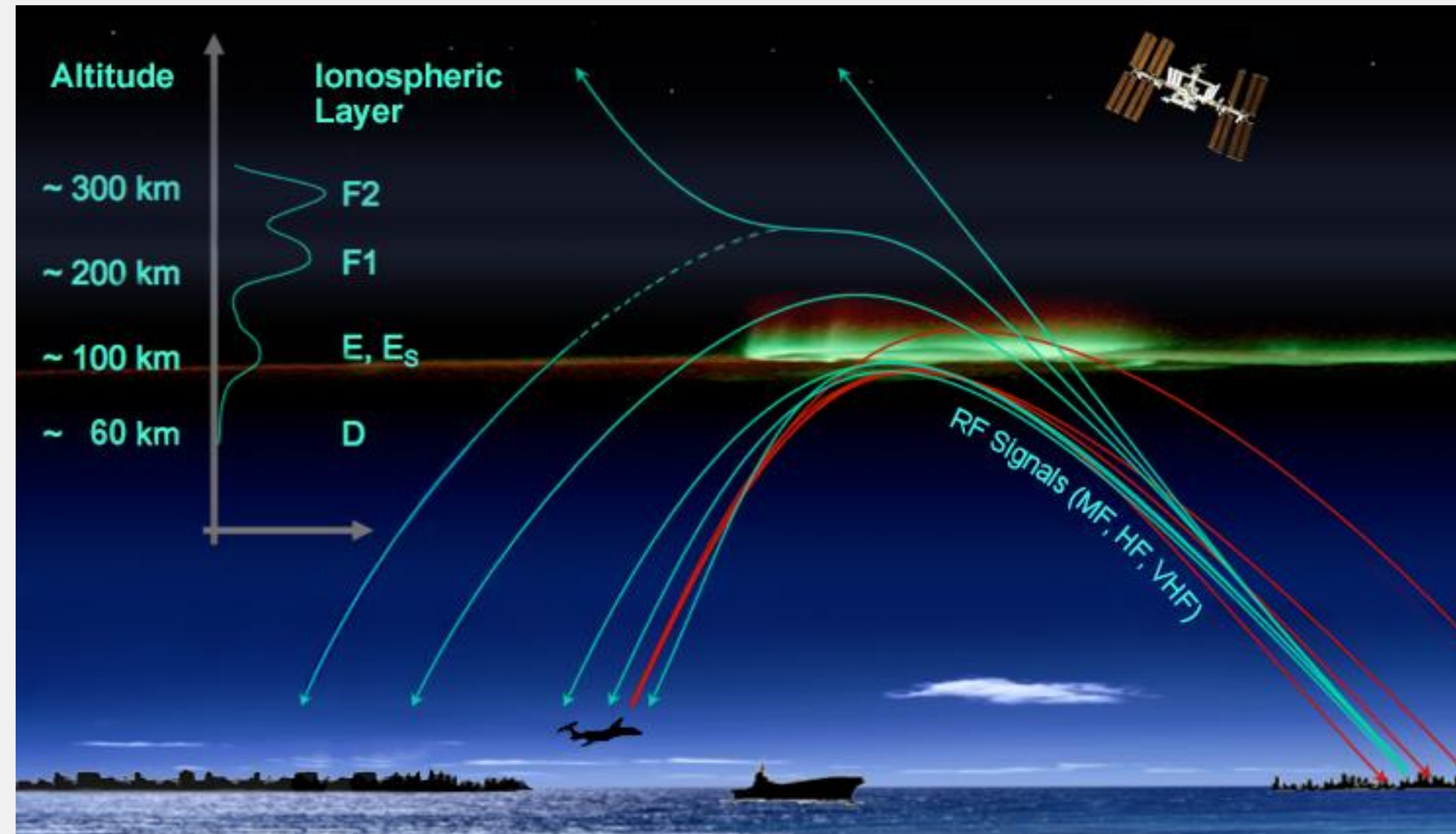


# Reflection of EM Waves

- ❖ Plasma frequency  $\omega_p$  directly related to electron density
- ❖ Radio waves above  $\omega_p$  pass through the ionosphere; electrons cannot respond fast enough
- ❖ Radio waves below  $\omega_p$  are reflected; electrons are “shaken” and re-radiate

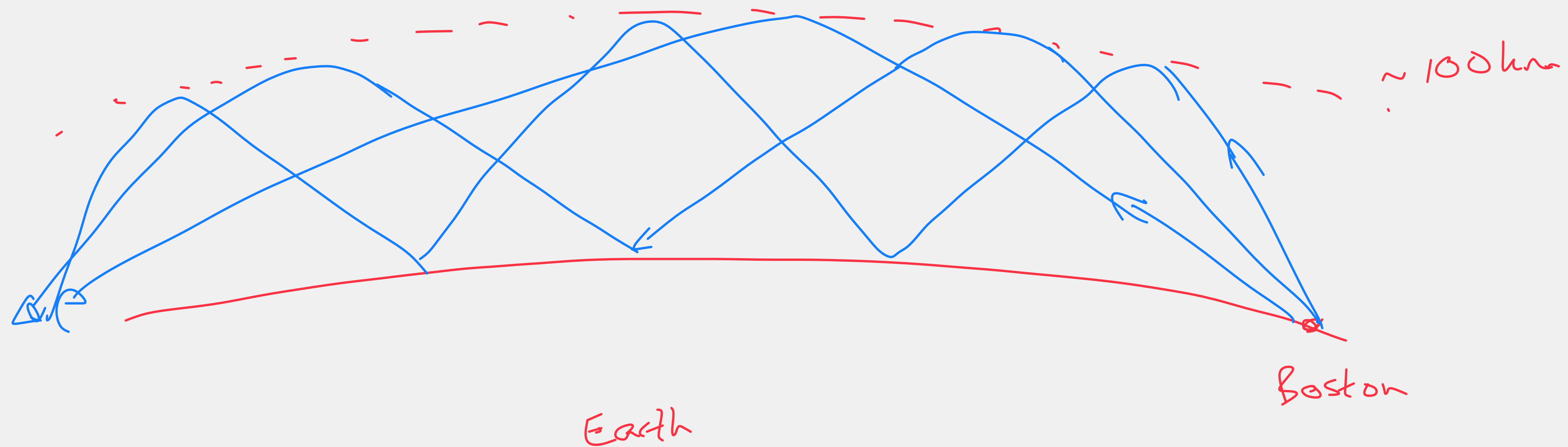
- ❖ **Implications:**

- ❖ must use frequencies above  $\omega_p$  to talk to satellites
- ❖ Can communicate over-the-horizon with frequency near / below  $\omega_p$



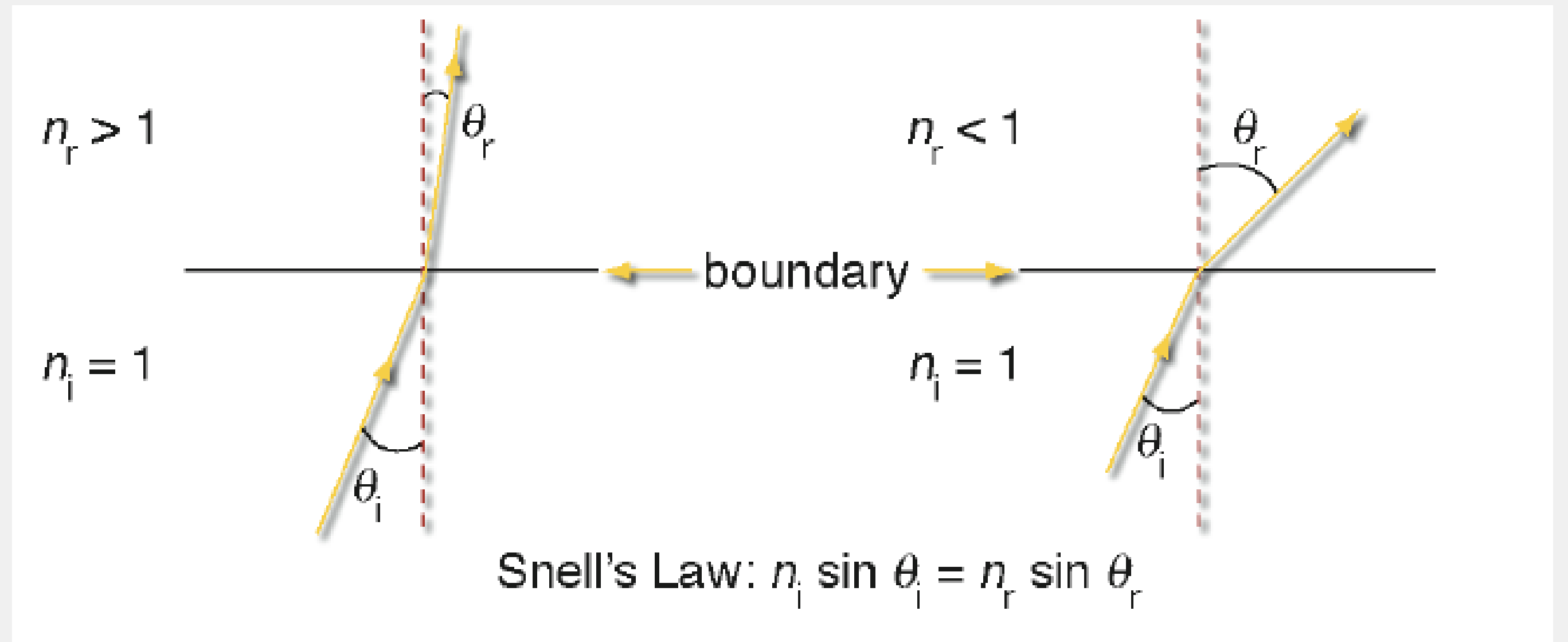


# Over-the-horizon radar or communication



# Index of Refraction

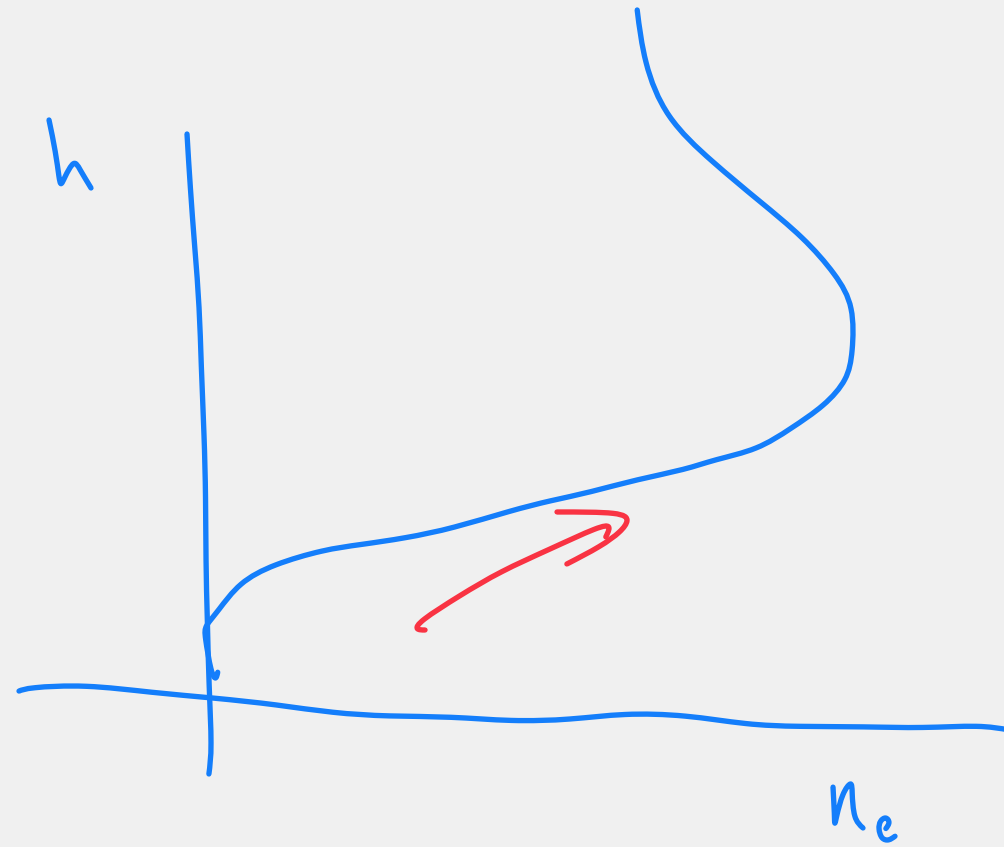
- ❖ As a radio wave propagates from one medium to another, its propagation direction is **refracted**, based on the **indices of refraction**,  $n_1$  and  $n_2$ .



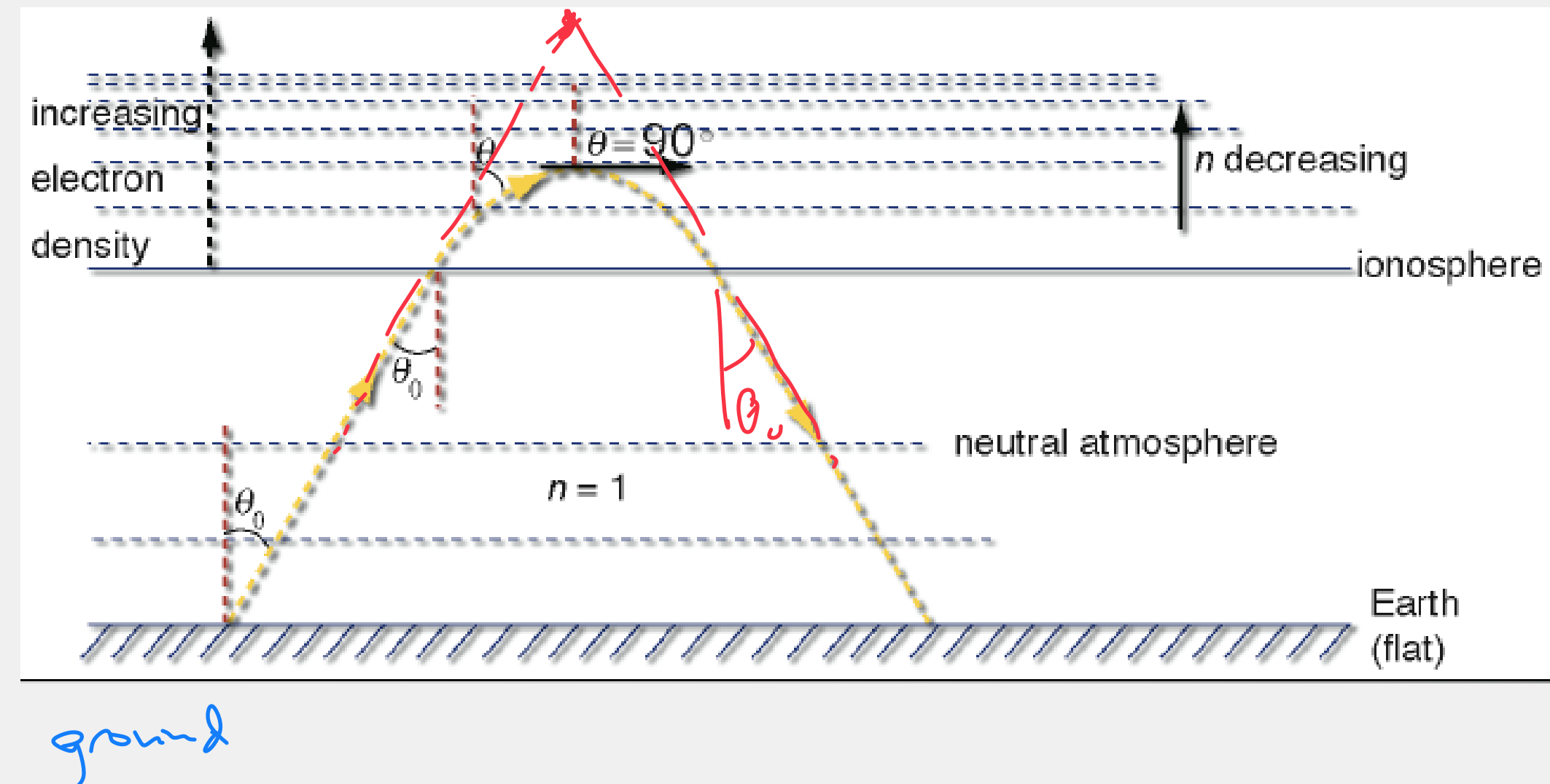
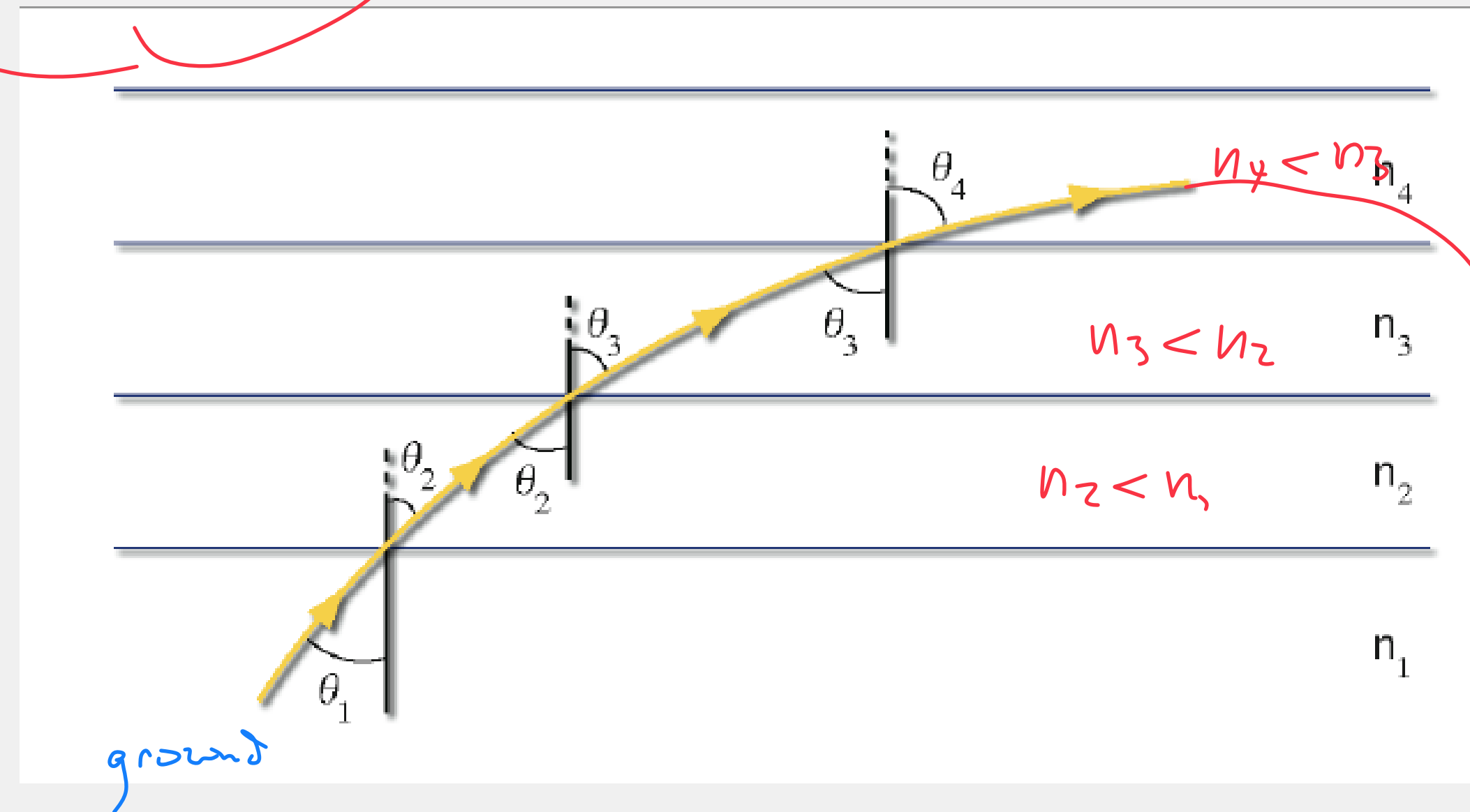


# Ionospheric Refraction

$$n^2 = 1 - \frac{\omega_p^2}{\omega^2} = 0$$



- ❖ We can treat the ionosphere as successive layers, and look at refraction from one layer to the next
- ❖ Continuous refraction
- ❖ End result: ray “bends” and turns back to the ground. Not a hard reflection!



# Critical Frequencies in the Ionosphere

- ❖ In the F-region,  $f_c \sim 3\text{--}30$  MHz

- ❖ higher frequencies pass through the ionosphere, with some refraction
- ❖ over-the-horizon radio

- ❖ In the E-region,  $f_c \sim 1\text{--}2$  MHz

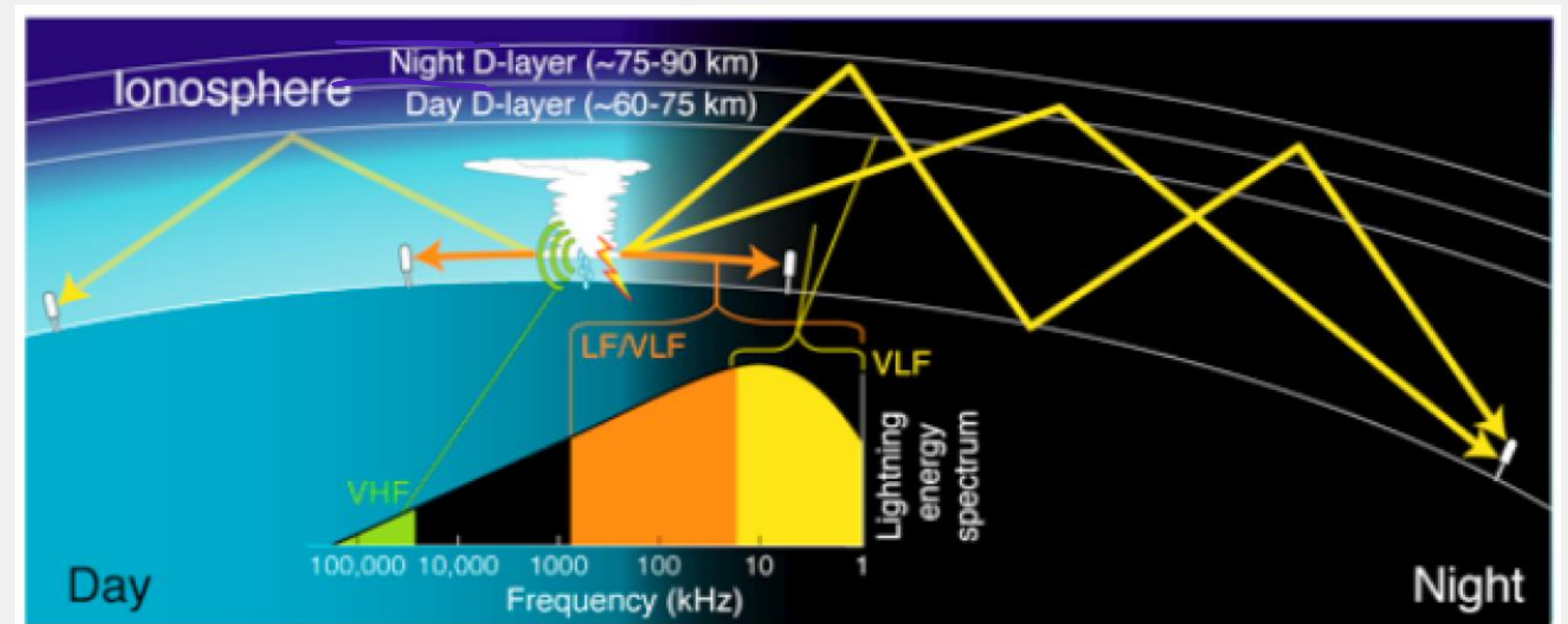
- ❖ but sporadic-E increases  $f_c$  up to 100 MHz

- ❖ In the D-region, our model breaks.

- ❖ Lots of neutrals means high collision frequency; our index of refraction is more complicated.  $e-\nu$
- ❖ Absorption of MHz waves (next)
- ❖ Reflection of waves below  $\sim 100$  kHz; VLF waves (below  $\sim 50$  kHz) used for long-range communications with submarines

$$\omega_p = \sqrt{\frac{q_e^2 n_e}{m_e \epsilon_0}}, \quad f_p = \frac{\omega_p}{2\pi} \sim n_{e, \text{max}}$$

$$X \quad n^2 = 1 - \frac{\omega_p^2}{\omega^2} \approx 0$$





# Waves in Plasmas

- ❖ We need three equations to describe wave propagation in a cold plasma.  
Ampere's Law and Faraday's Law (i.e. Maxwell's equations):

$$\begin{aligned} \nabla \times \bar{B} &= \mu_0 \bar{J} + \mu_0 \epsilon_0 \frac{d\bar{E}}{dt} \quad \rightarrow \quad \frac{d}{dt} \rightarrow j\omega = i\omega \\ \nabla \times \bar{E} &= -\frac{d\bar{B}}{dt} \quad \rightarrow \quad \nabla \times \rightarrow j\bar{k} \times \end{aligned}$$

$E(t) = A e^{j(\omega t - kx)}$   
 $k = \frac{2\pi}{\lambda}$

- ❖ And the Langevin equation (simply  $F = ma$ ):

$$m_e \frac{dv_e}{dt} = \sum F = q_e \bar{E} + q_e (\bar{v}_e \times \bar{B}) - \underbrace{\nu m_e \bar{v}_e}_{\text{"ny"}} + \dots$$

$$\bar{J}_e = q_e n_e \bar{v}_e$$

$$n = \frac{kc}{\omega}$$

$$\frac{d\bar{J}_e}{dt} = \frac{q_e n_e}{m_e} (\bar{E} + \bar{v} \times \bar{B}_0) - q n_e \nu \bar{J}$$

# Index of refraction in a cold plasma

- ❖ In general, index of refraction is given by the Appleton-Hartree equation:

$$n^2 = 1 - \frac{X}{1 - \textcircled{iZ} - \frac{\frac{1}{2}Y^2 \sin^2 \theta}{1 - X - \textcircled{iZ}} \pm \frac{1}{1 - X - \textcircled{iZ}} \left( \frac{1}{4}Y^4 \sin^4 \theta + Y^2 \cos^2 \theta (1 - X - \textcircled{iZ})^2 \right)^{1/2}}$$

↑  
angle between  $\vec{B}_0$  and  $\vec{k}$

$$X = \frac{\omega_p^2}{\omega^2} = \frac{q_e^2 n_e}{m_e \epsilon_0 \omega^2}$$

$$Y = \frac{\omega_c}{\omega} \xrightarrow{\text{gyrofrequency}} = \frac{q_e B_0}{m_e \omega}$$

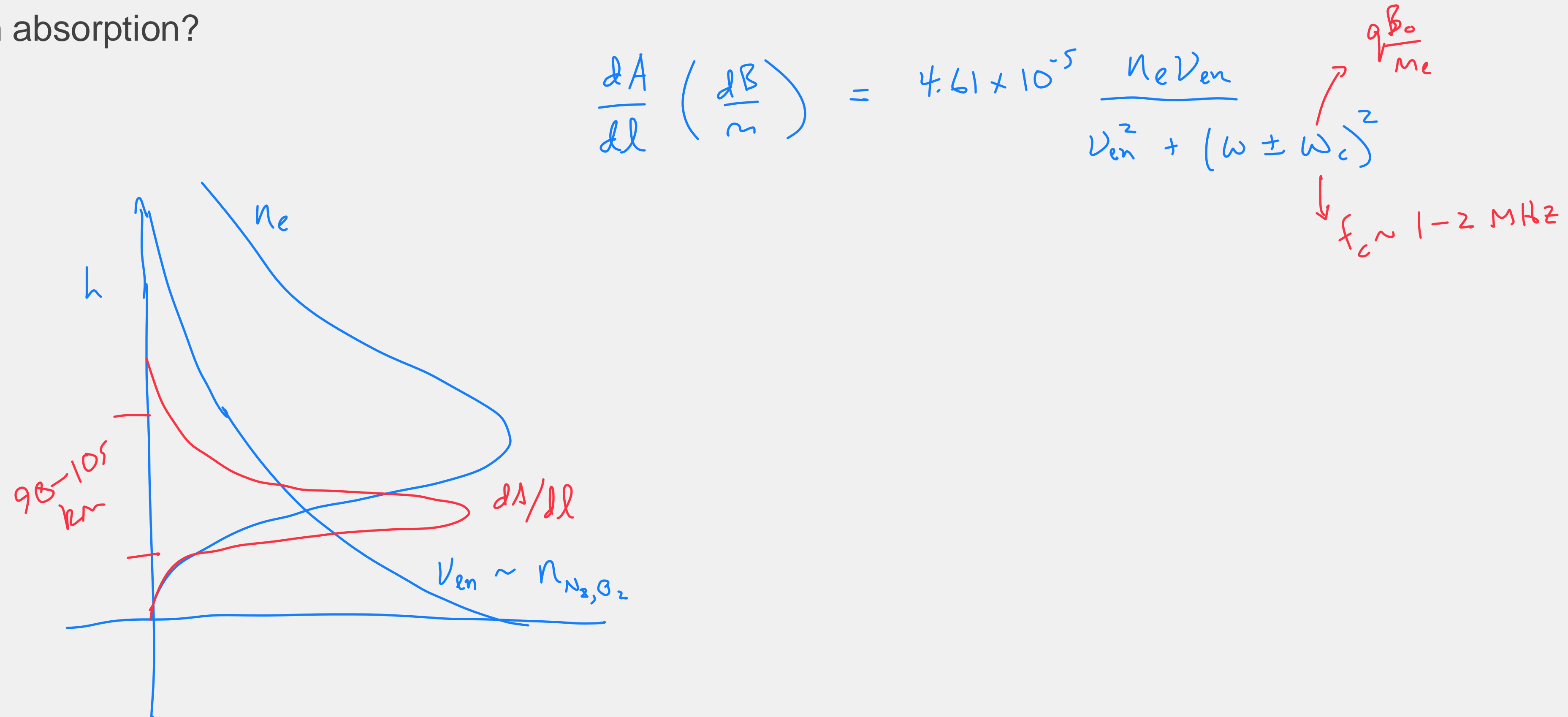
$$Z = \frac{\nu}{\omega}, \quad \nu = \text{coll. freq.} \quad : \quad \text{collisions make } n \text{ complex.}$$

$$n = \alpha + j\beta$$



# D-region absorption

- ❖ As electrons get excited by waves with  $f < f_c$ , they collide with neutrals
- ❖ Some of the EM wave energy gets transferred to heat; radio waves suffer absorption
- ❖ How much absorption?



# Collision Frequency?

- ❖ Electrons (few) randomly collide with neutrals (many)
- ❖ Radio wave energy converts to electron kinetic energy and then to neutral thermal energy (i.e., neutrals are “heated”)
- ❖ This is collisional heating, and a sink for radio wave energy

- ❖ Collision frequency depends on neutral density ( $N_2$ ,  $O_2$ ) and on electron temperature
- ❖ Does not depend on electron density; **why?**

$$\nu_{av}(e, N_2) = 2.33 \times 10^{-17} \underline{N_{N_2}} (1 - \overbrace{1.21 \times 10^{-4} T_e}^{\text{small}}) \overbrace{T_e}^{\sim T_e}$$

$$\nu_{av}(e, O_2) = 1.82 \times 10^{-16} \underline{N_{O_2}} (1 + \overbrace{0.036 T_e^{1/2}}^{\sim T_e}) T_e^{1/2}$$

$$\underline{\nu_{en} = \nu_{av}(e, N_2) + \nu_{av}(e, O_2)} \quad , \quad \text{1/sec}$$

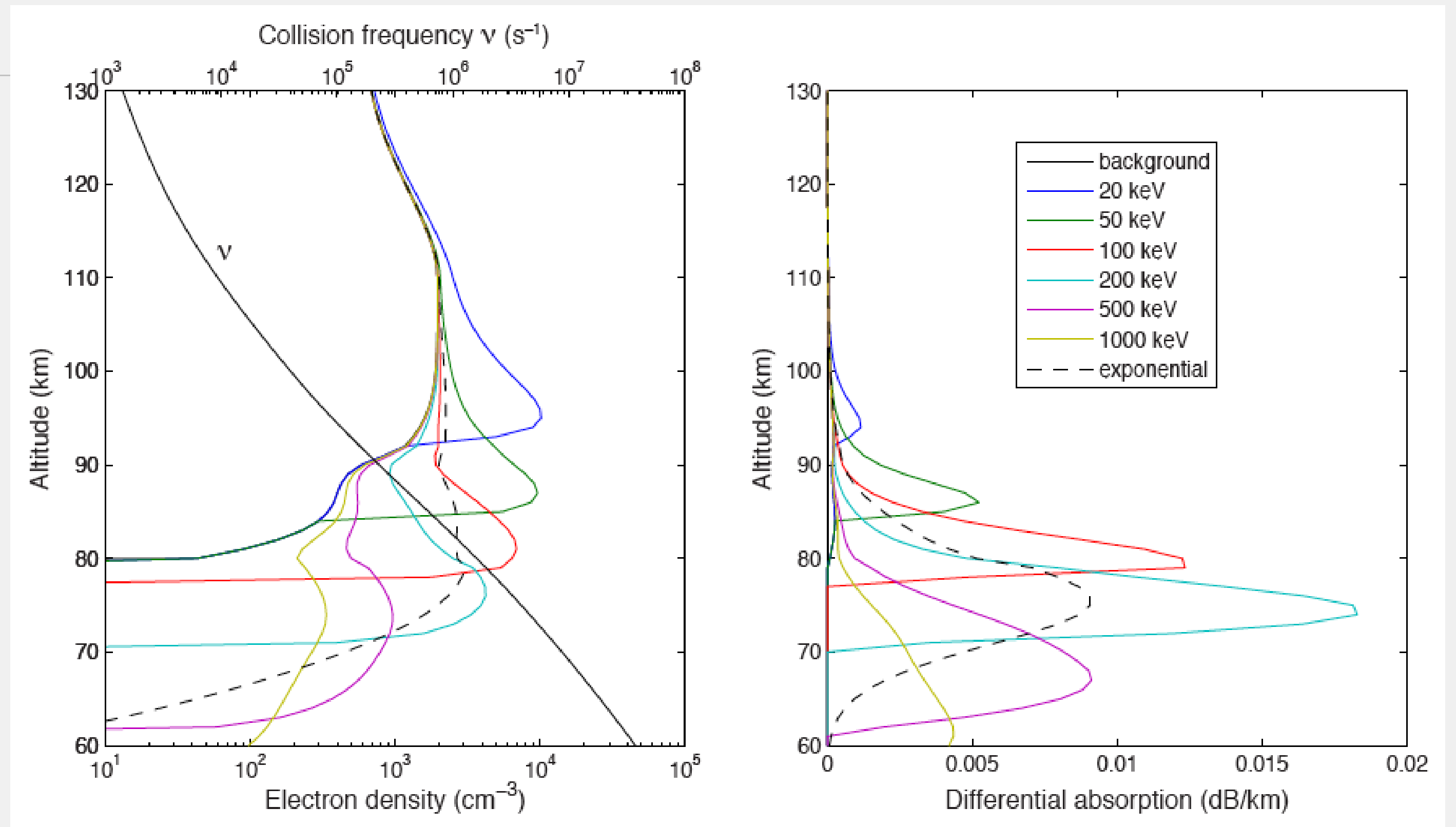
per electron



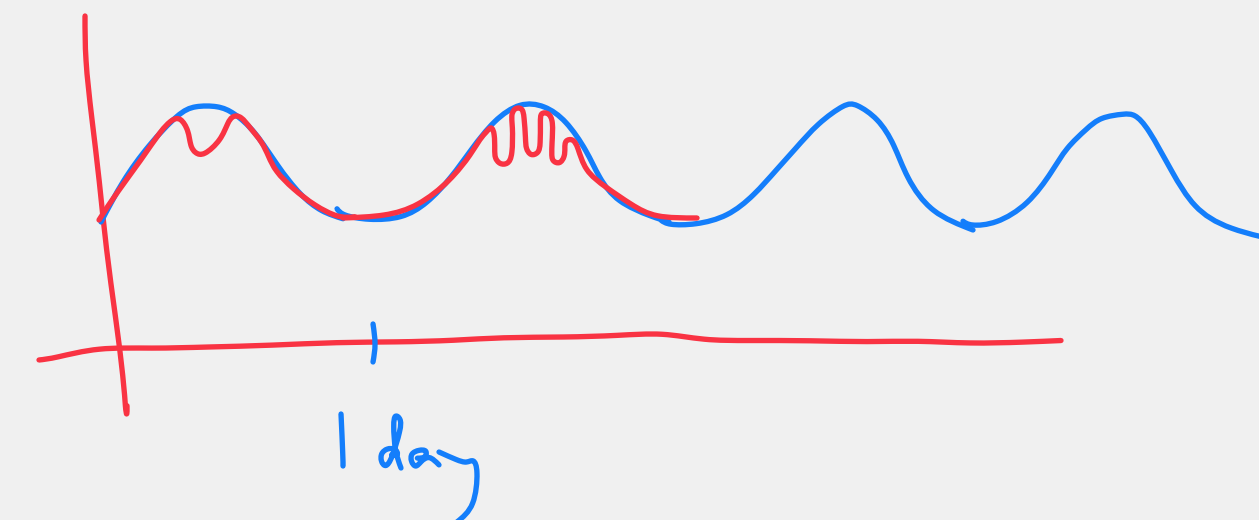
# D-region absorption

- ❖ Shown here: absorption of 30 MHz radio wave due to electron precipitation from the radiation belts

Alaska

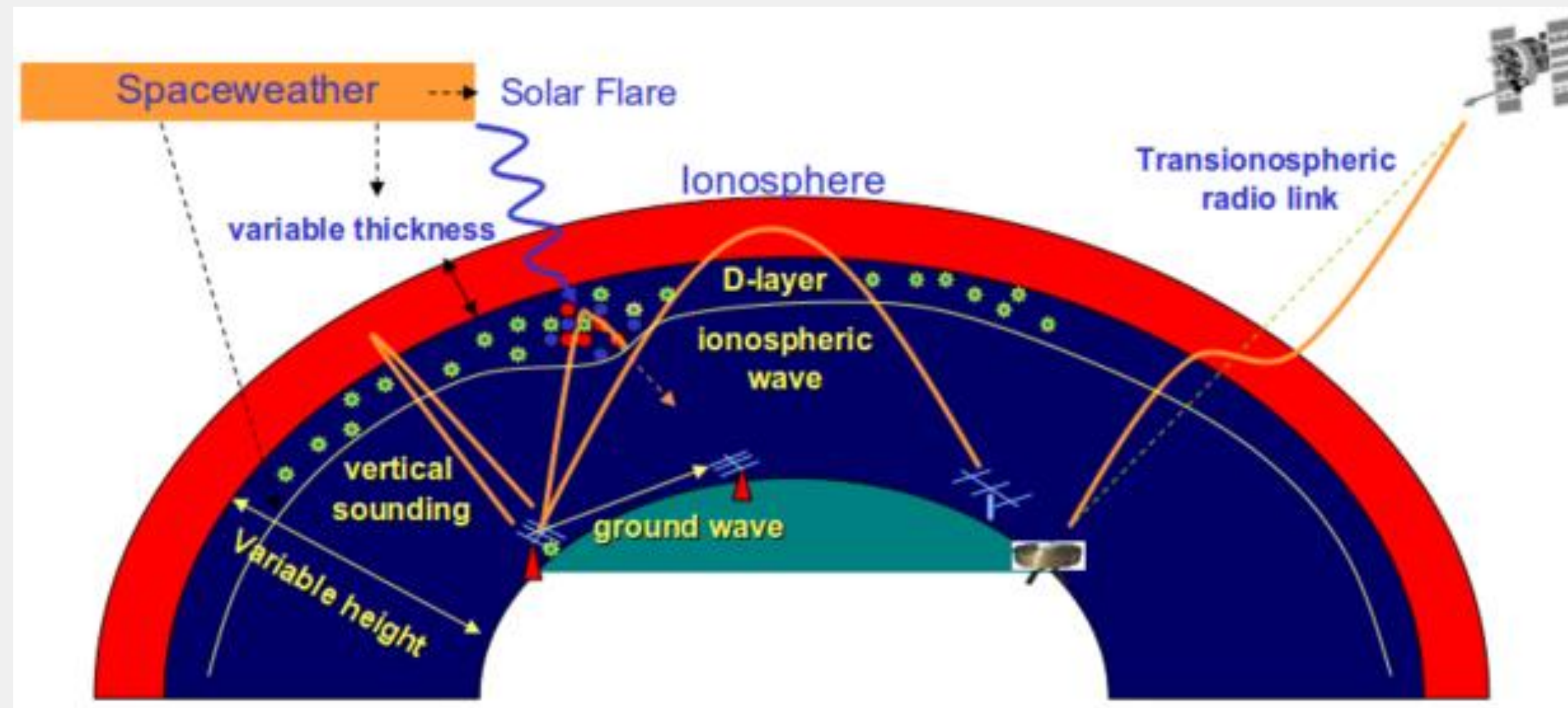


- ❖ **Riometer**: passive instrument that measures D-region absorption by monitoring cosmic noise at  $\sim 30$  MHz



# Sudden Ionospheric Disturbances (SIDs)

- ❖ SID is ionospheric response to a solar flare (X-rays)
  - ❖ X-rays ionize the D-region, causing a huge increase in D-region electron density (orders of magnitude)
  - ❖ Higher  $n_e$  leads to higher radio wave absorption
  - ❖ Lower D-region reflection height perturbs VLF signals





# Short-Wave Fade

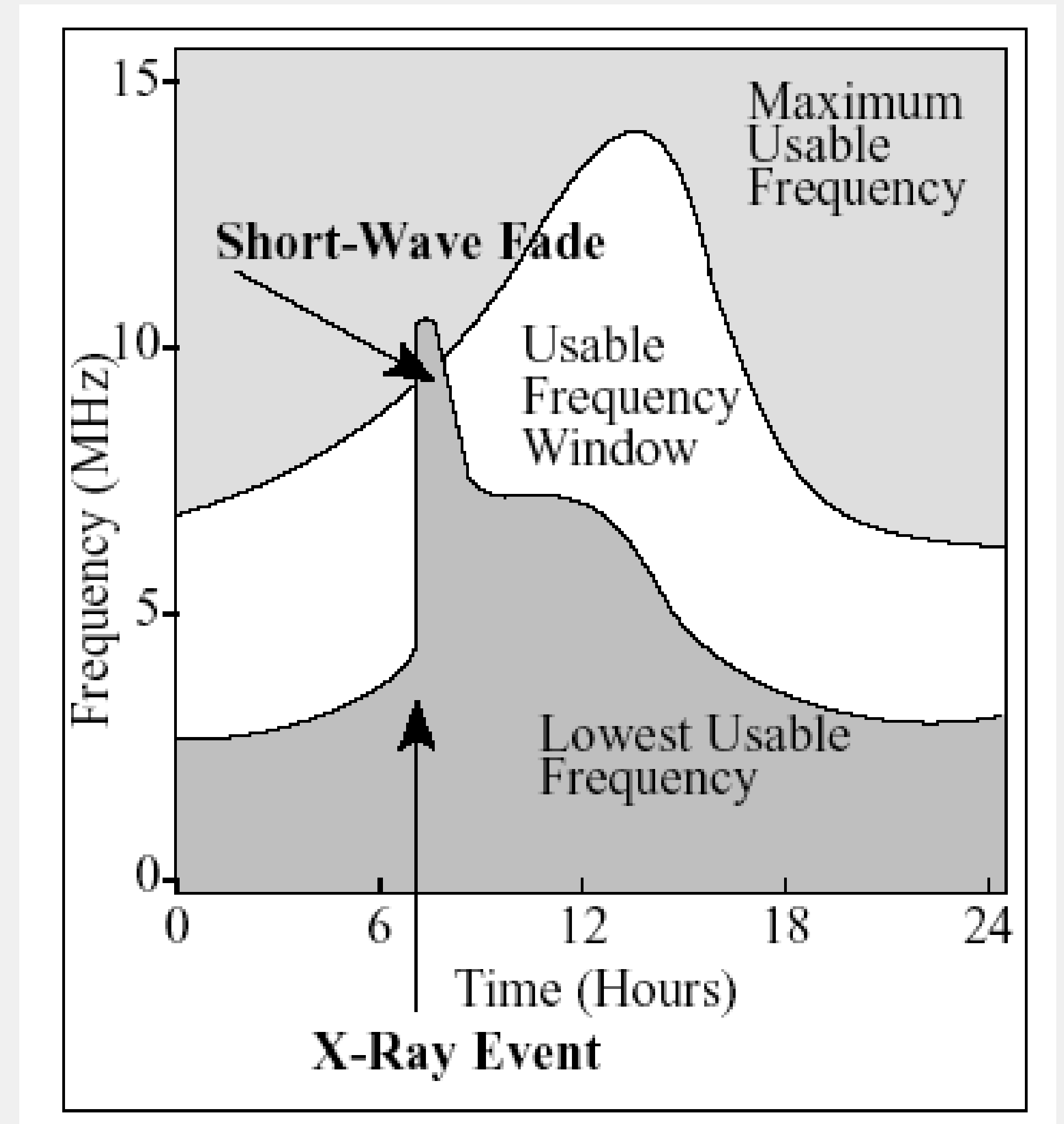
## ❖ Issue for over-the-horizon radar

- ❖ There is a maximum frequency we can use, above which waves pass through the F-region
- ❖ There is a minimum frequency we can use, because

- ❖ lower frequencies suffer too much absorption

$$\frac{dA}{dl} = 4.6 \times 10^{-5} \frac{n_e \nu}{\omega^2}$$

- ❖ Usable “Frequency Window”
- ❖ After a major X-ray flare, Absorption can increase to prevent any useful communication



# GPS and TEC

$$f \sim 1-1.5 \text{ GHz}, \quad f \gg f_p, f_c$$

- ❖ Even for frequencies above  $f_c$ , the ionosphere introduces some interesting effects

- ❖ Small change in index of refraction from

$$n^2 = 1 - \frac{\omega_p^2}{\omega^2}$$

- ❖ Expand in Taylor series:

$$n = 1 + \frac{c_2}{f^2} + \frac{c_3}{f^3} + \frac{c_4}{f^4} + \dots$$

- ❖ Cut off after first term:

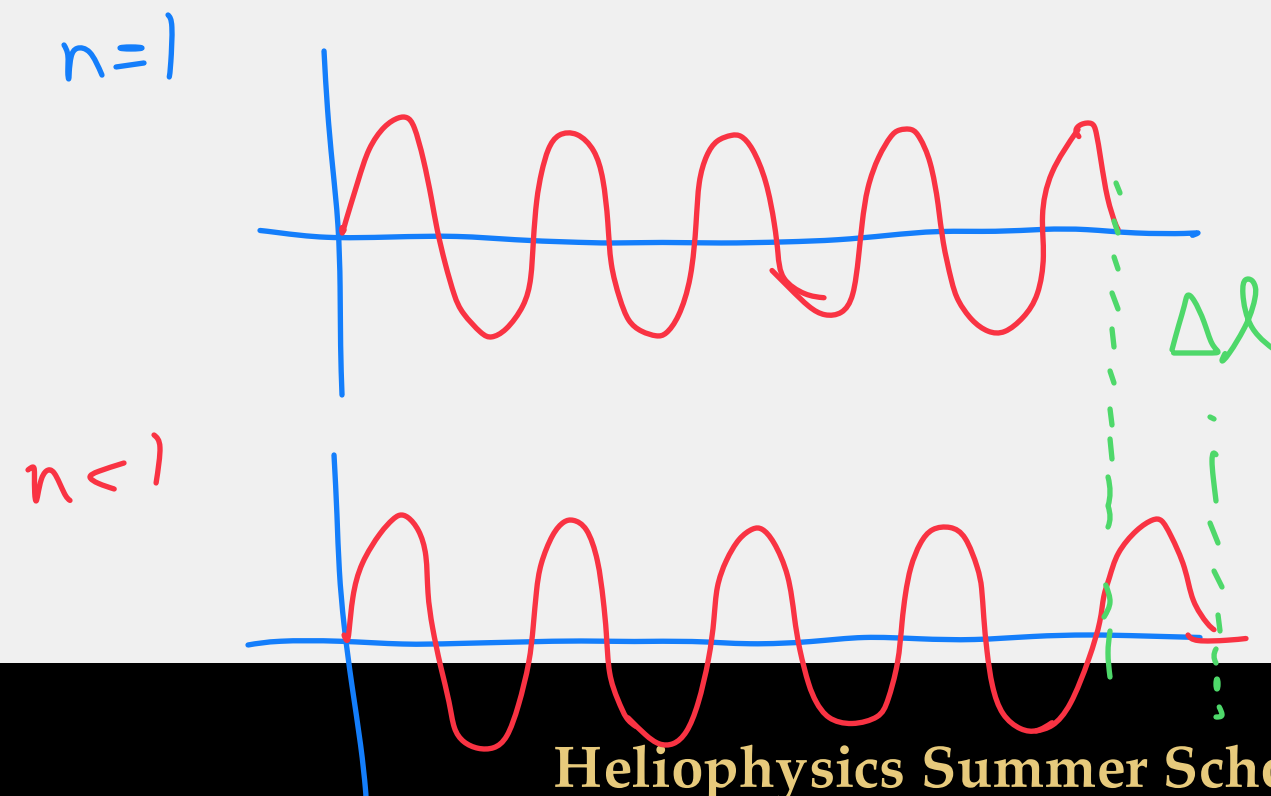
$$n = 1 + \frac{c_2}{f^2}$$

- ❖ Change in path length:

$$\Delta l_{\text{iono}} = -\frac{40.3}{f^2} \text{TEC}$$

$$\text{TEC} = \int_{-\infty}^{\infty} n_e(l) dl \quad (m^{-2})$$

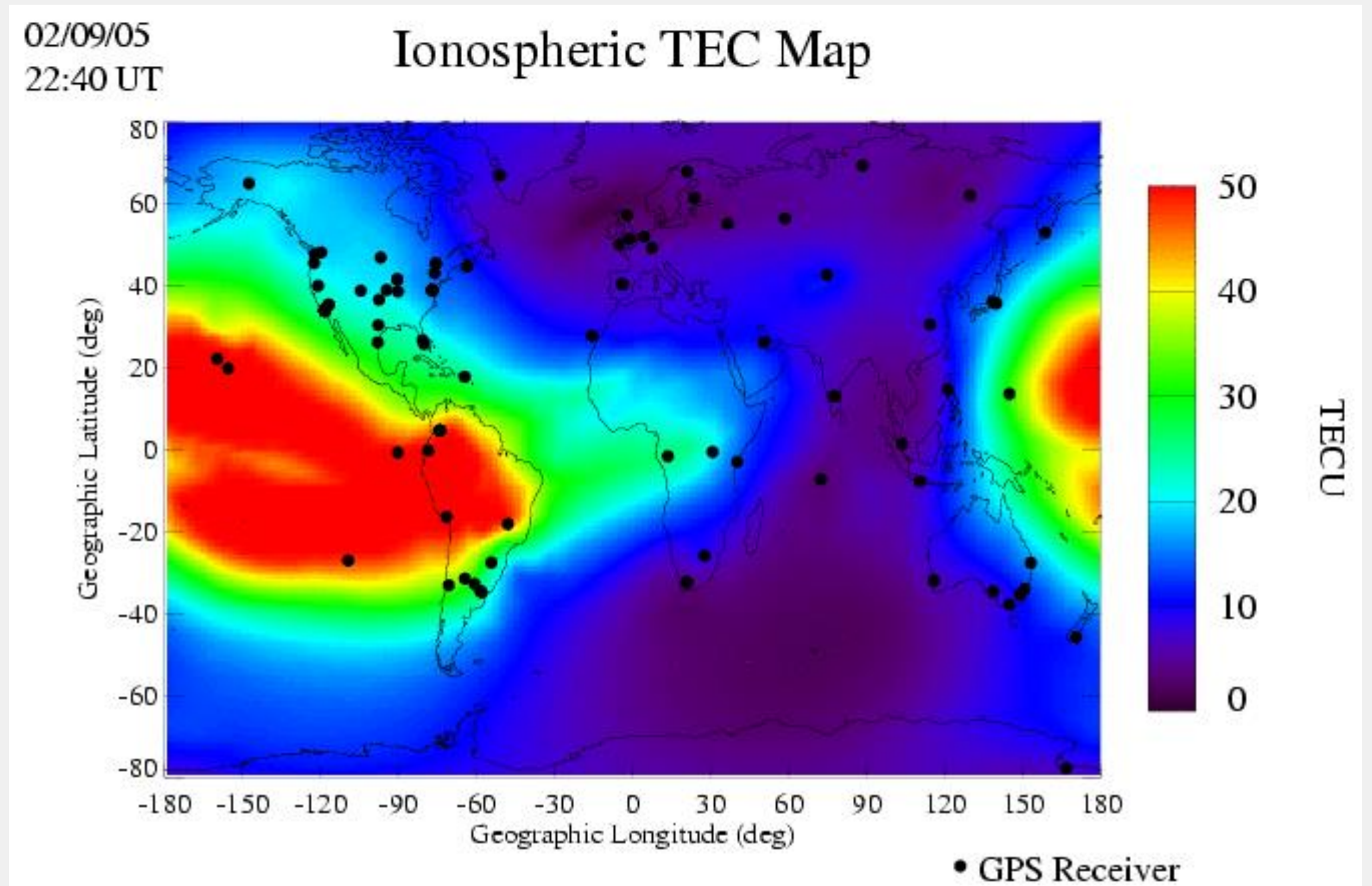
- ❖ Where TEC is total electron content, integrated along signal path





# TEC maps

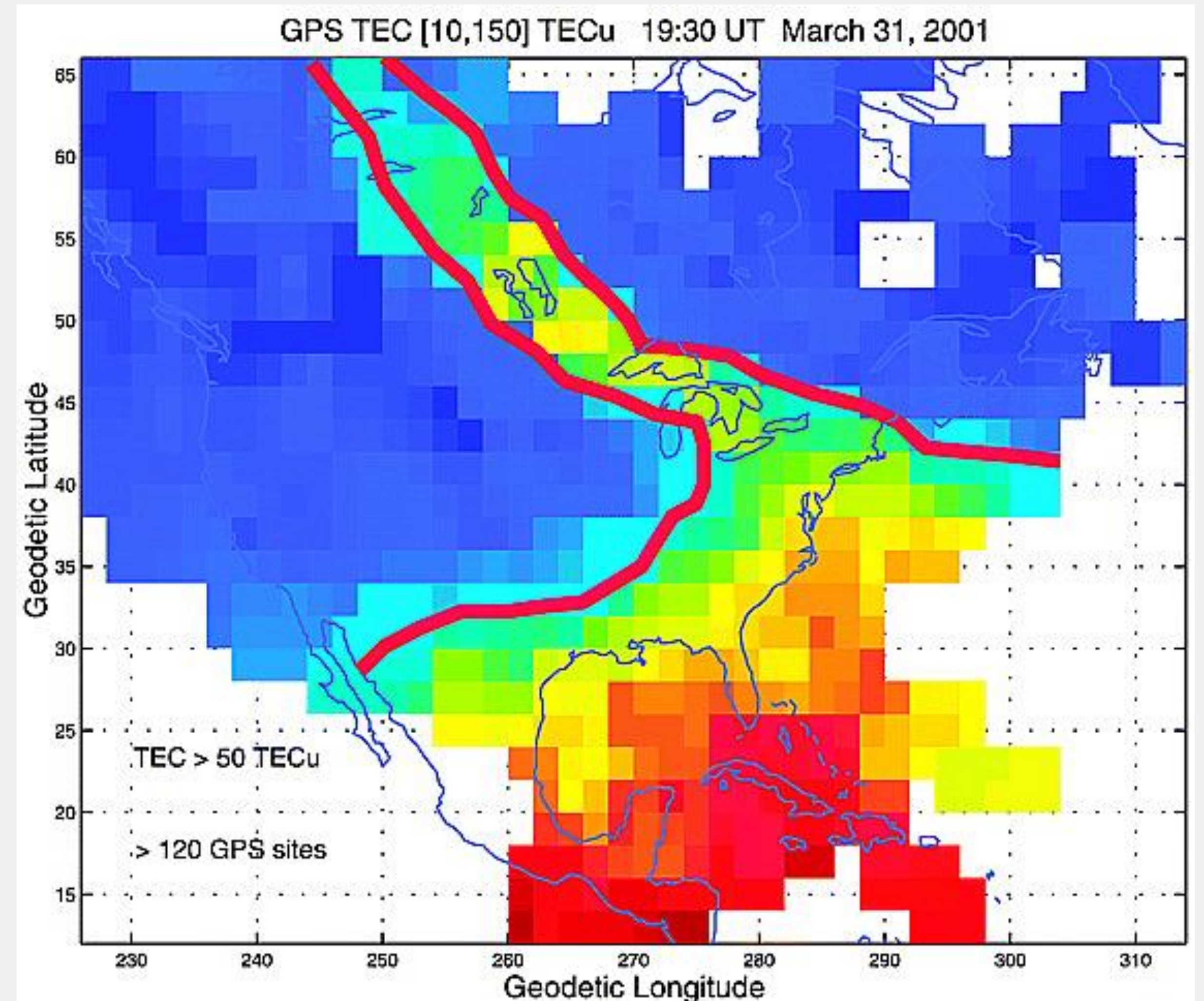
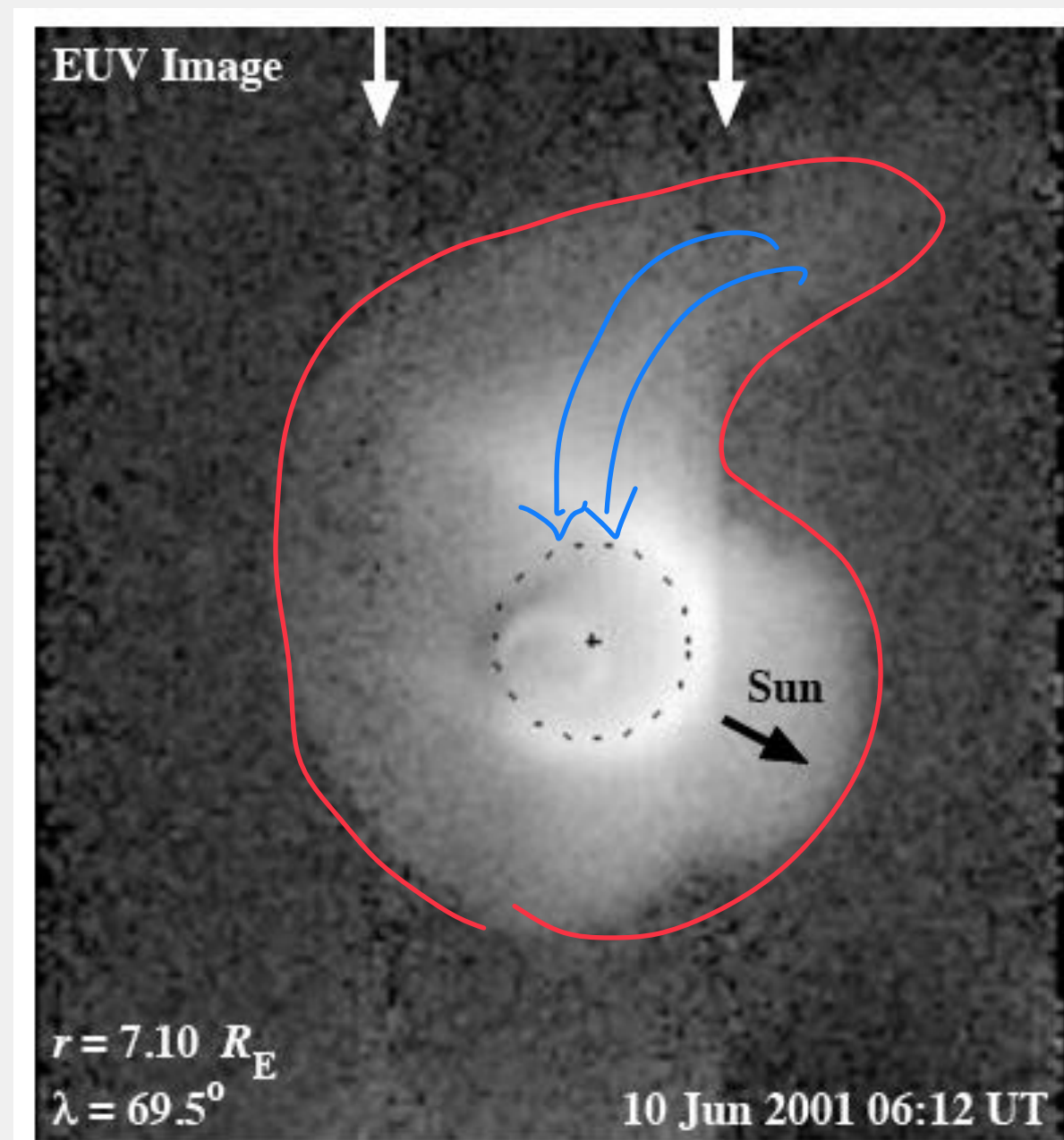
- ❖  $1 \text{ TECU} = 10^{16} \text{ el/m}^2$
- ❖ receivers all over the Earth's surface;  
20+ satellites to provide pierce-points
- ❖ Interpolate results onto 2D (or 3D) map





# GPS TEC and ionospheric science

- ❖ GPS TEC can be used to observe ionospheric disturbances
- ❖ “Plume” here, extending over North America, is footprint of plasmasphere “plume” during geomagnetic storm





# Ionosphere Missions

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- ❖ **ICON**

- ❖ Using airglow to infer ion densities and winds

- ❖ **Ampere**

- ❖ Using magnetic fields to measure currents

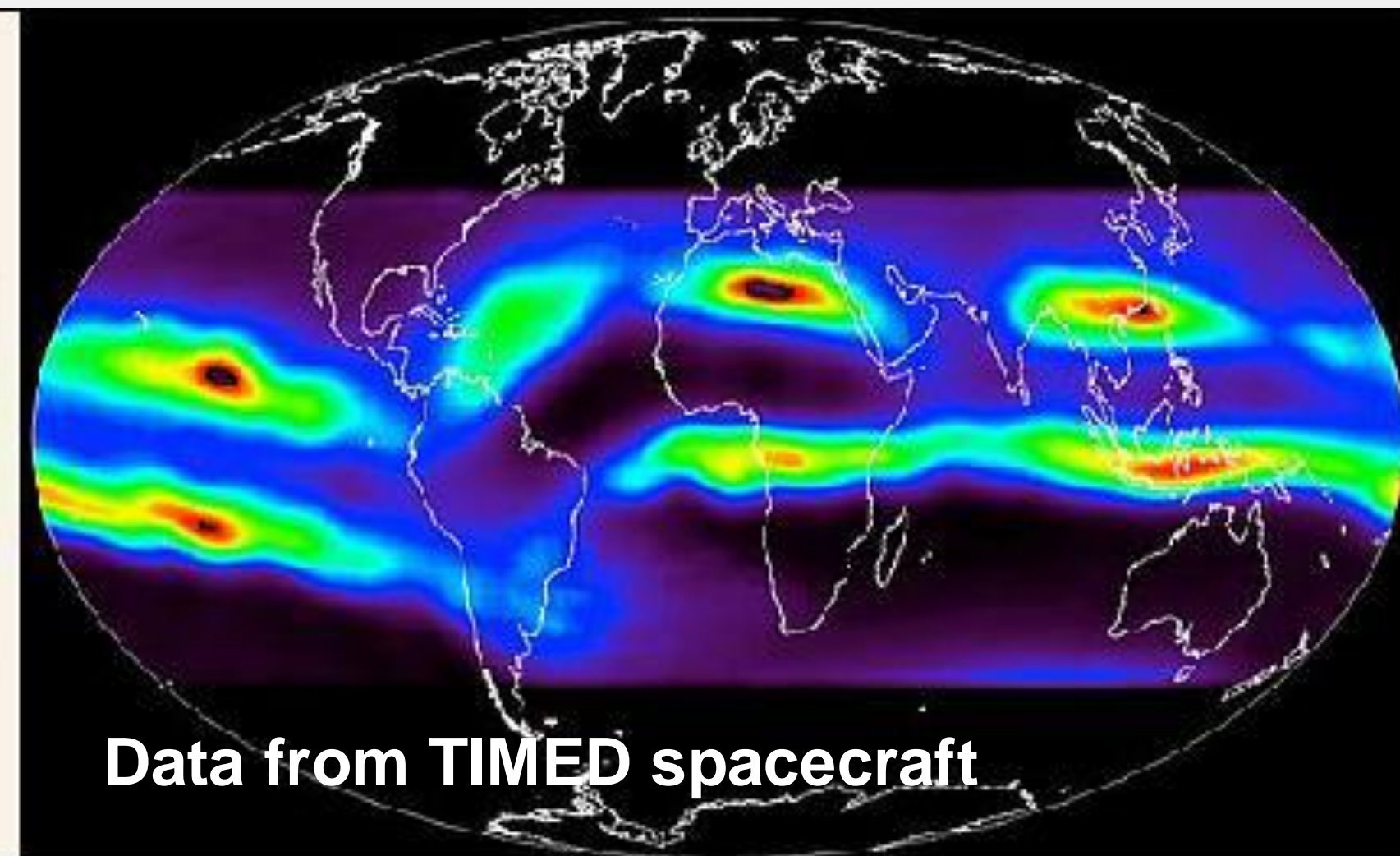
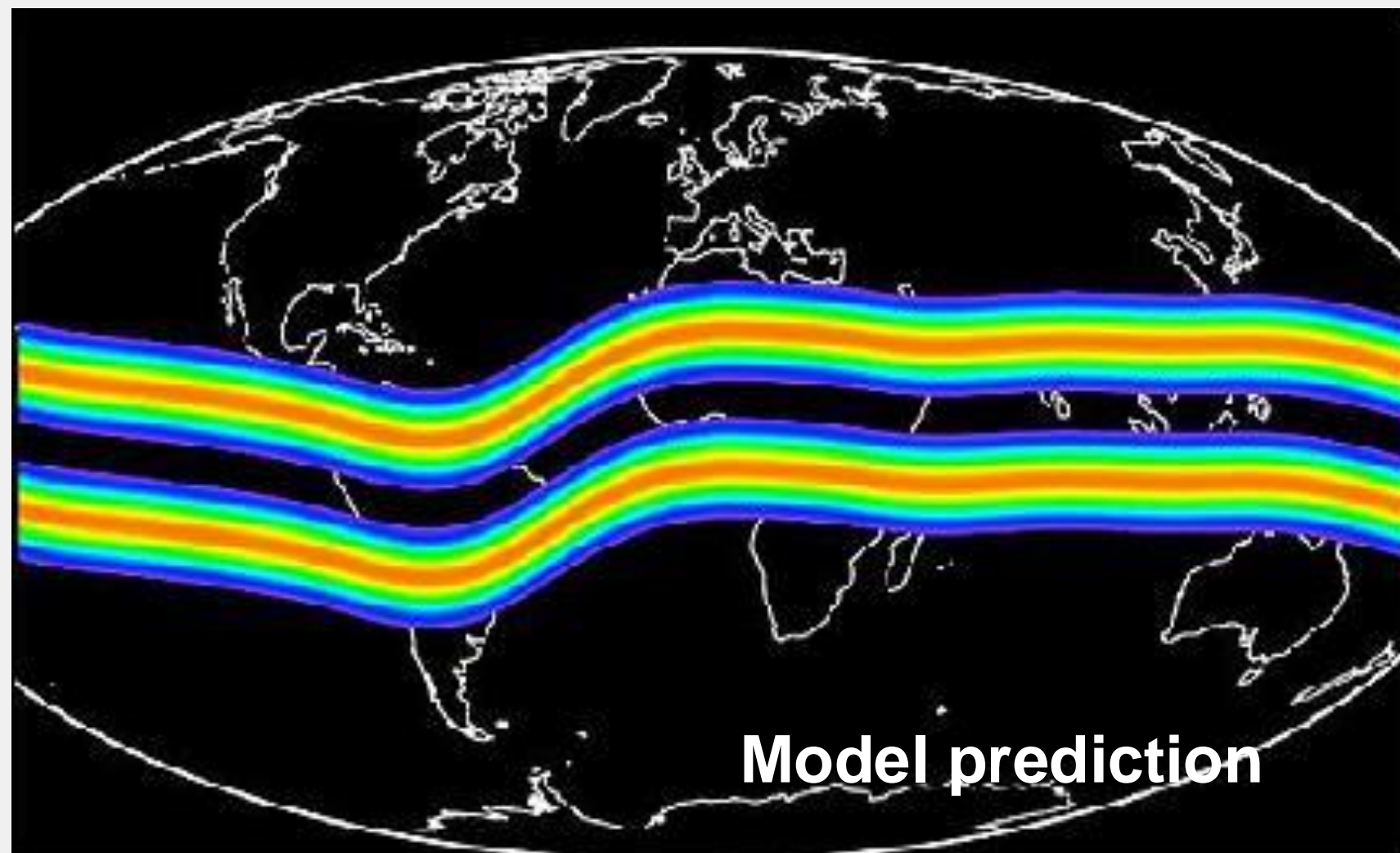
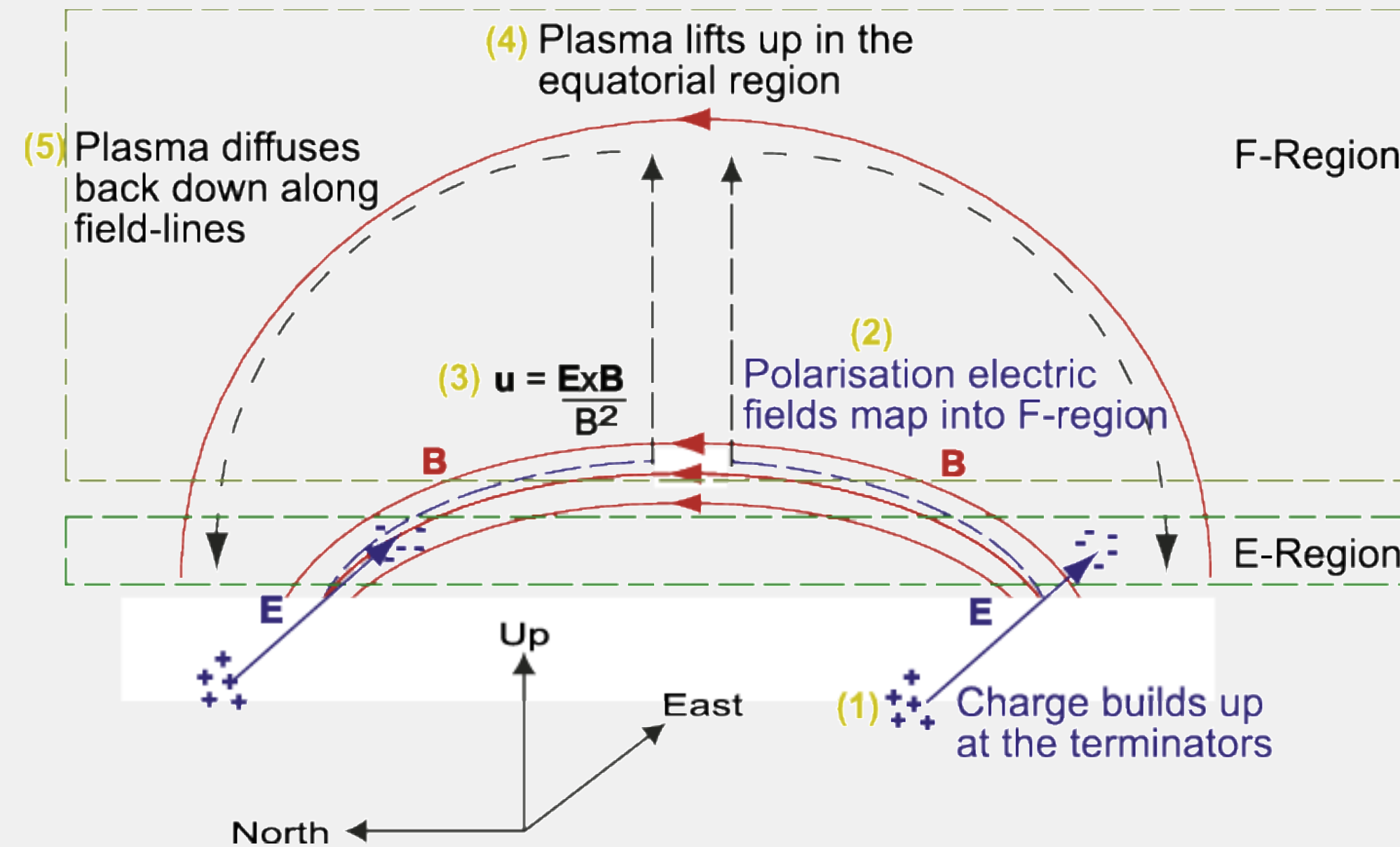
- ❖ **COSMIC** and **GPS**

- ❖ Measuring the ionosphere using radio occultation / path delay

- ❖ *Hidden Figures* and *Apollo 13*: Re-entry comm problem

# The Equatorial Ionosphere

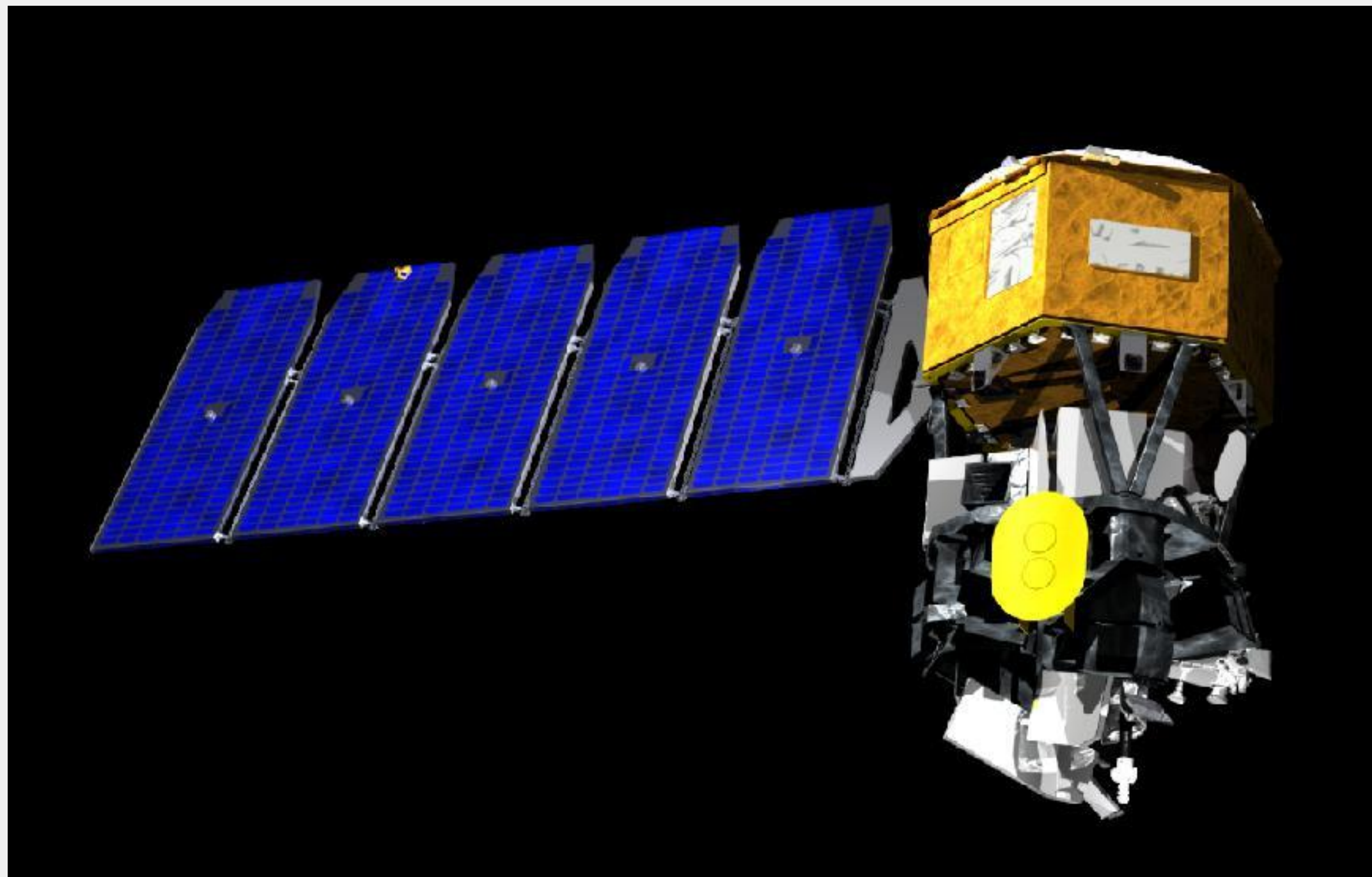
- ❖ The Fountain effect predicts two bands of enhanced electron density above and below the magnetic equator
- ❖ The truth? A bit more complicated....





# ICON Science and Spacecraft

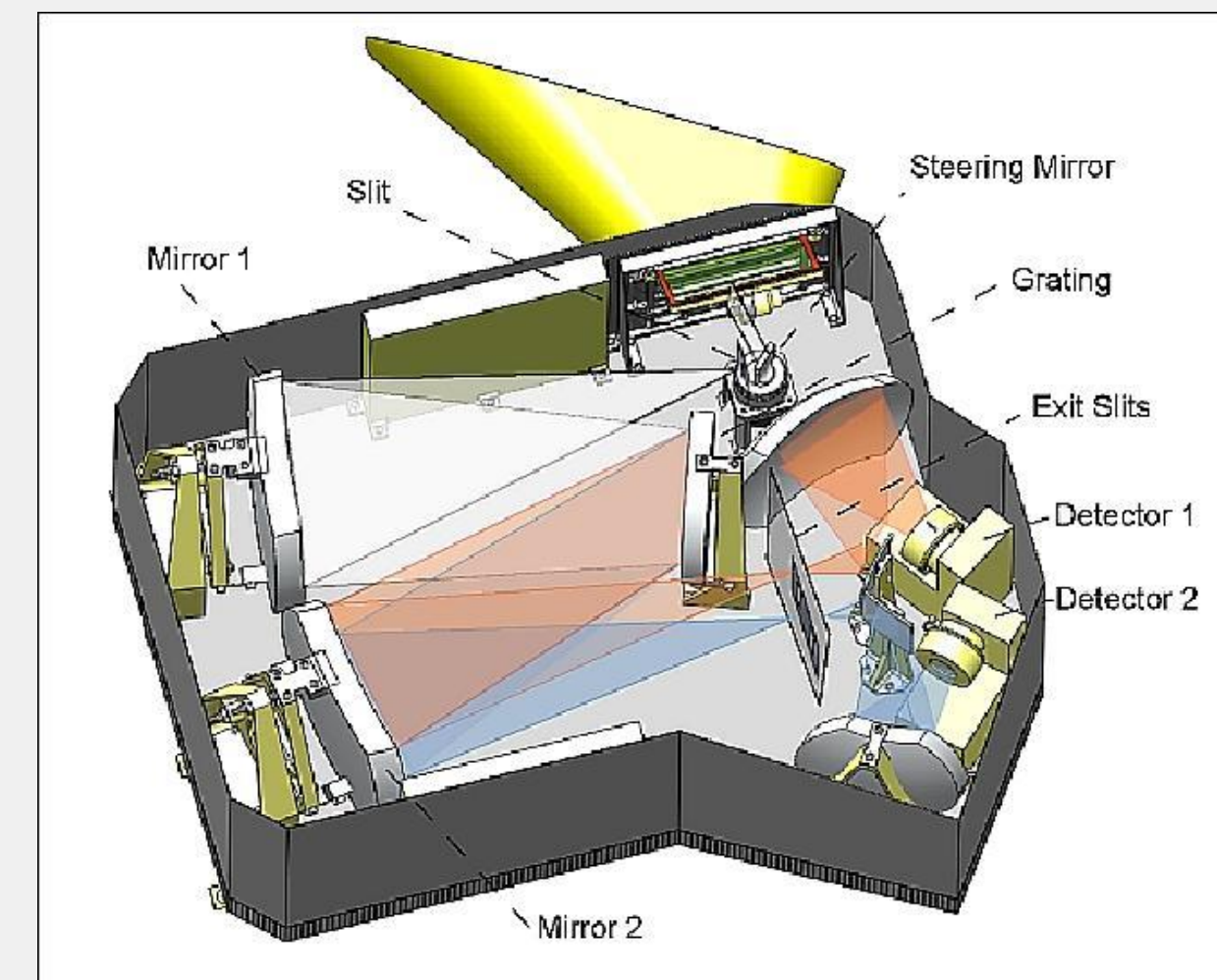
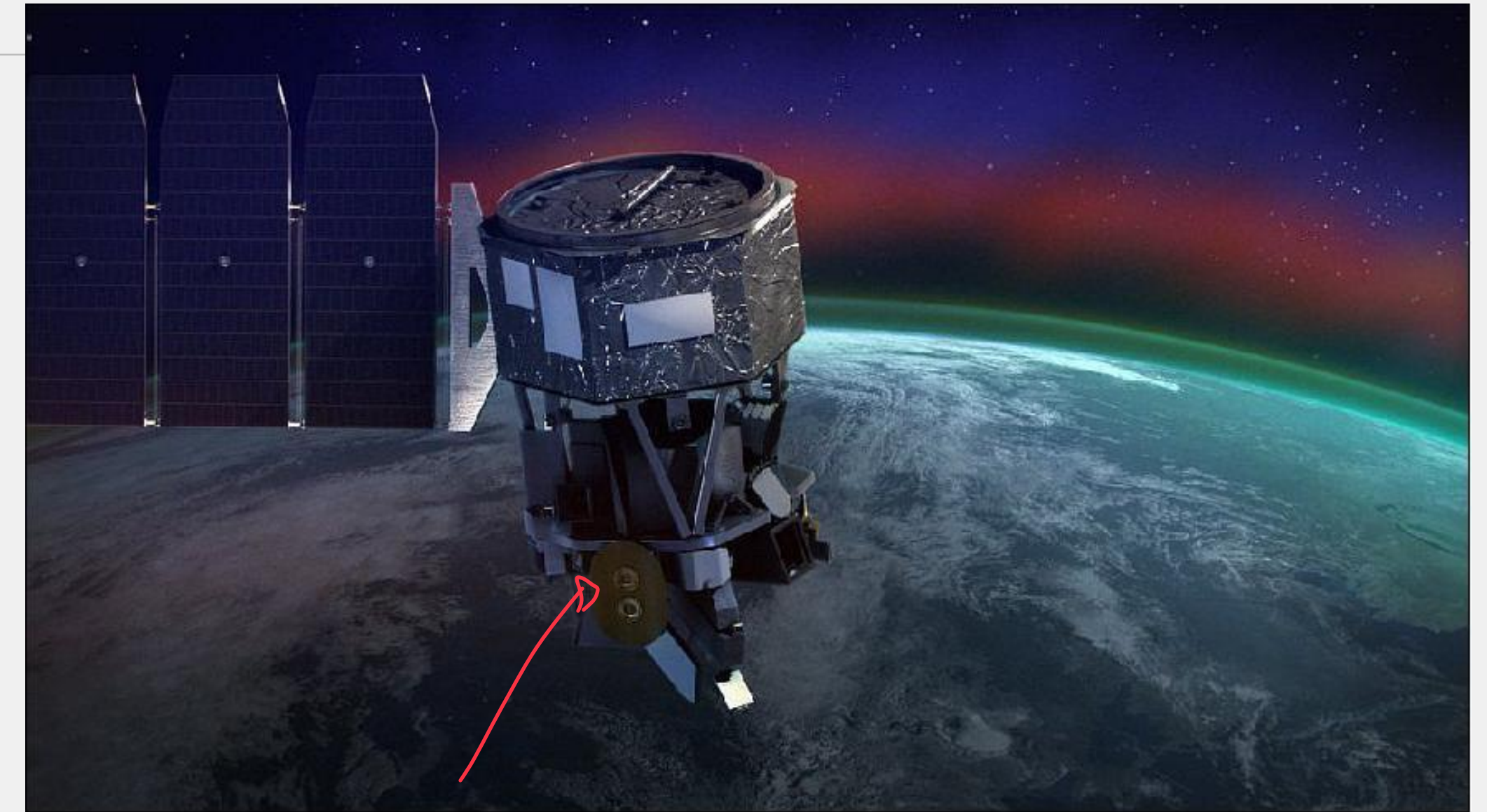
- ❖ Understand drivers of ionospheric variability
- ❖ Explain how energy / momentum from lower atmosphere reach the space environment (e.g. gravity waves!)
- ❖ Explain how drivers create extreme conditions observed during solar-driven geomagnetic storms



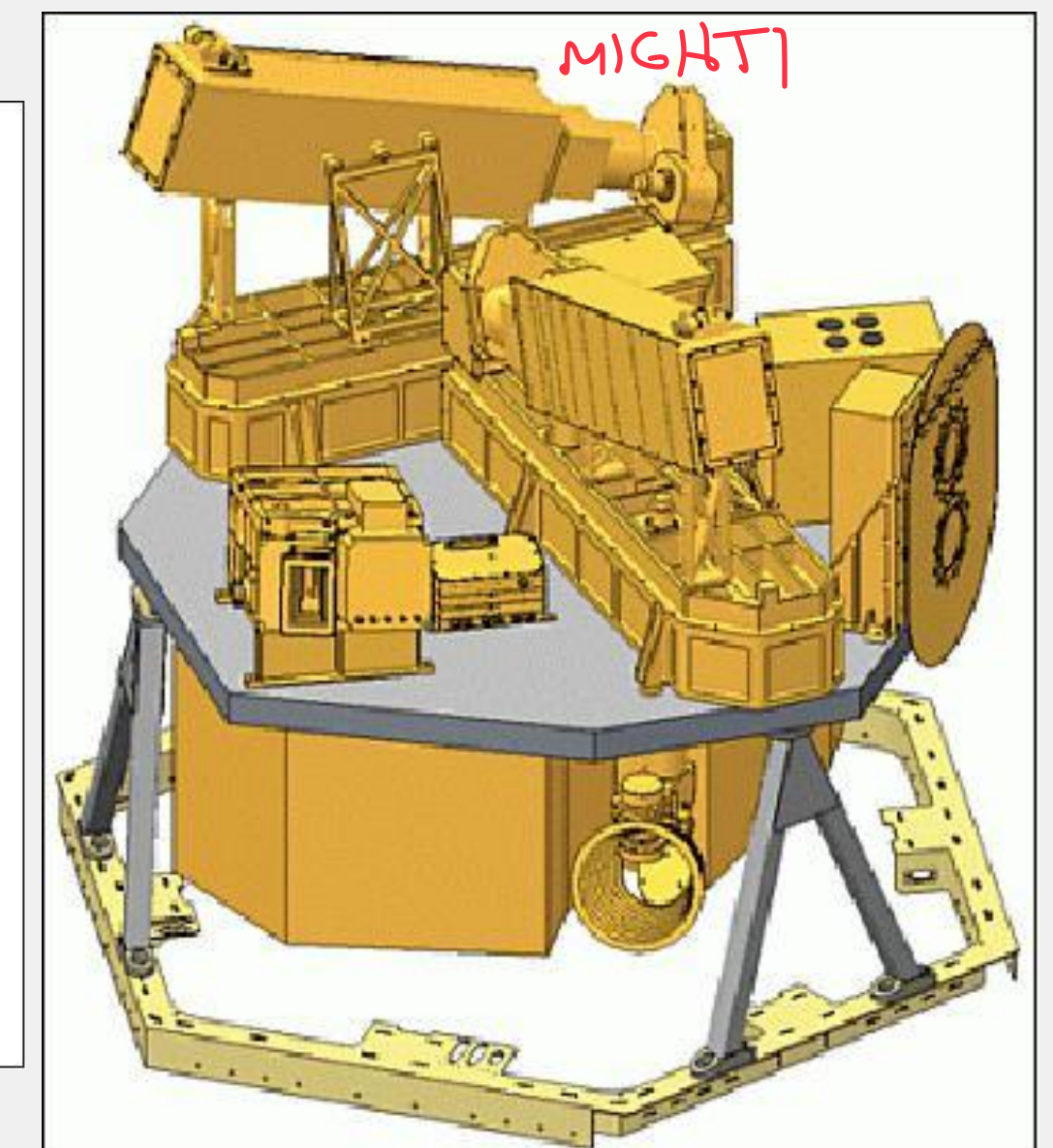


# ICON instrumentation

- ❖ Four main instruments:
  - ❖ **MIGHTI** is a Michelson Interferometer to measure winds and temperatures
  - ❖ **FUV** is an FUV imager; observes UV emissions of  $N_2$  and  $O$  to determine  $O/N_2$  ratio
  - ❖ **EUV** images 83.4 nm emission from  $O$ ; resonantly scattered by  $O^+$ : gives ion density
  - ❖ **IVM** is the ion velocity meter; uses a Retarded Potential Analyzer (RPA) to measure relative velocity of ions, therefore winds, as well as temperature and density



FUV



MIGHTI

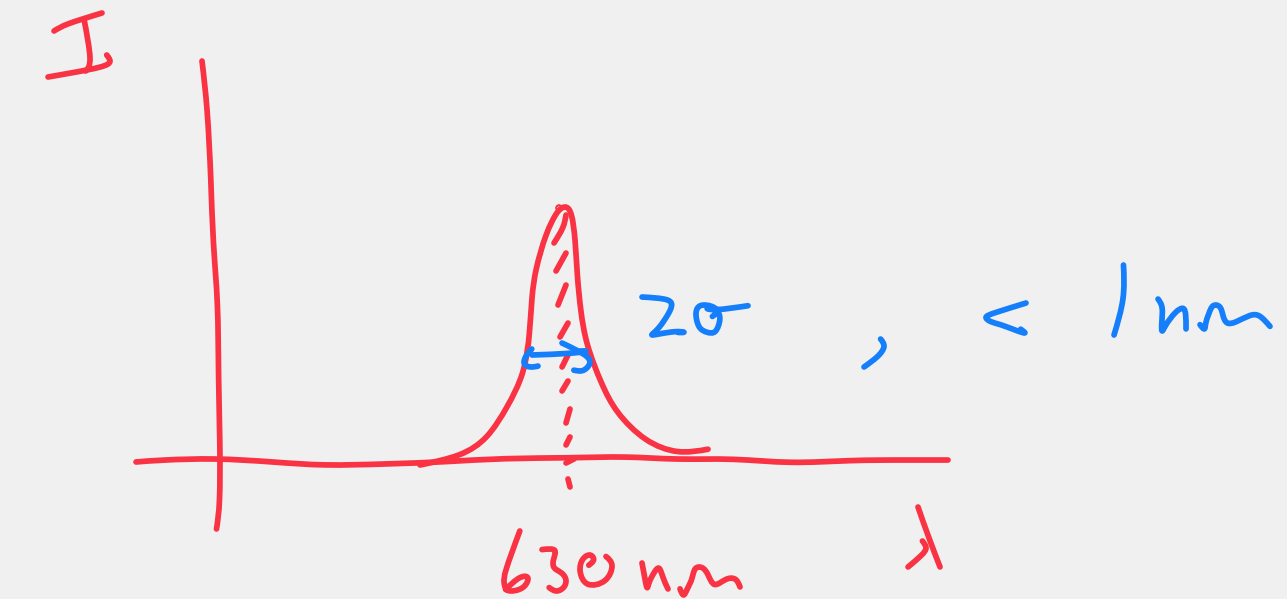


# How do you get temperature from optical emissions?

- ❖ Line emissions: atomic oxygen has emission lines at 630.0 nm and 557.7 nm (red and green lines)
- ❖ If the O atoms were completely stationary, emissions would always be at exactly these wavelengths
- ❖ O atoms are not stationary; have some velocity in random directions due to the gas temperature
- ❖ Atom moving at  $v'$ , relative to observer, will emit a photon that is Doppler shifted in wavelength by

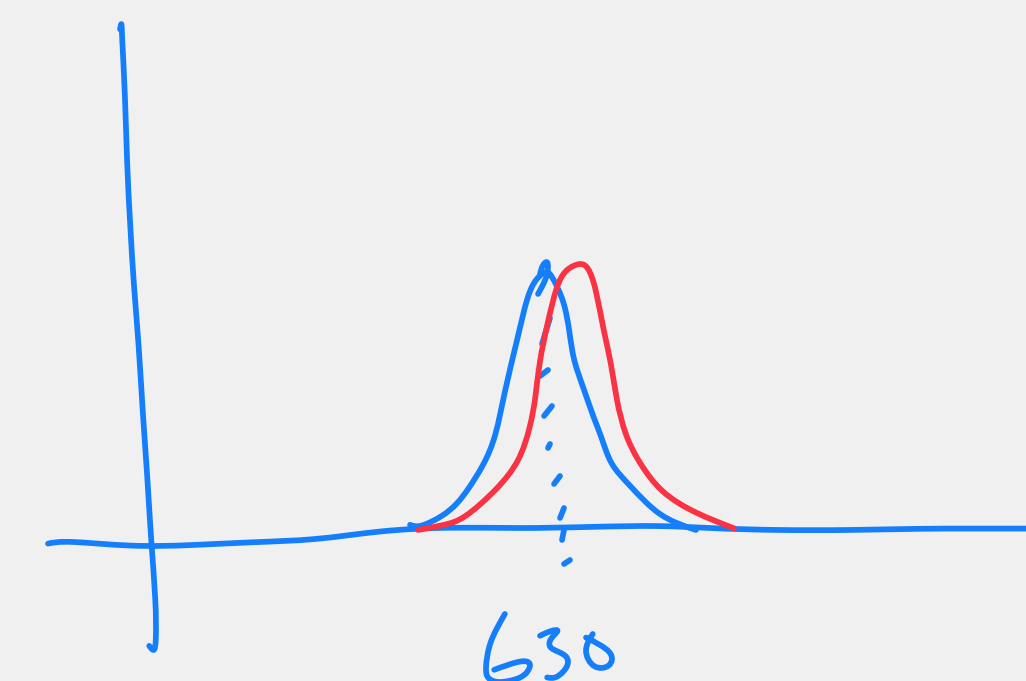
$$f' = \left(1 + \frac{v'}{c}\right) f_0$$

- ❖ Add up all the different  $v$ 's in the Maxwell-Boltzmann distribution, and you get a distribution of wavelengths that is Gaussian
- ❖ Line broadening
- ❖ Line gets broader when temperature is higher
- ❖ Need a really good spectrometer to resolve this line!



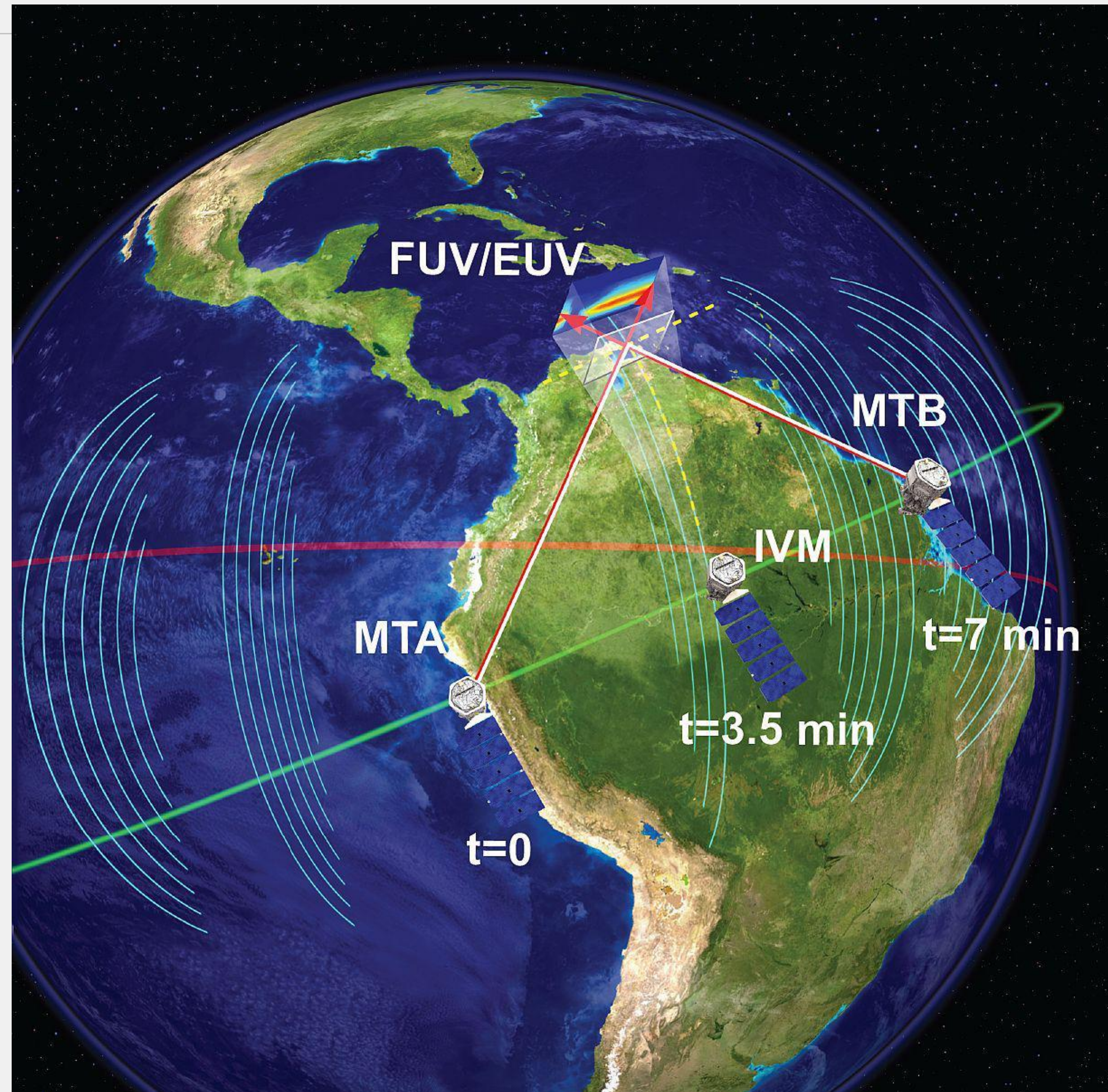
$$\sigma = \sqrt{\frac{kT}{m_e c^2}} f_0,$$

$$f_0 = c/\lambda$$



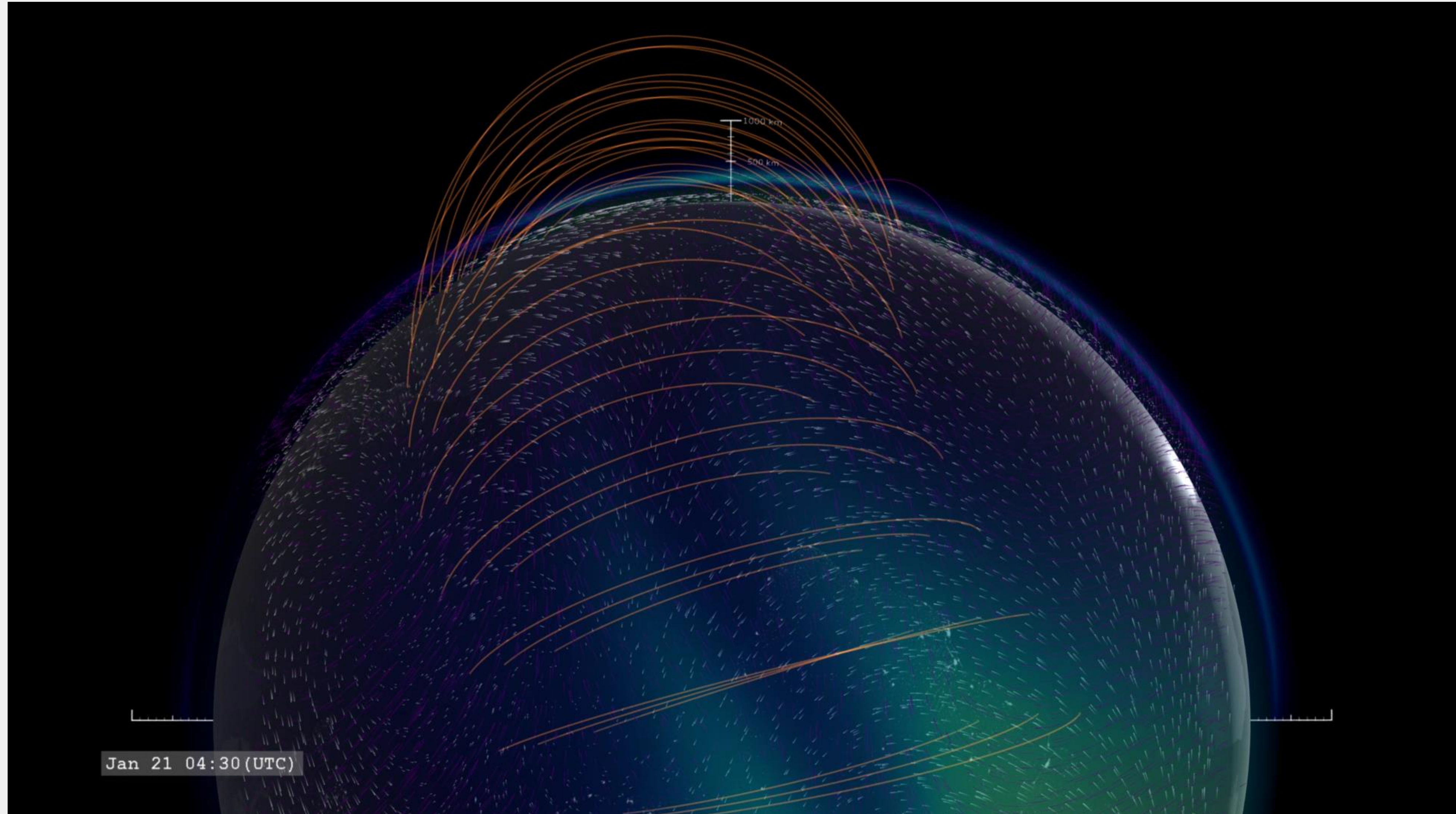


# ICON CONOPS





# ICON CONOPS made awesome





# A word from our sponsor

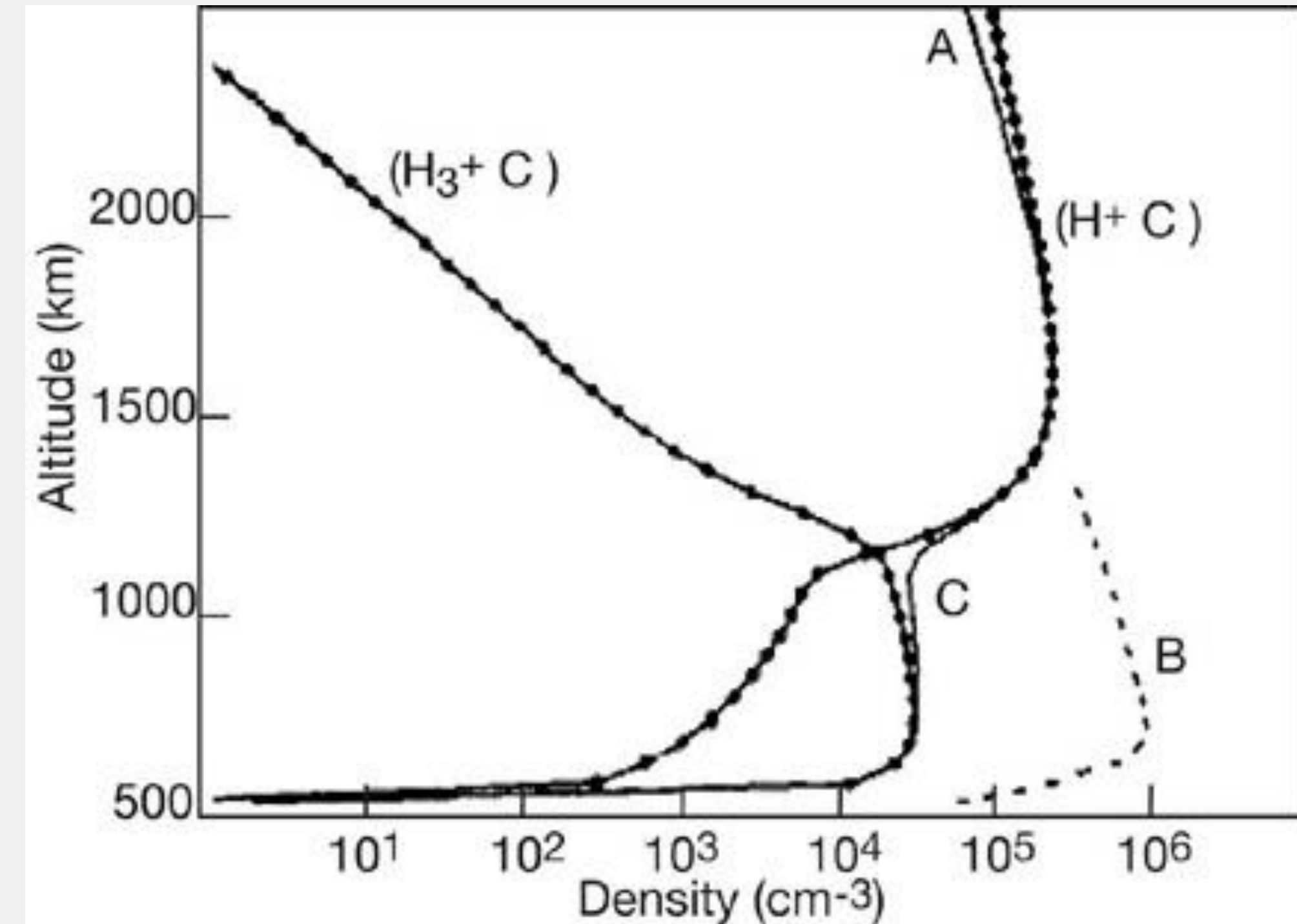
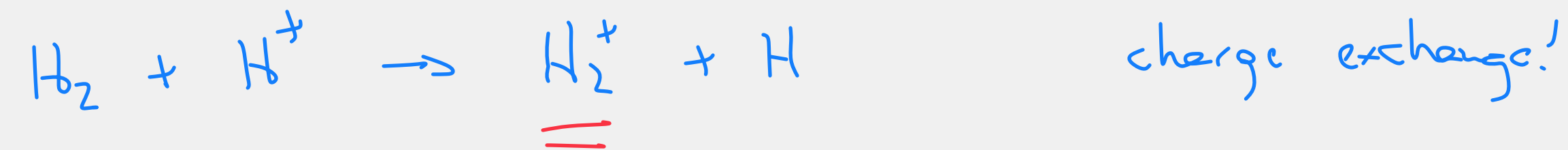
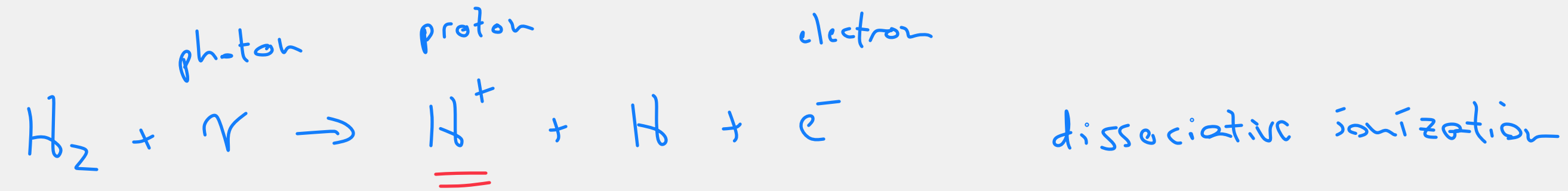


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# Comparative Ionospheres: Jupiter and Mars

# Jupiter's Ionosphere

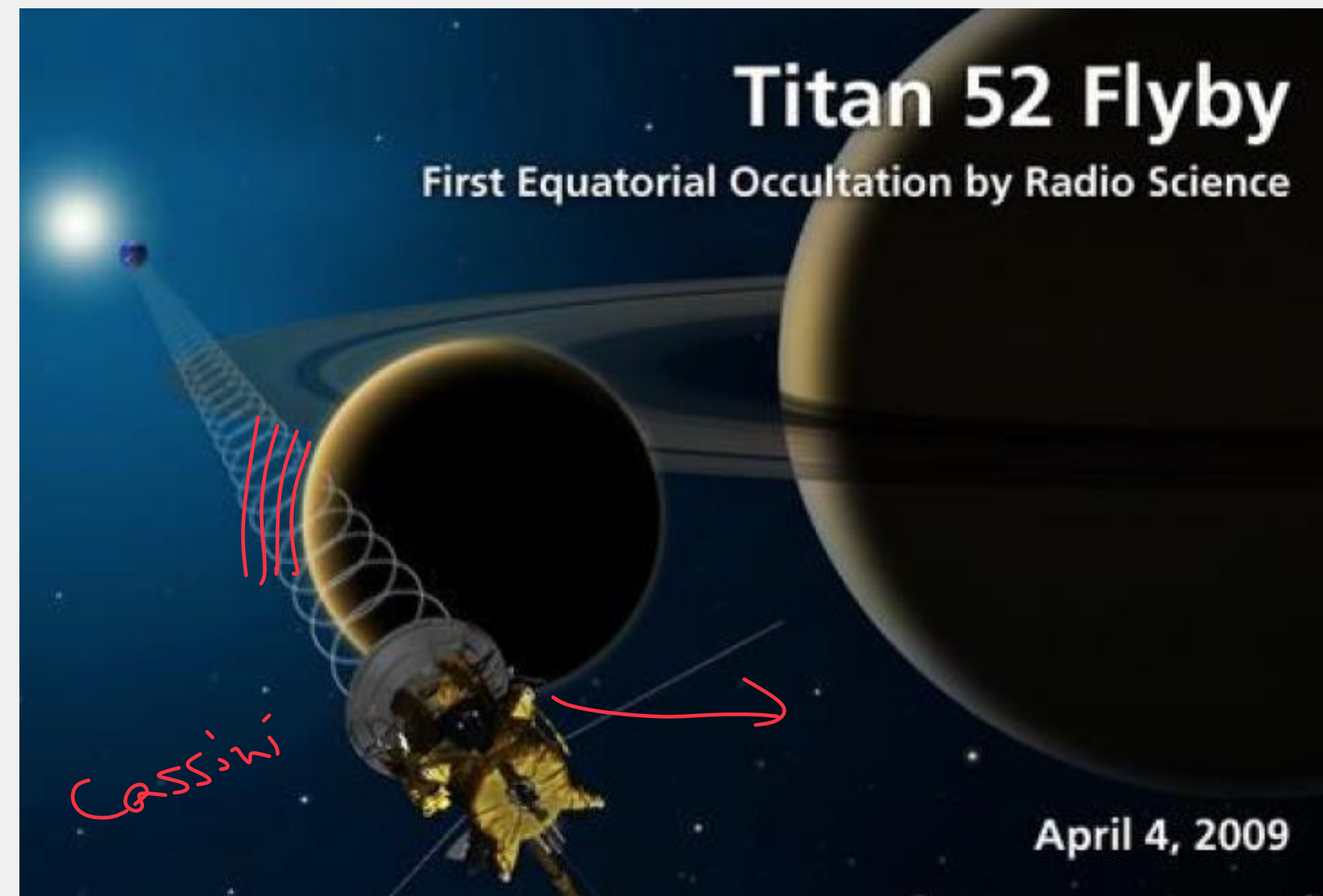
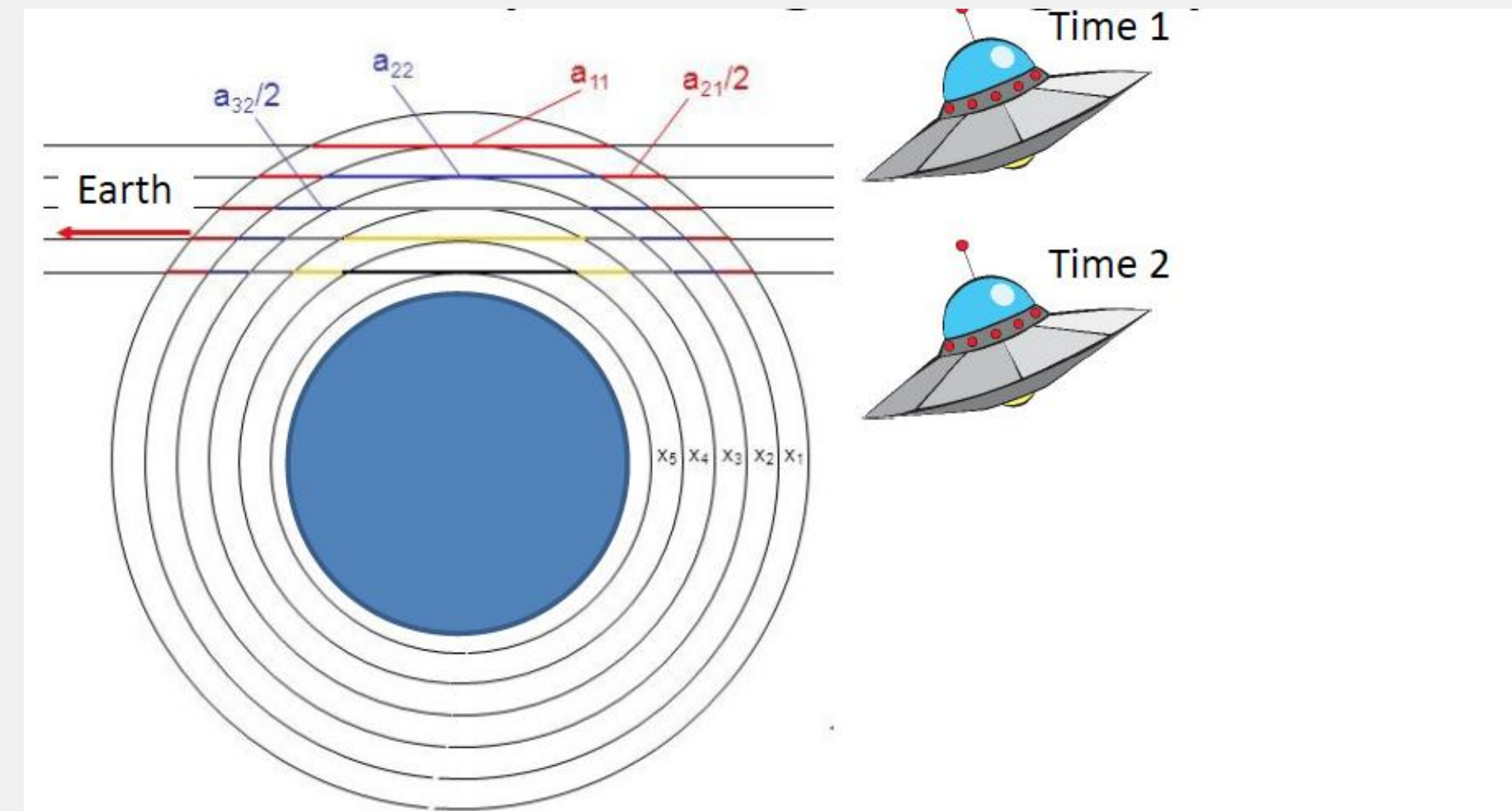
- ❖ Atmosphere is mostly  $\text{H}_2$ , so we would expect  $\text{H}_2^+$  (maybe  $\text{H}^+$ ), right?





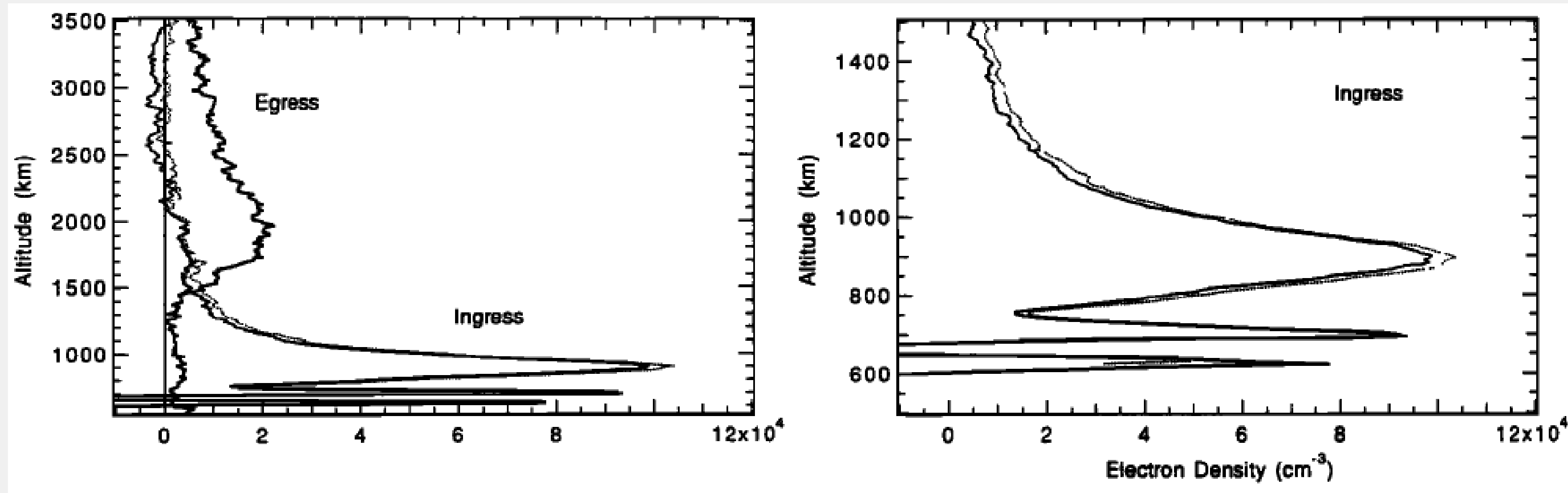
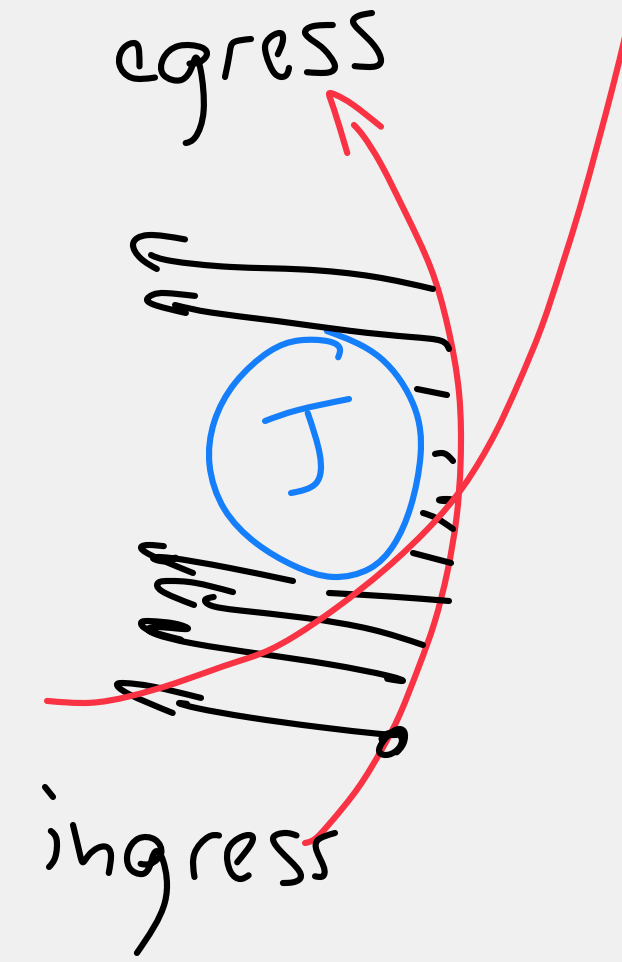
# How do we measure the ionosphere?

- ❖ Transmit radio waves from spacecraft to Earth
- ❖ **As we pass behind atmosphere / ionosphere, we get:**
  - ❖ Absorption at specific frequencies: atmosphere composition
  - ❖ Refraction / ray-bending: ionosphere density
  - ❖ Faraday rotation: magnetic field strength
- ❖ **Get successive slices through atmosphere as orbit progresses**
- ❖ Big matrix inversion to determine altitude profile



# Altitude Profiles

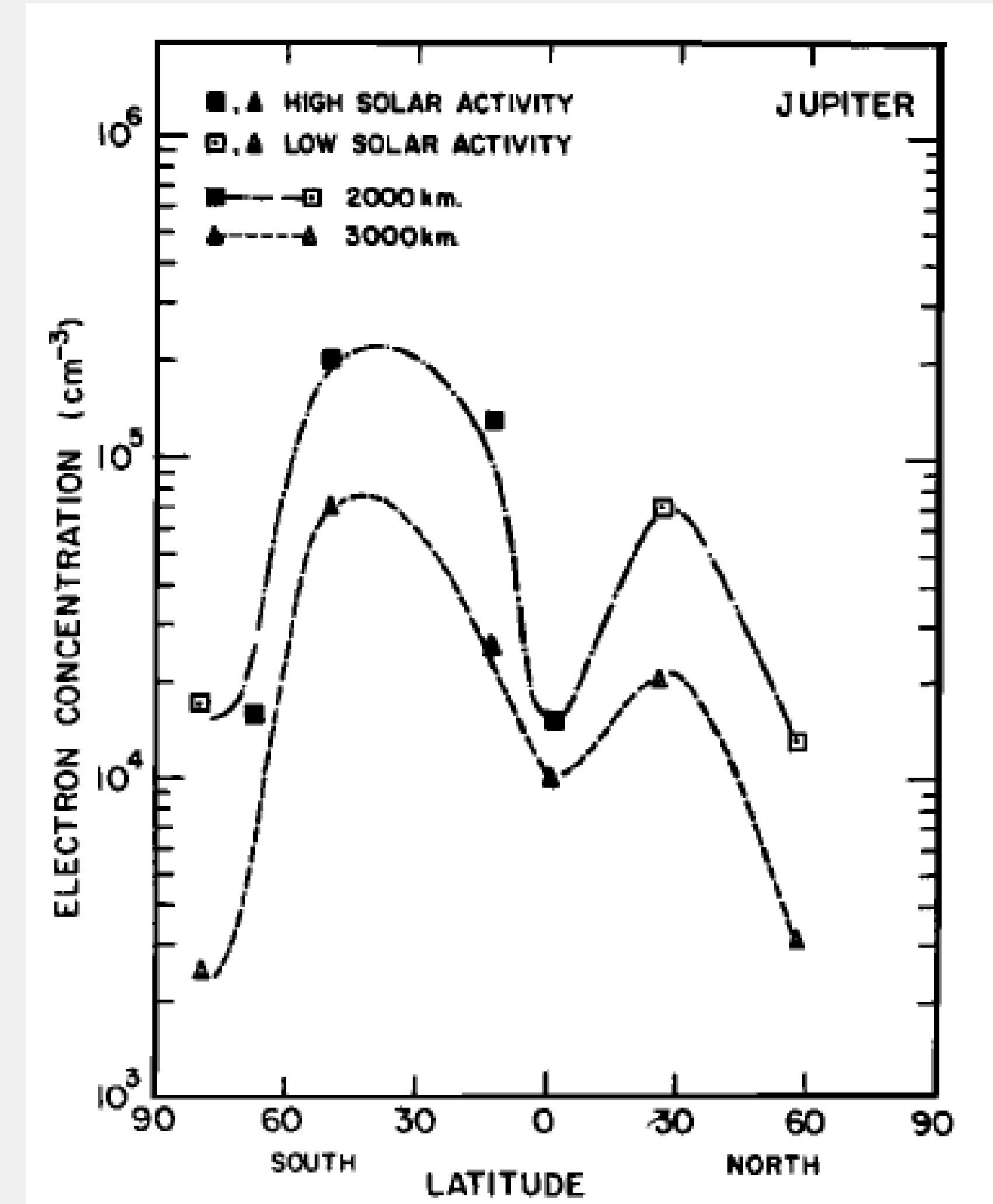
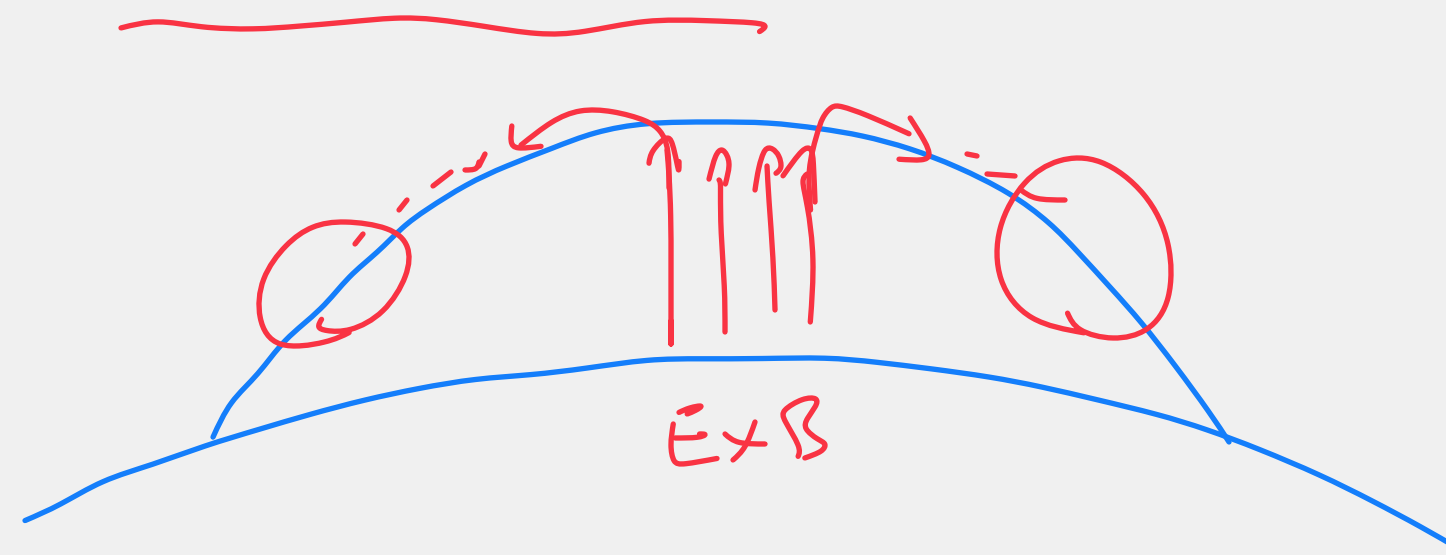
- ❖ Measured by radio occultation (Galileo spacecraft, mid-1990s)
- ❖ Ingress: passing behind planet
- ❖ Egress: emerging from behind planet
- ❖ Note very different ionospheres on the two sides of the planet!
- ❖ Lower layers potentially due to gravity waves, or other plasma processes





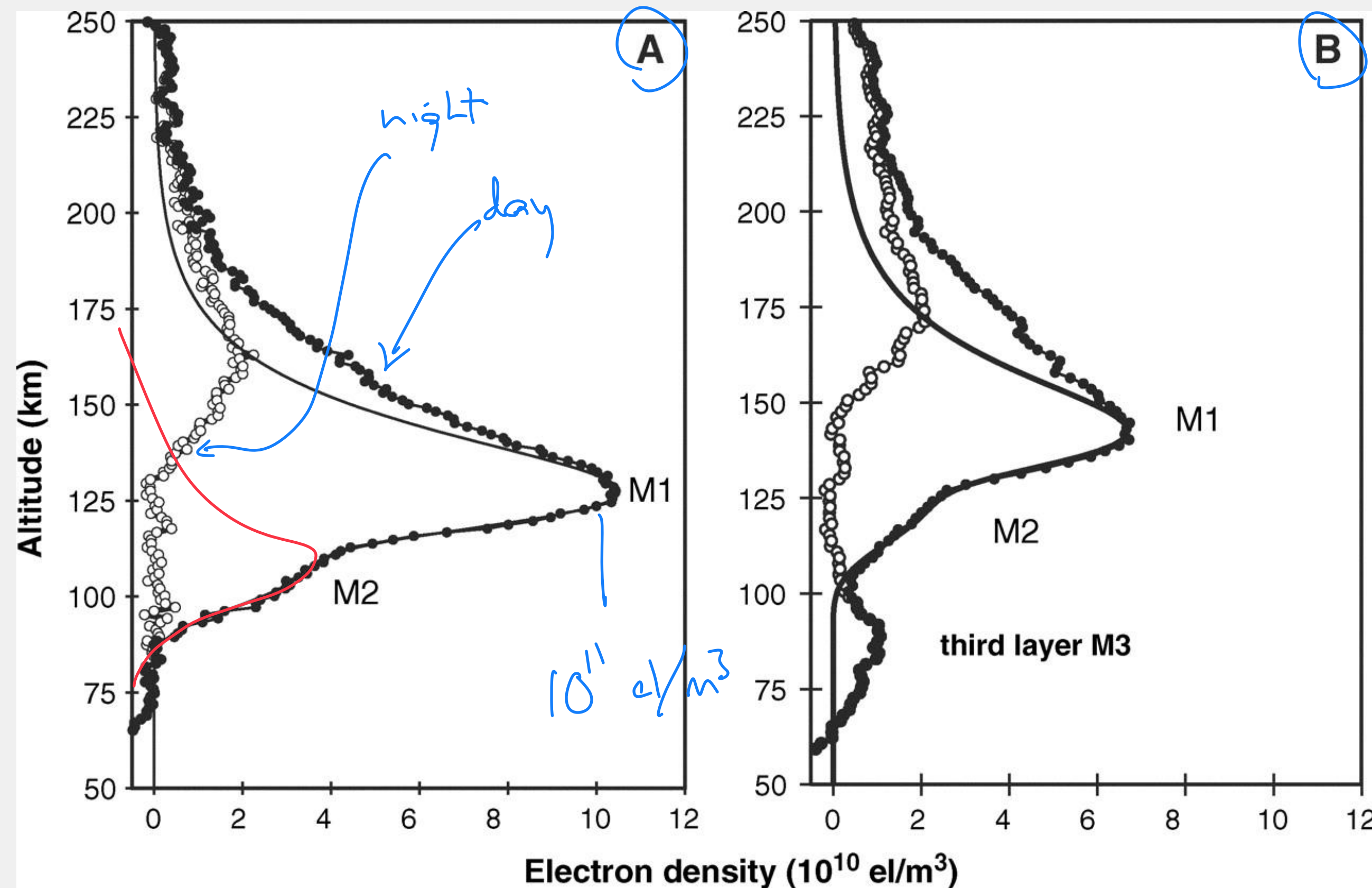
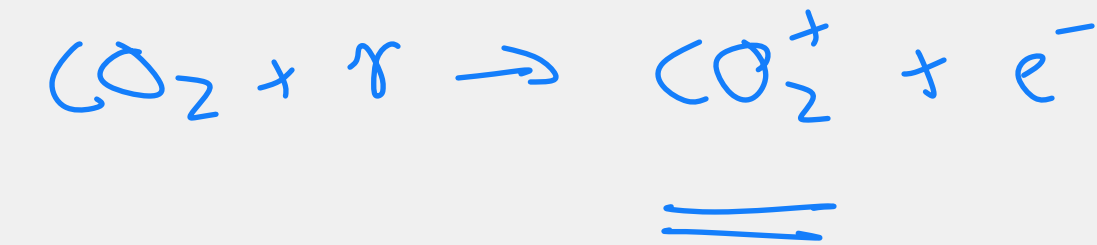
# Other Features in Jupiter's Ionosphere?

- ❖ Jupiter has a nice strong magnetosphere similar in structure to Earth's
- ❖ The magnetic field is important in the ionosphere, producing interesting plasma phenomena:
  - ❖ Sporadic-E, Spread-F, the Equatorial Anomaly, Polar Cap absorption, Aurora, etc.
- ❖ We expect that many of these occur at Jupiter as well
  - ❖ Right: Equatorial Anomaly



# Mars' Ionosphere: Layers

- ❖ Mars' Ionosphere forms the same way as Earth's: product of solar radiation (EUV) and molecules to ionize
- ❖ Good fit to a Chapman layer

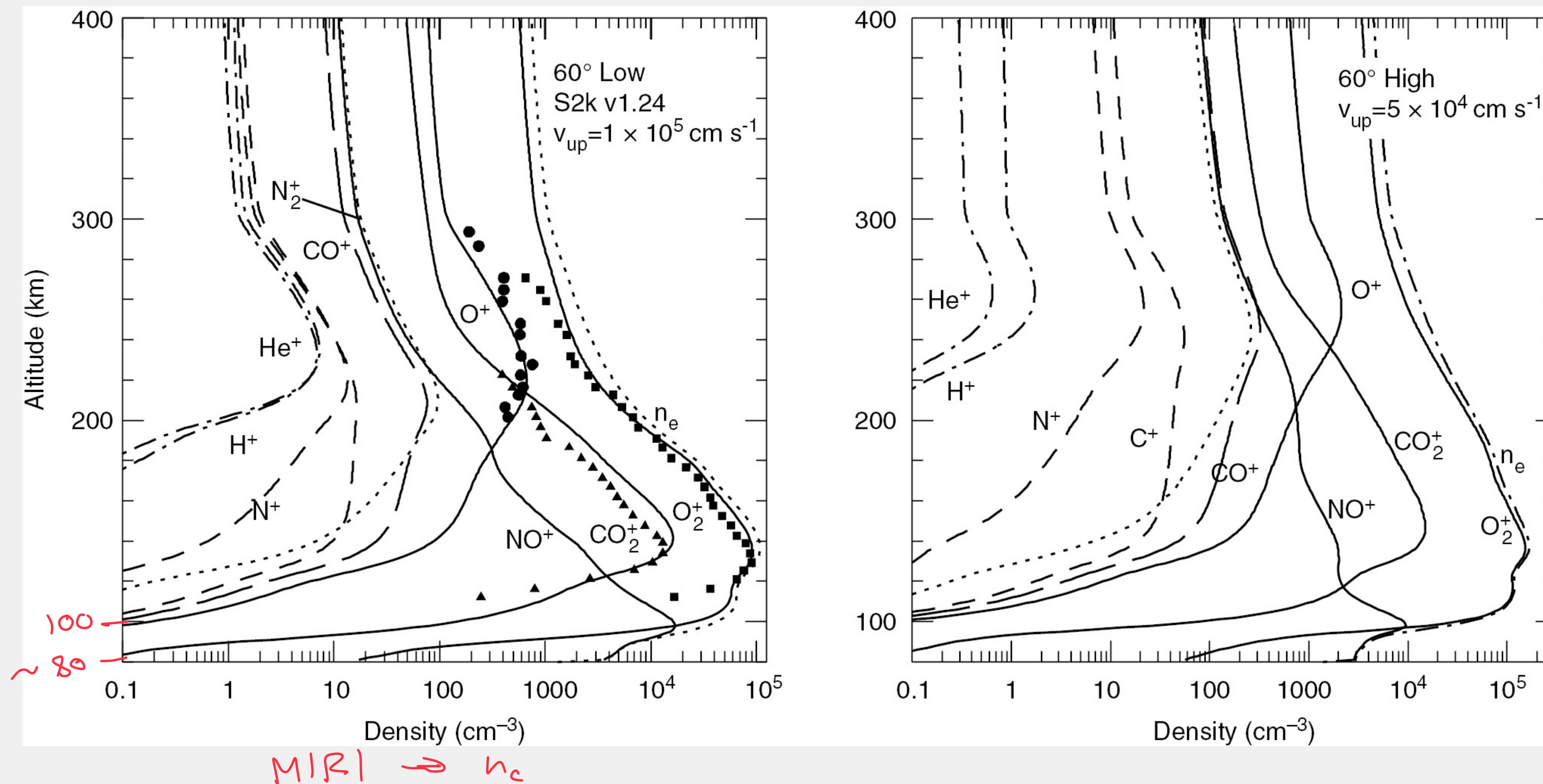


$$\frac{dn_e}{dt} = P - L$$
$$L = \alpha n_e^2$$
$$L = \alpha n_e n_i$$



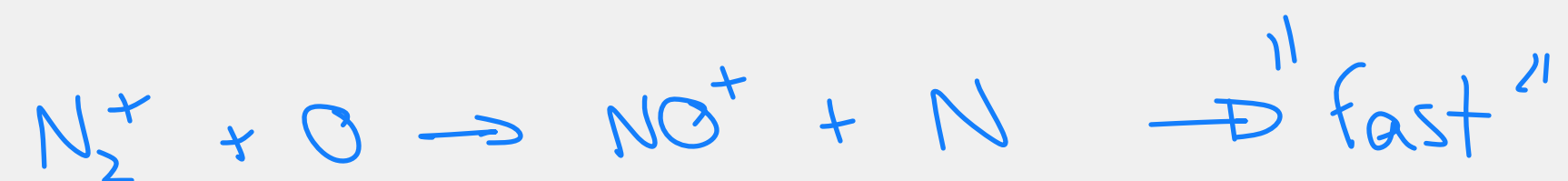
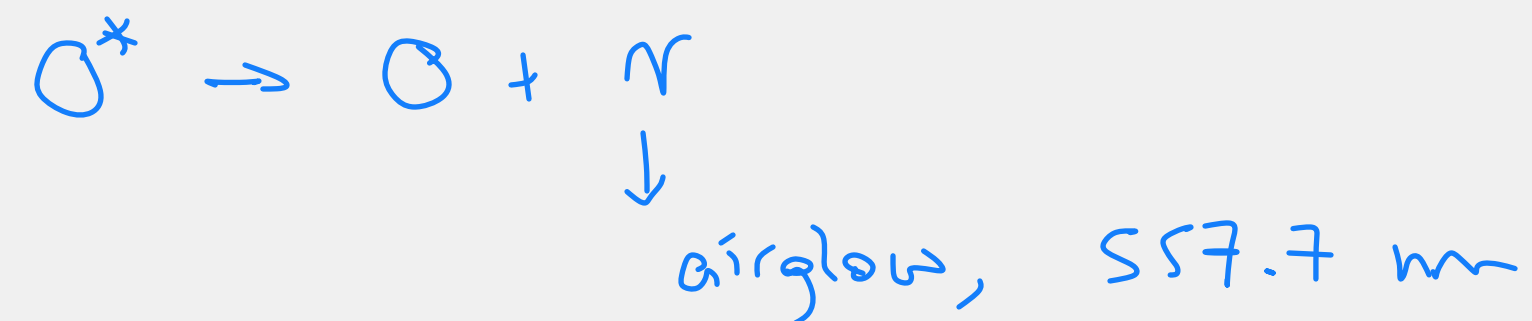
# Ionosphere density and composition

- ❖ Electron density peaks at about  $10^{11}$  electrons/m<sup>-3</sup>, at about 150 km altitude
- ❖ Ion composition is about 90% O<sub>2</sub><sup>+</sup> and 10% CO<sub>2</sub><sup>+</sup>
- ❖ Some O<sup>+</sup> at higher altitudes



# Mars Ionosphere Chemistry

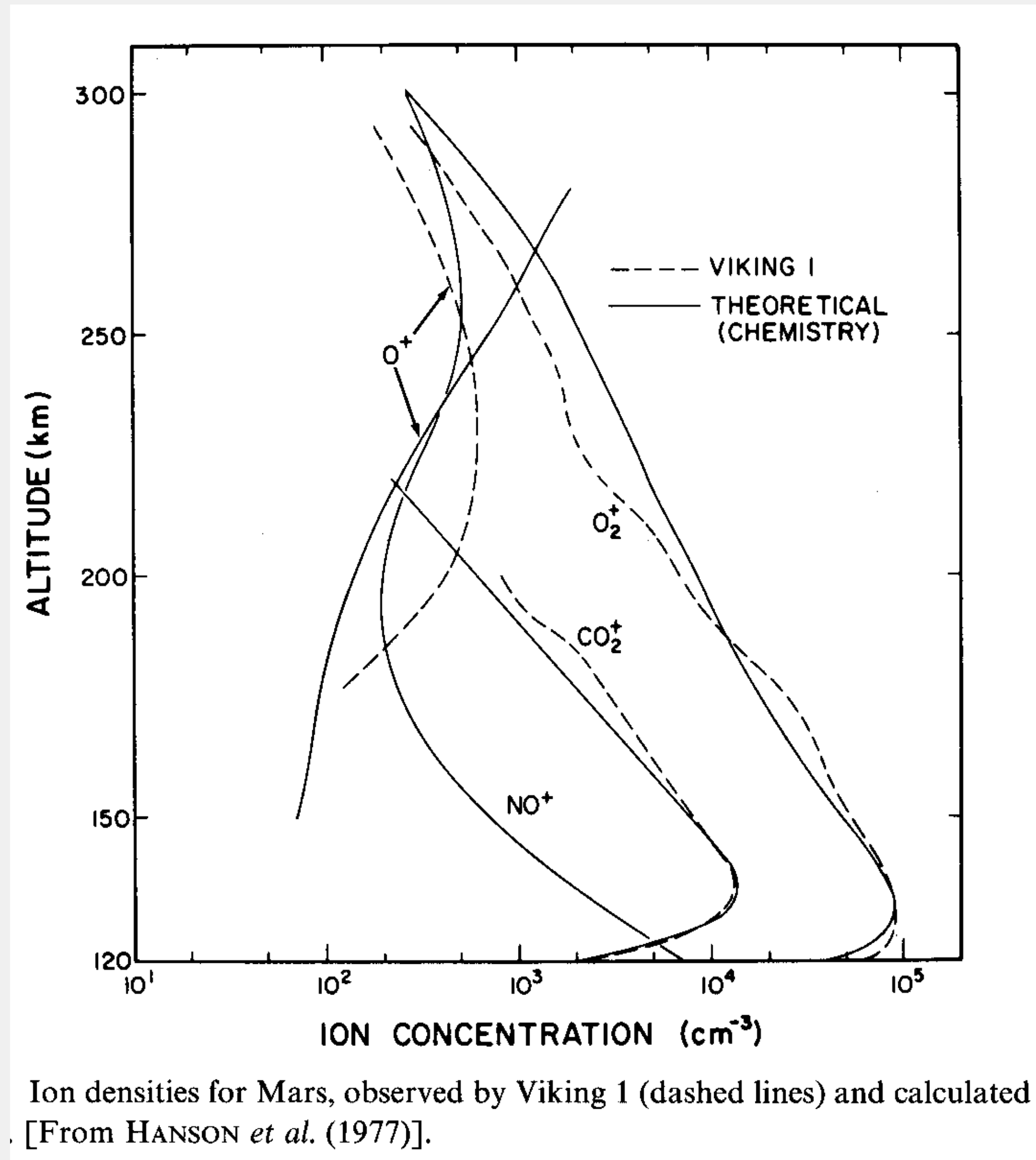
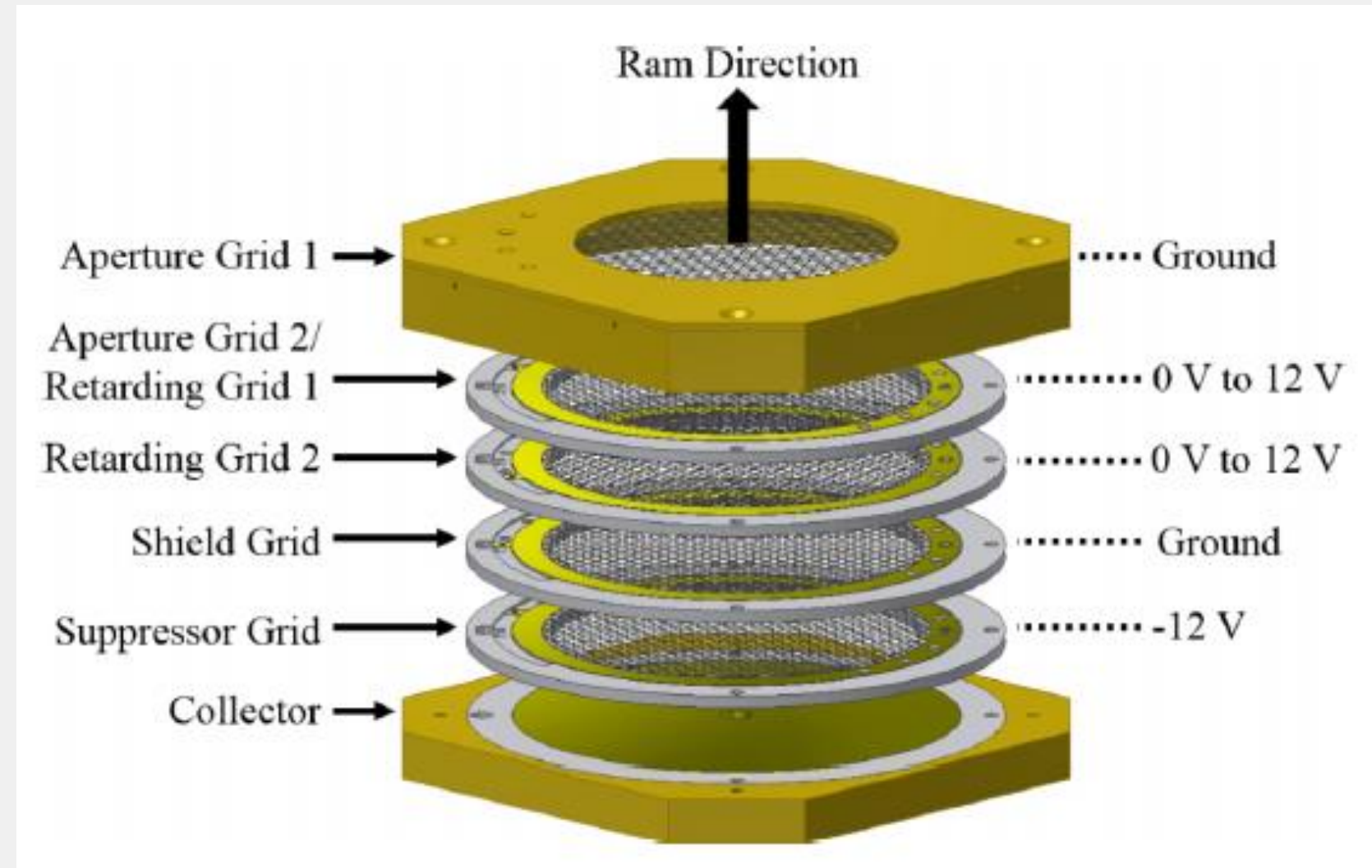
- ❖ How do we get  $O_2^+$  despite not having much oxygen?





# Viking Measurements

- ❖ Viking 1 and 2 landers took measurements of the ion densities and composition during descent to planet's surface
- ❖ Use Retarding Potential Analyzer (RPA) technique

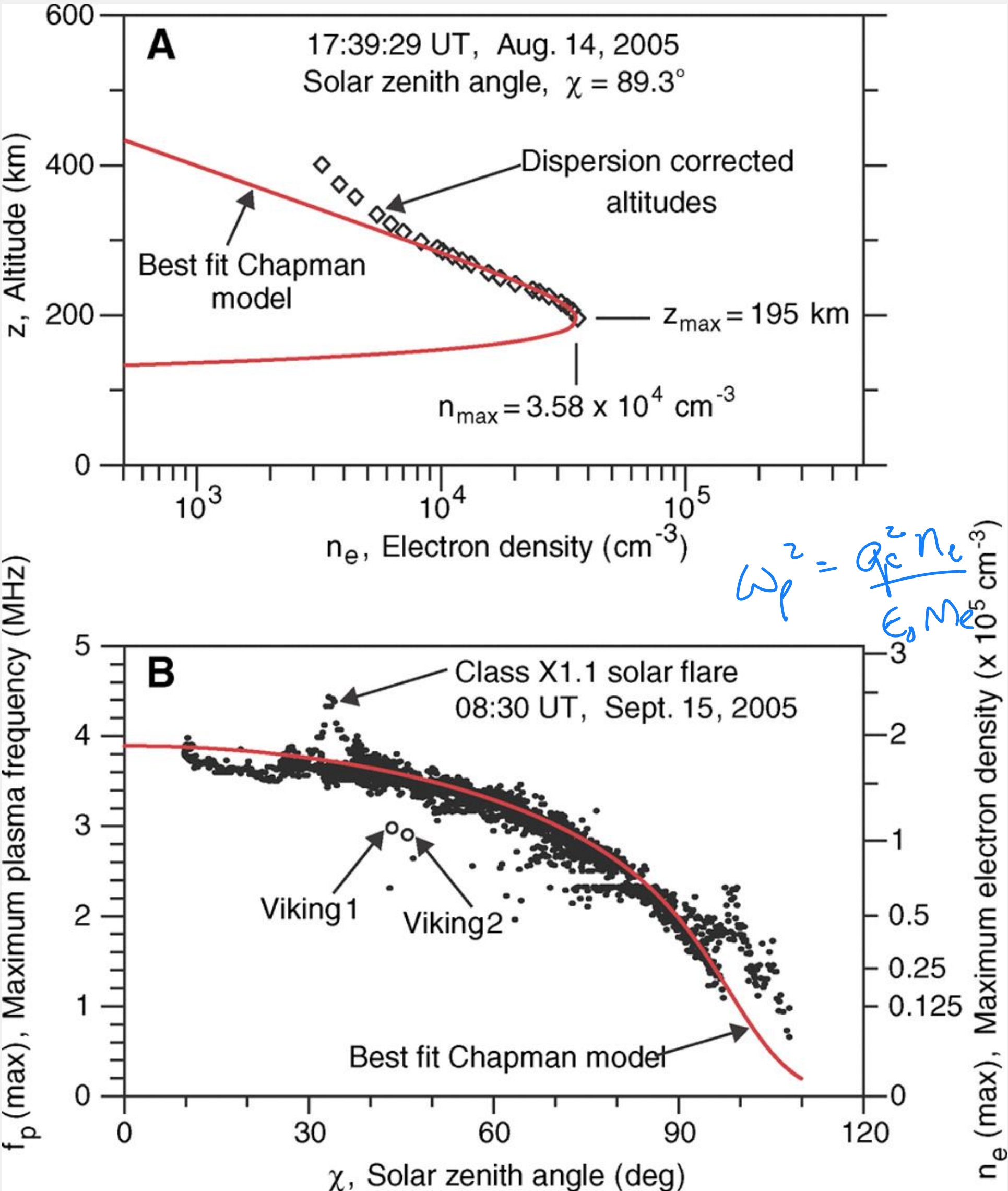
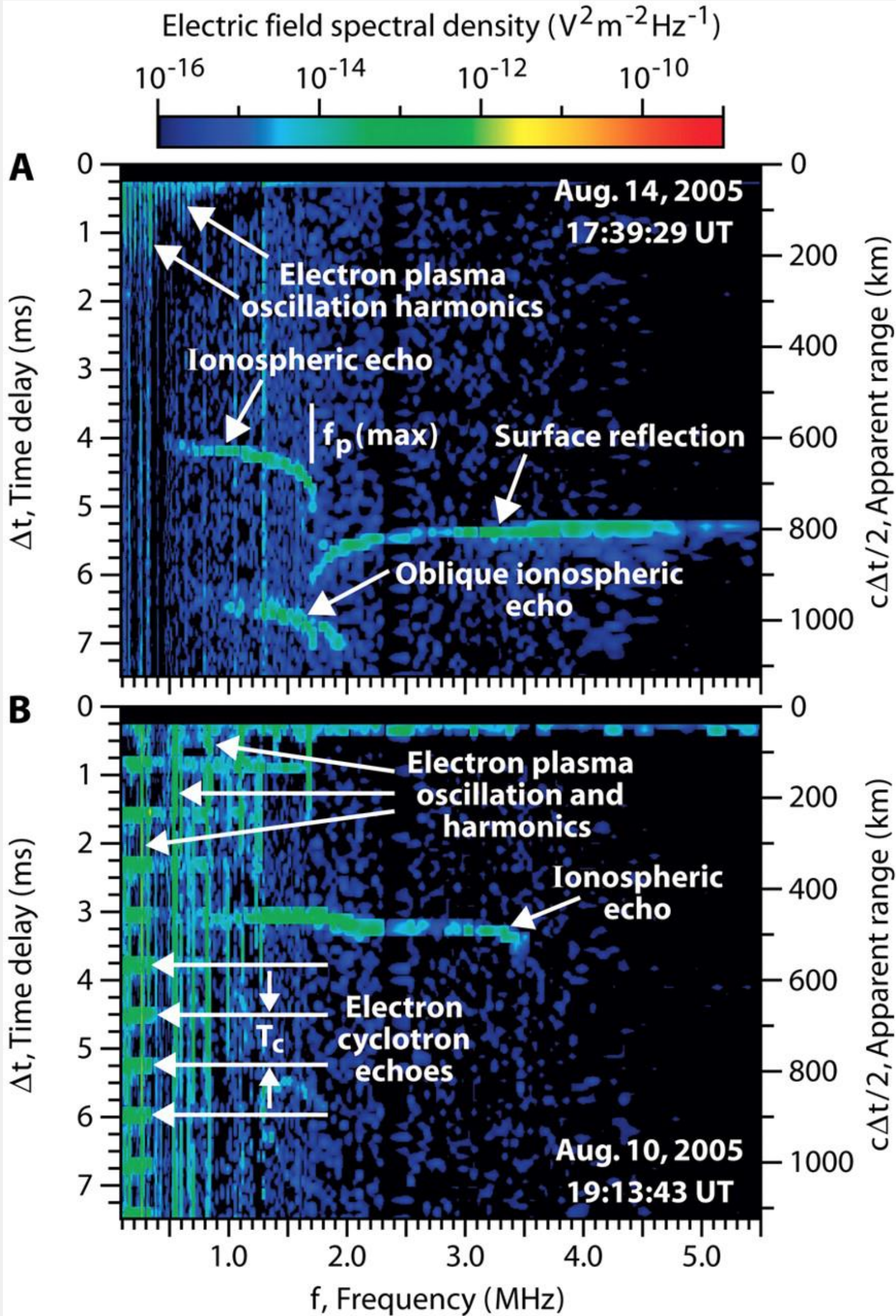




# Radar Measurements

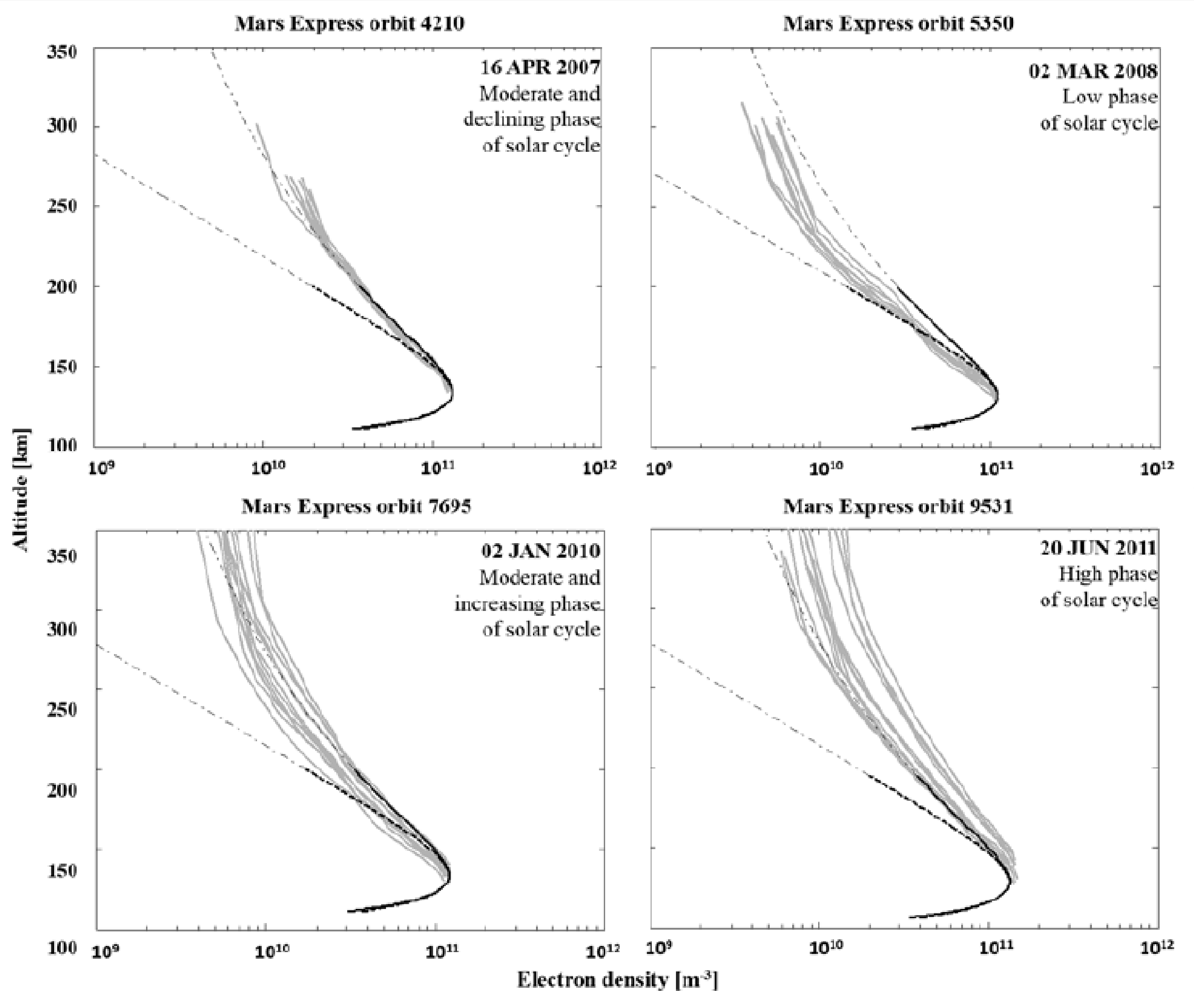
: from orbiter

Mars Global Surveyor

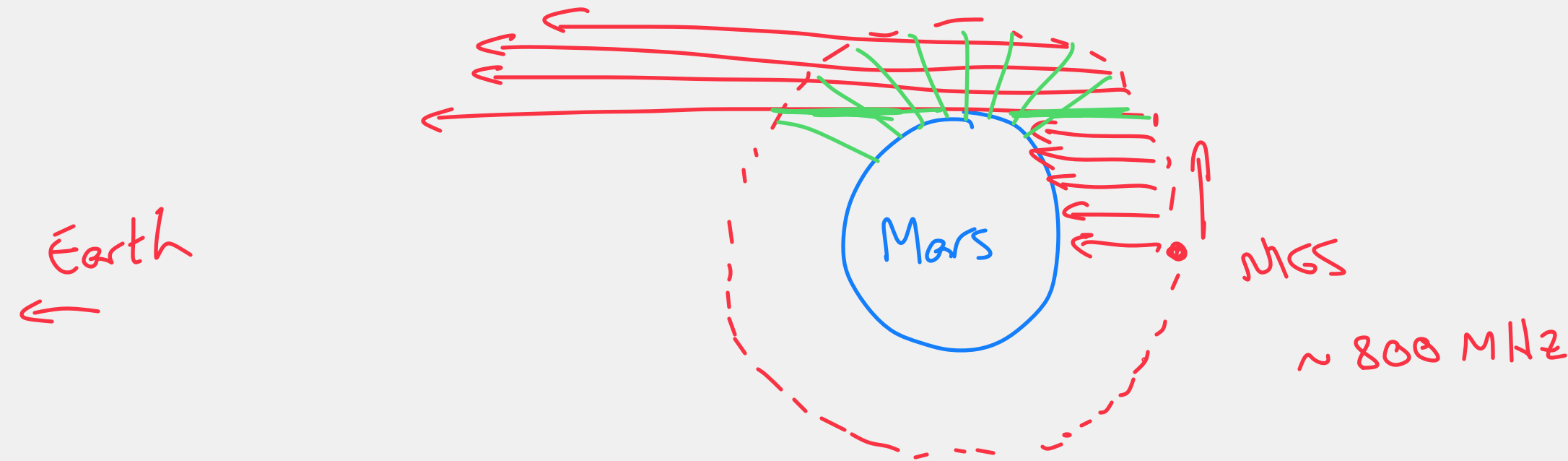




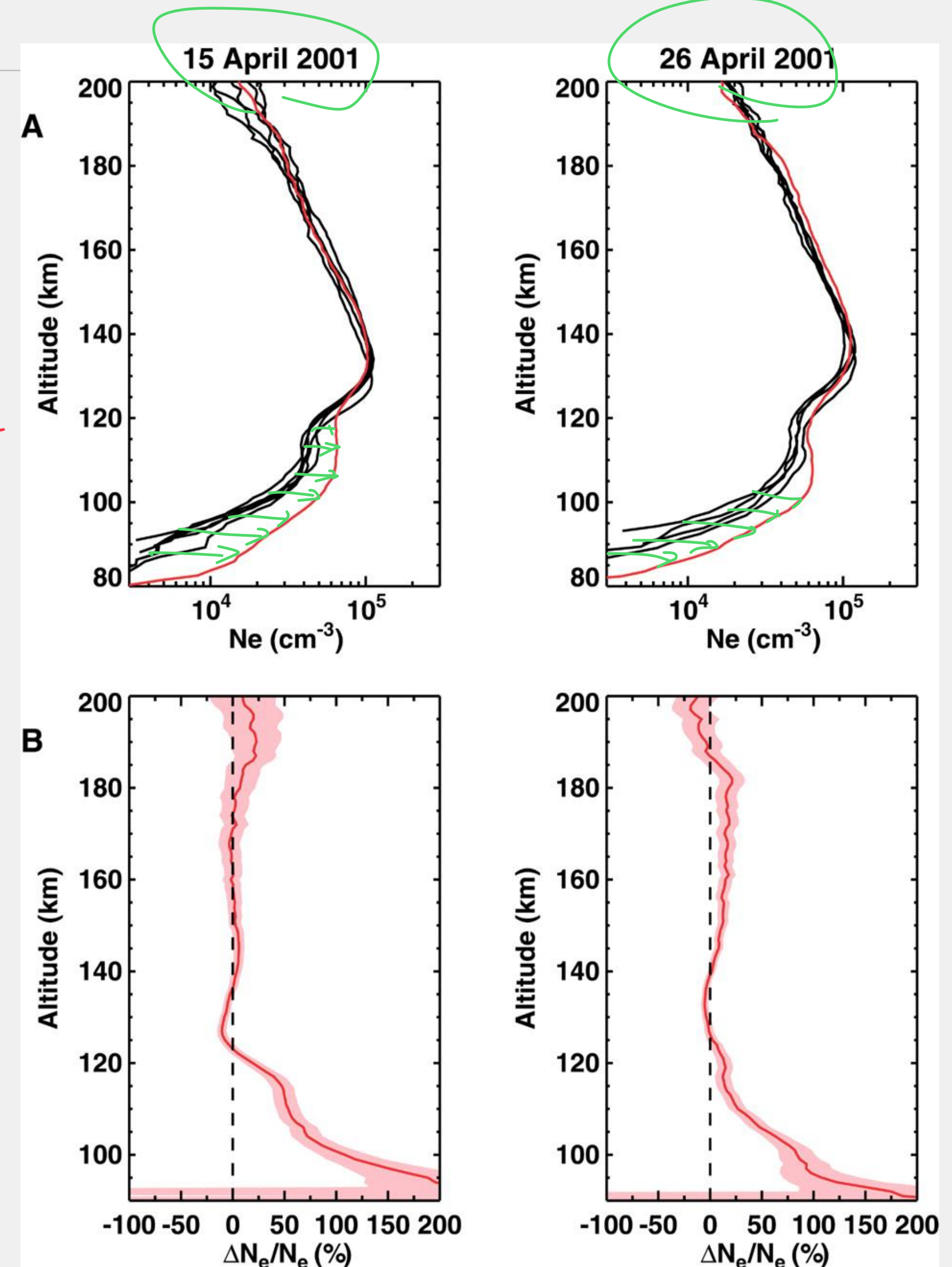
# Solar cycle variation



# Effect of Solar Flares



- ❖ from Mendillo et al 2006; Mars Global Surveyor radio occultation measurements
- ❖ Solar flare X-rays ionize the lowest part of the atmosphere (below 100 km or so)
- ❖ Harder x-rays reach deeper, close to Mars' surface
- ❖ This event (right) probably mostly soft x-rays (a few keV)





# Summary

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- ❖ Mars has an atmosphere **similar** to Earth's in many ways, but also **different**:
  - ❖ **no stratosphere** so likely no ozone layer
  - ❖ **primarily CO<sub>2</sub>** instead of N<sub>2</sub>
  - ❖ **primarily atomic oxygen (O) in thermosphere**
  - ❖ **Scale height of 11 km** compared to Earth's 8 km
  - ❖ **Homosphere and heterosphere**
- ❖ Mars has an ionosphere **similar** to Earth's in many ways:
  - ❖ Peak density **comparable** to Earth, but at **150 km altitude**
  - ❖ **Mostly O<sub>2</sub><sup>+</sup>** due to reaction  $\text{CO}_2^+ + \text{O} \rightarrow \text{CO} + \text{O}_2^+$
  - ❖ Variability with solar cycle and solar flares
  - ❖ Same effect on radio wave propagation